autorob.org

EECS 367
Intro. to Autonomous Robotics

ROB 320
Robot Operating Systems

Winter 2022

Inverse Kinematics

Administrative

- Assignment #3: Forward Kinematics
  - Due Friday, February 18, 11:59pm
- New quiz policy
  - Late quizzes will be accepted (including quiz 1-3)
  - Late policy follows that of projects
    - Up to 80% within 2 weeks
    - 60% within 4 weeks
    - 50% by end of grading period
  - Quiz questions can’t be discussed on general slack
    - Discussion limited to direct course staff or during office hours

New Robot Definition

- Feature for assignment 3
  - Everyone will submit as a pair of students
  - You can choose pairs or come to interactive session
- Next Wednesday, February 16th
  - Dedicated course time for paired programming
- Following Wednesday, February 23rd
  - Every team will showcase their robot during interactive session (with pizza!)
  - Push your new definition to “robots/new_robot_description.js" by the showcase
- 1 point for working forward kinematics
- 1 point for showcasing their robot

Is your forward kinematics working?

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If yes, you can start working with real robots

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KinEval + *rosbridge*

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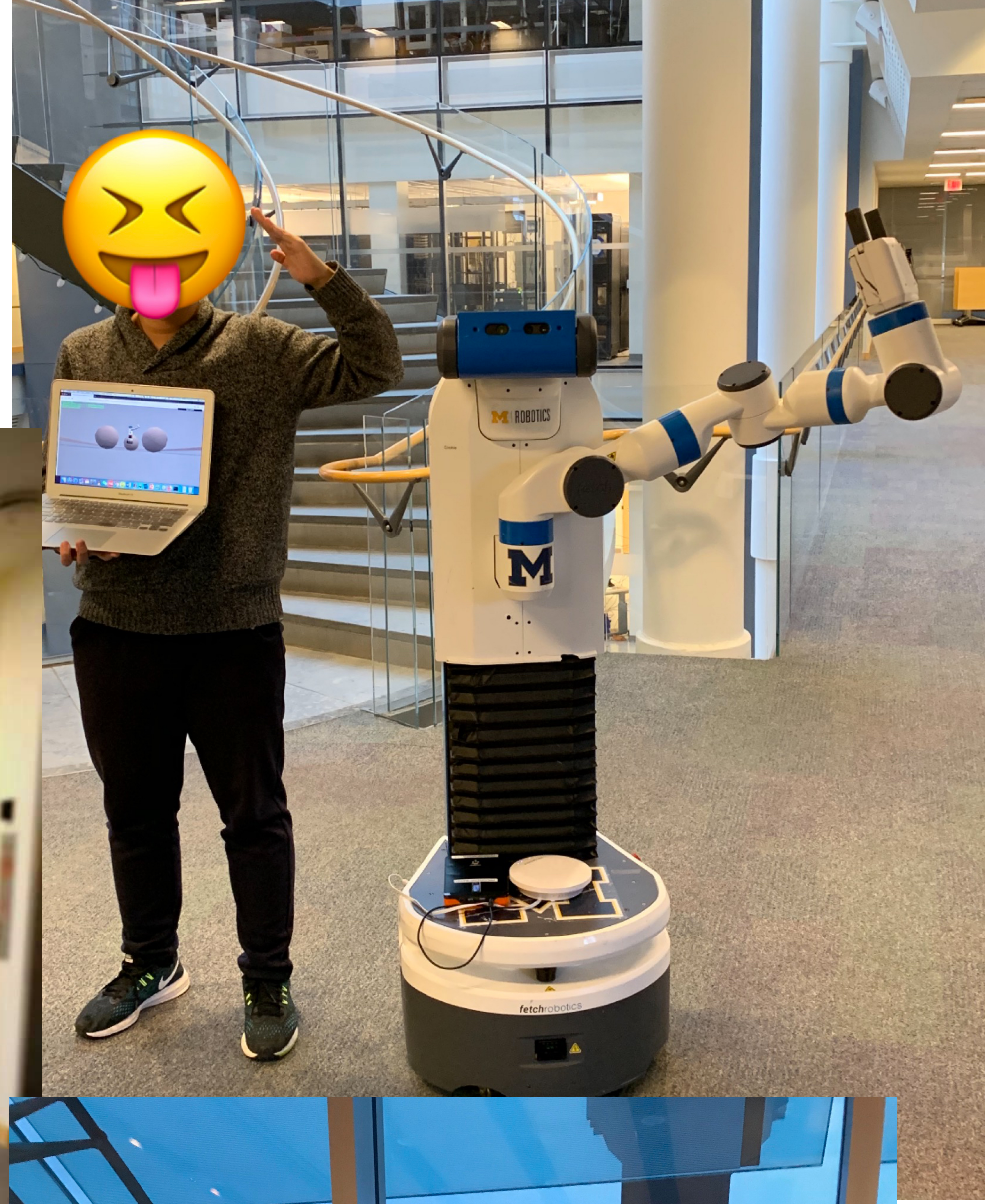
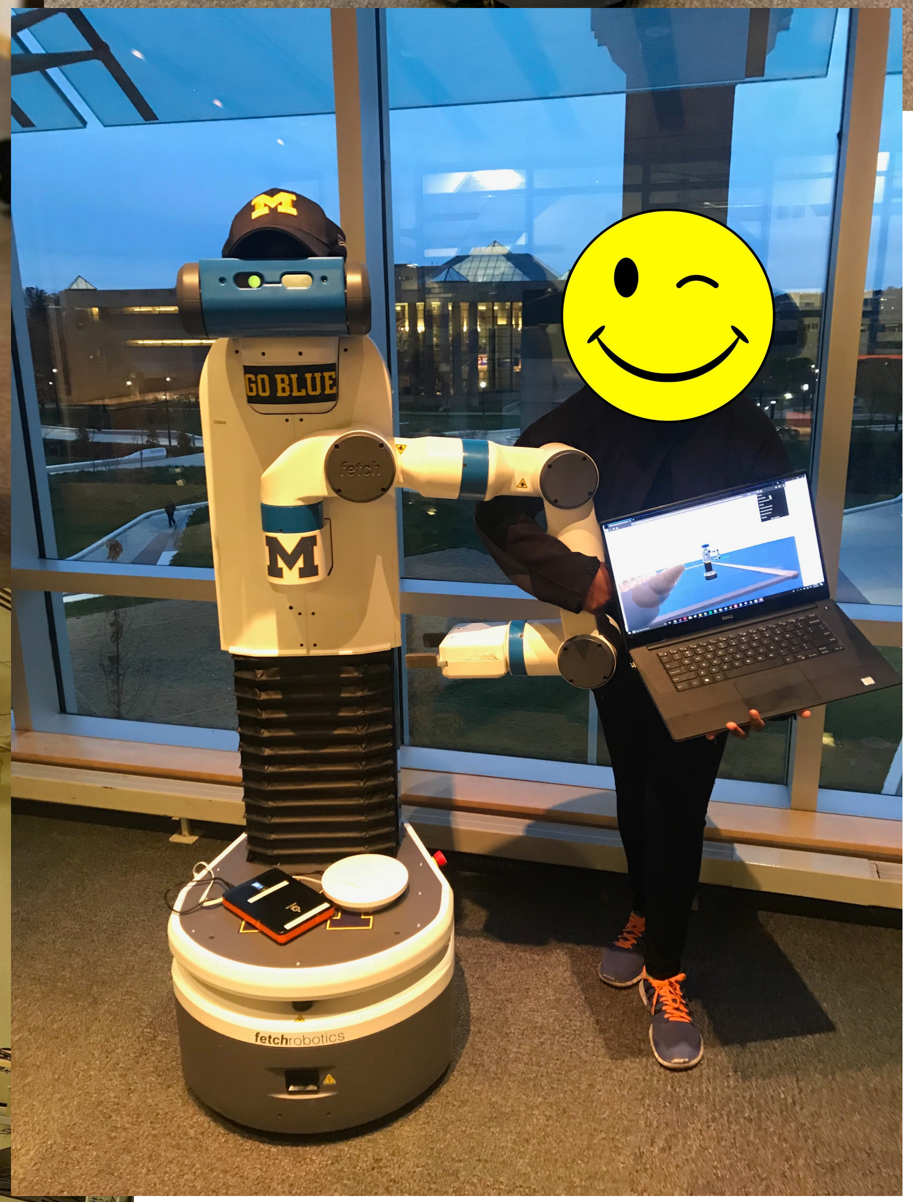
In non-COVID-19 semesters…

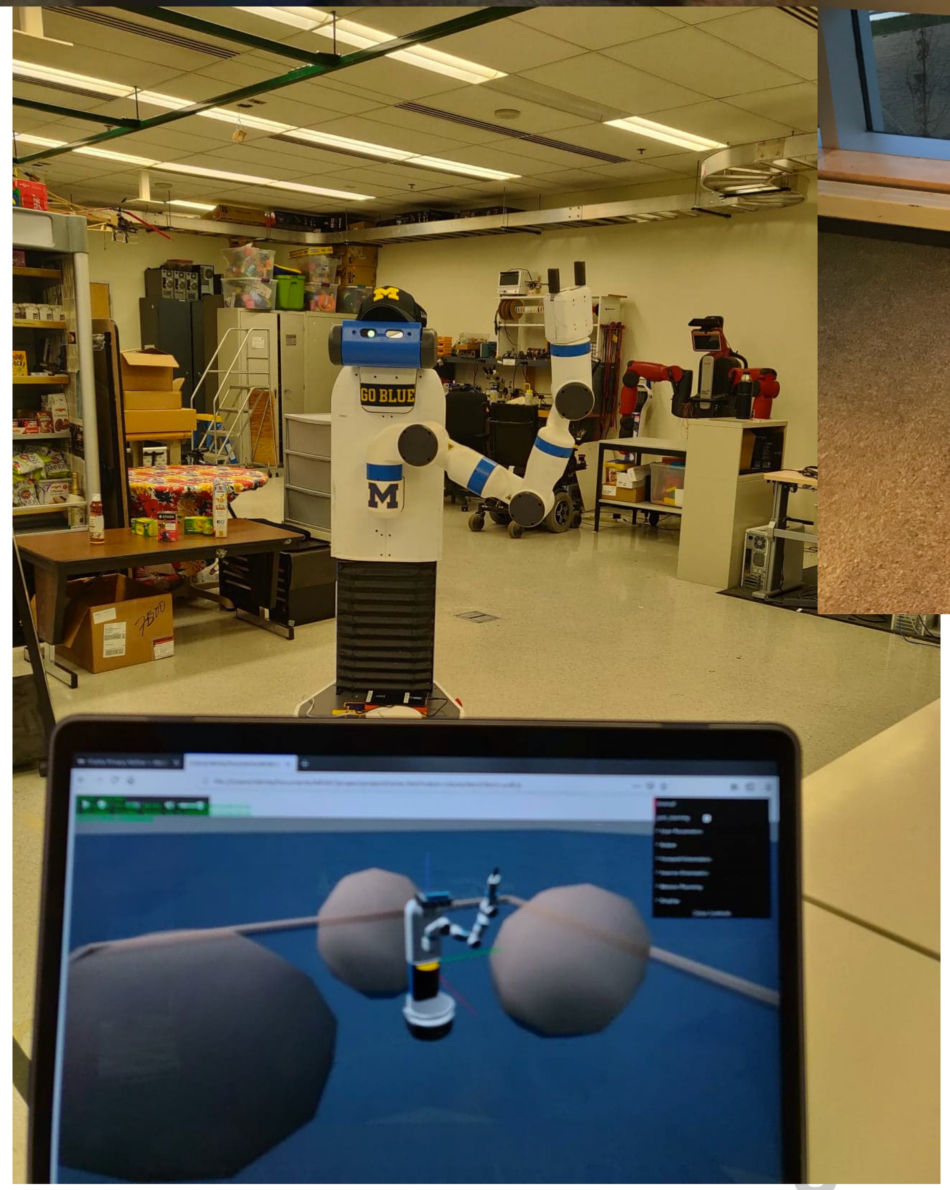
You would connect your working FK code to a real robot (Michigan Progress Fetch)

and take a picture together

For those who are interested, let the course staff know over slack. This will be possibile following winter break







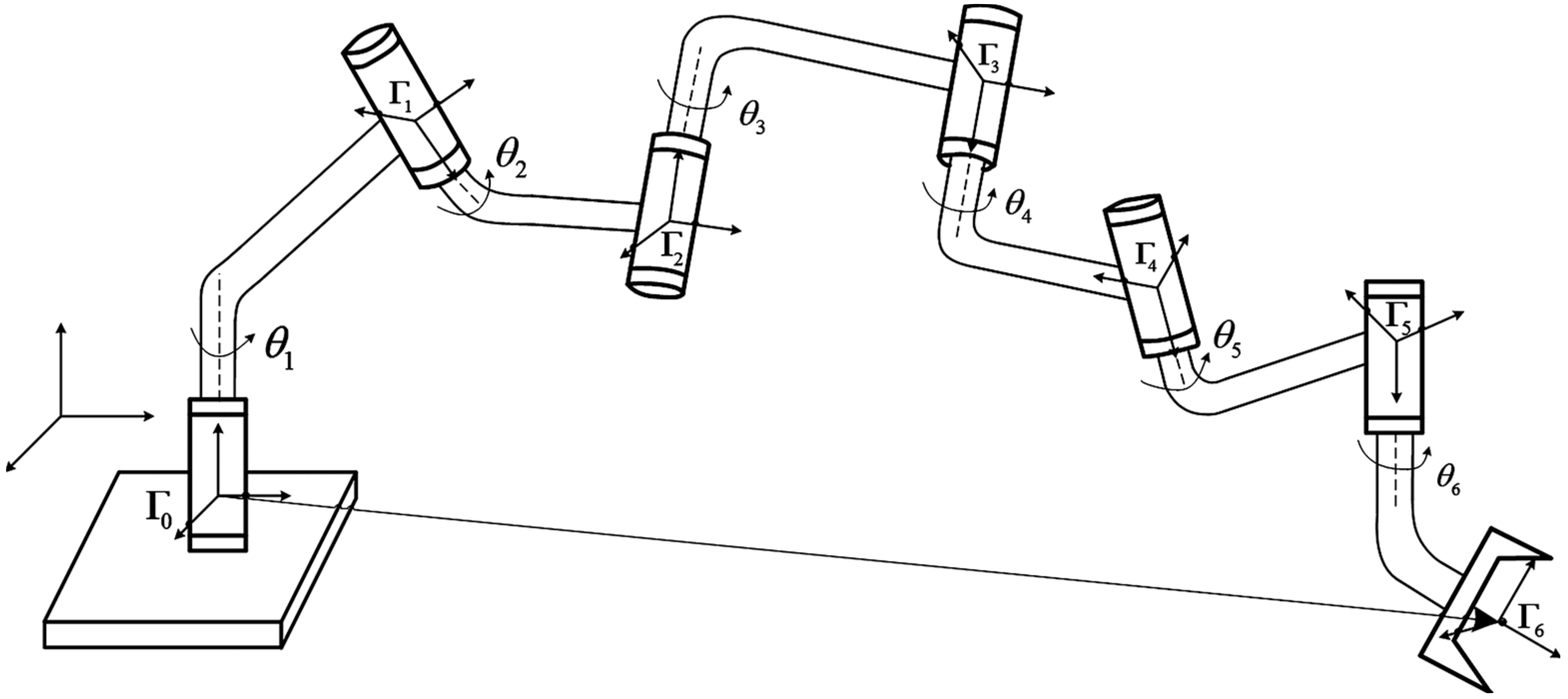
Robot Kinematics

Goal: Given the structure of a robot arm, compute

☑ **Forward kinematics**: infer the pose of the end-effector, given the state of each joint (Lecture 7-8)

– **Inverse kinematics**: inferring the joint states necessary to reach a desired end-effector pose.

☑ start with linear algebra refresher (Lecture 6)



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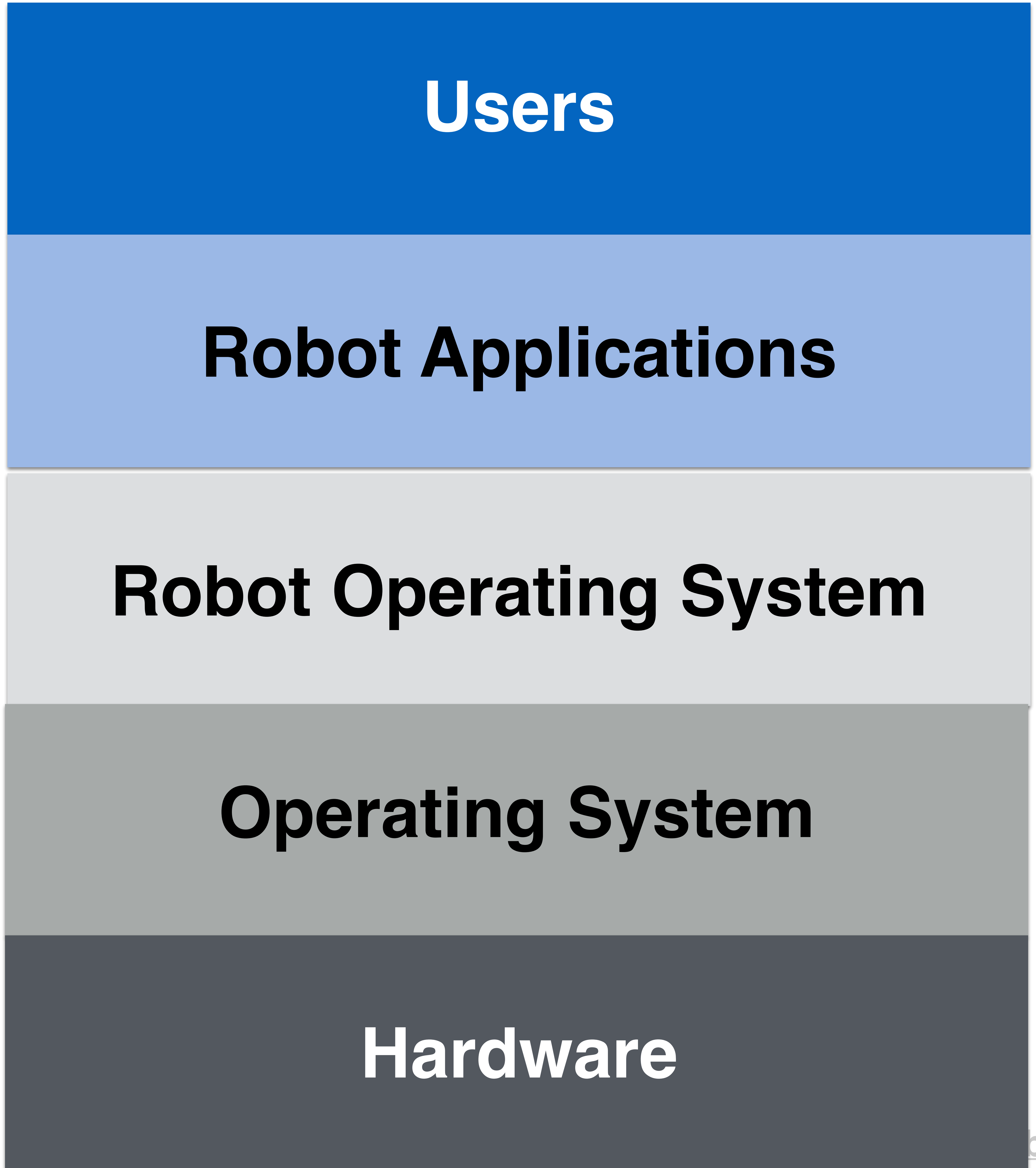
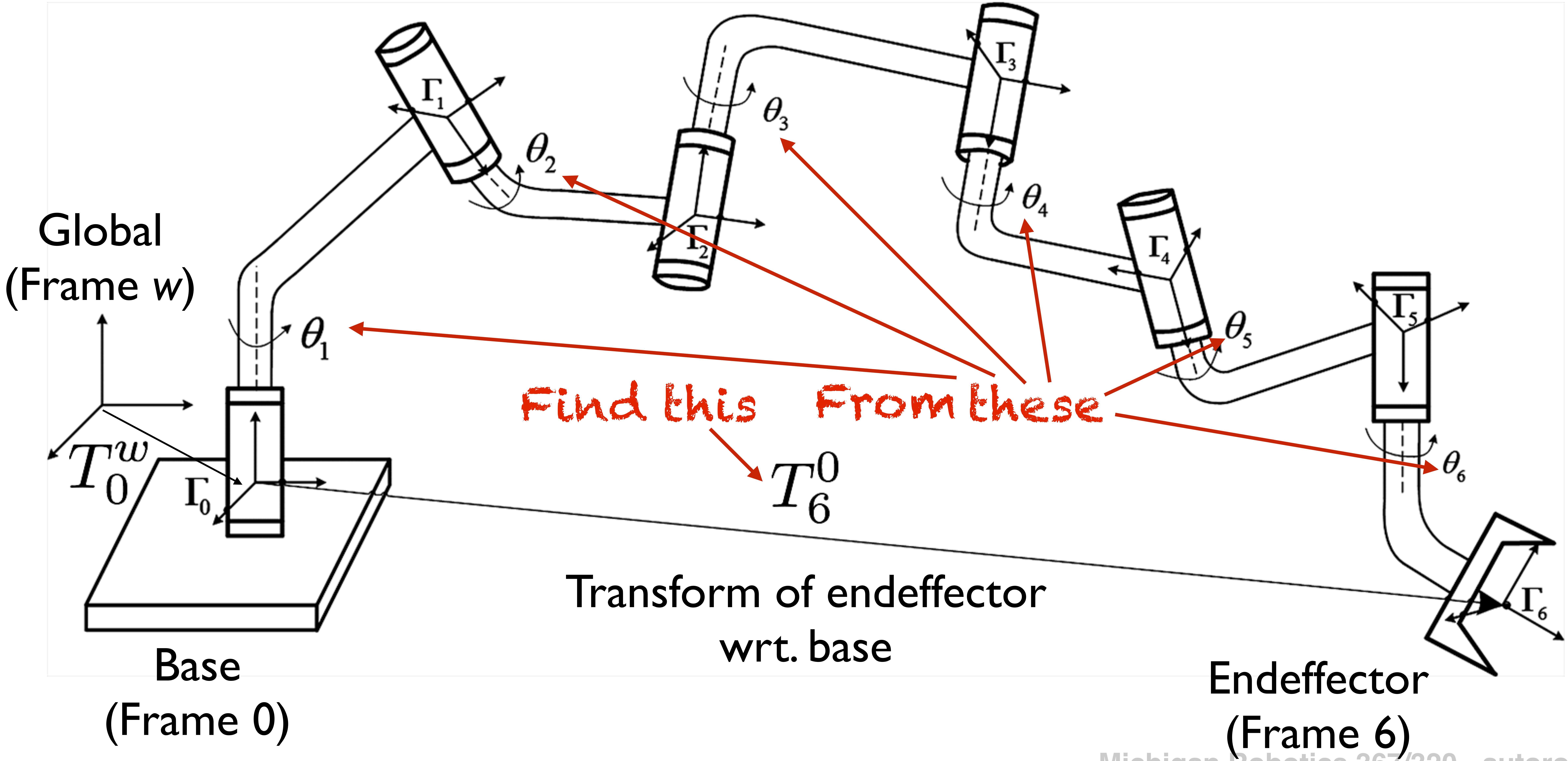


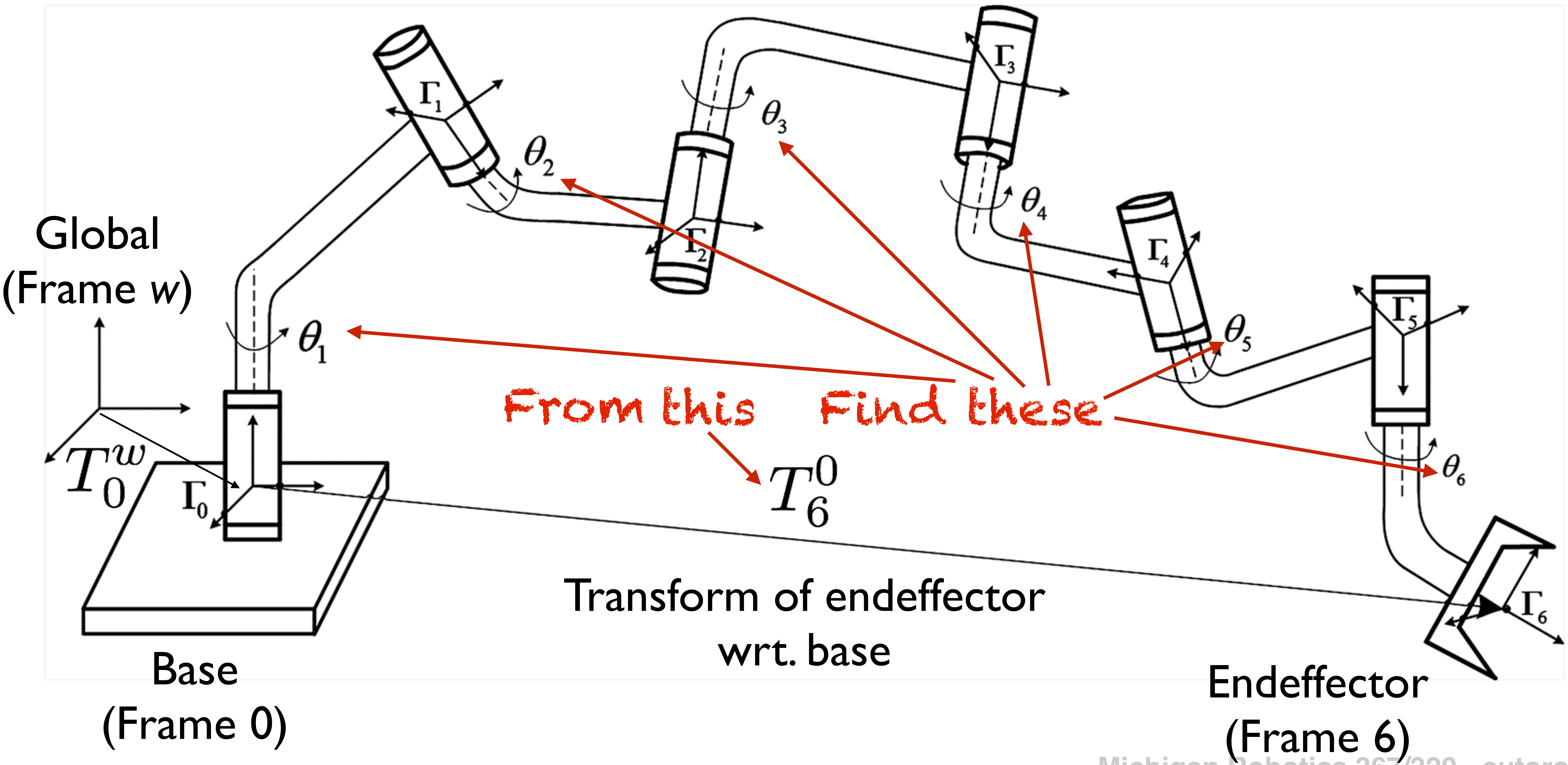
Robot Operating System

Covered at breadth in AutoRob

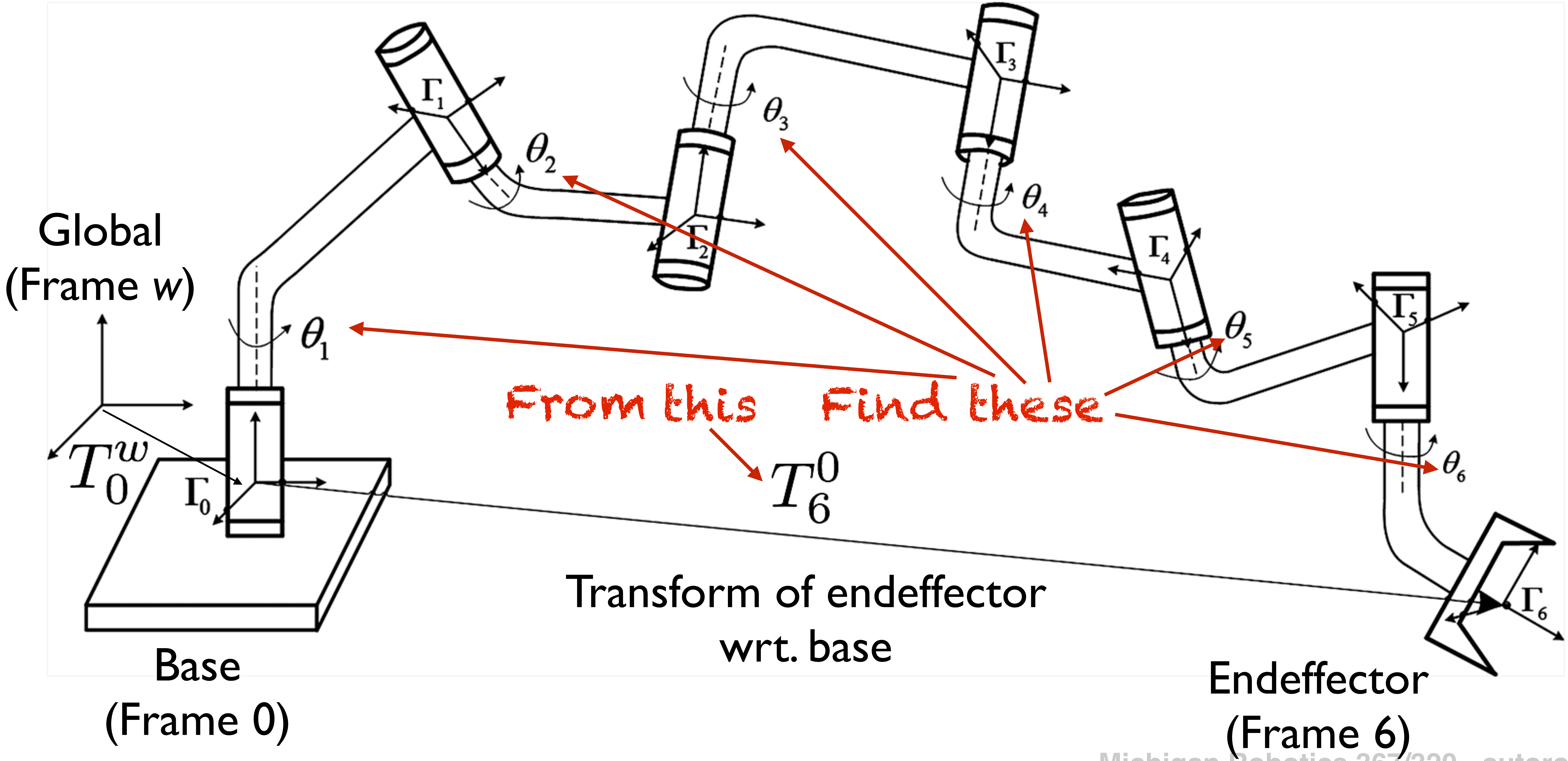
Forward kinematics: many-to-one mapping of robot configuration to reachable workspace endeffector poses



Inverse kinematics: one-to-many mapping of workspace endeffector pose to robot configuration



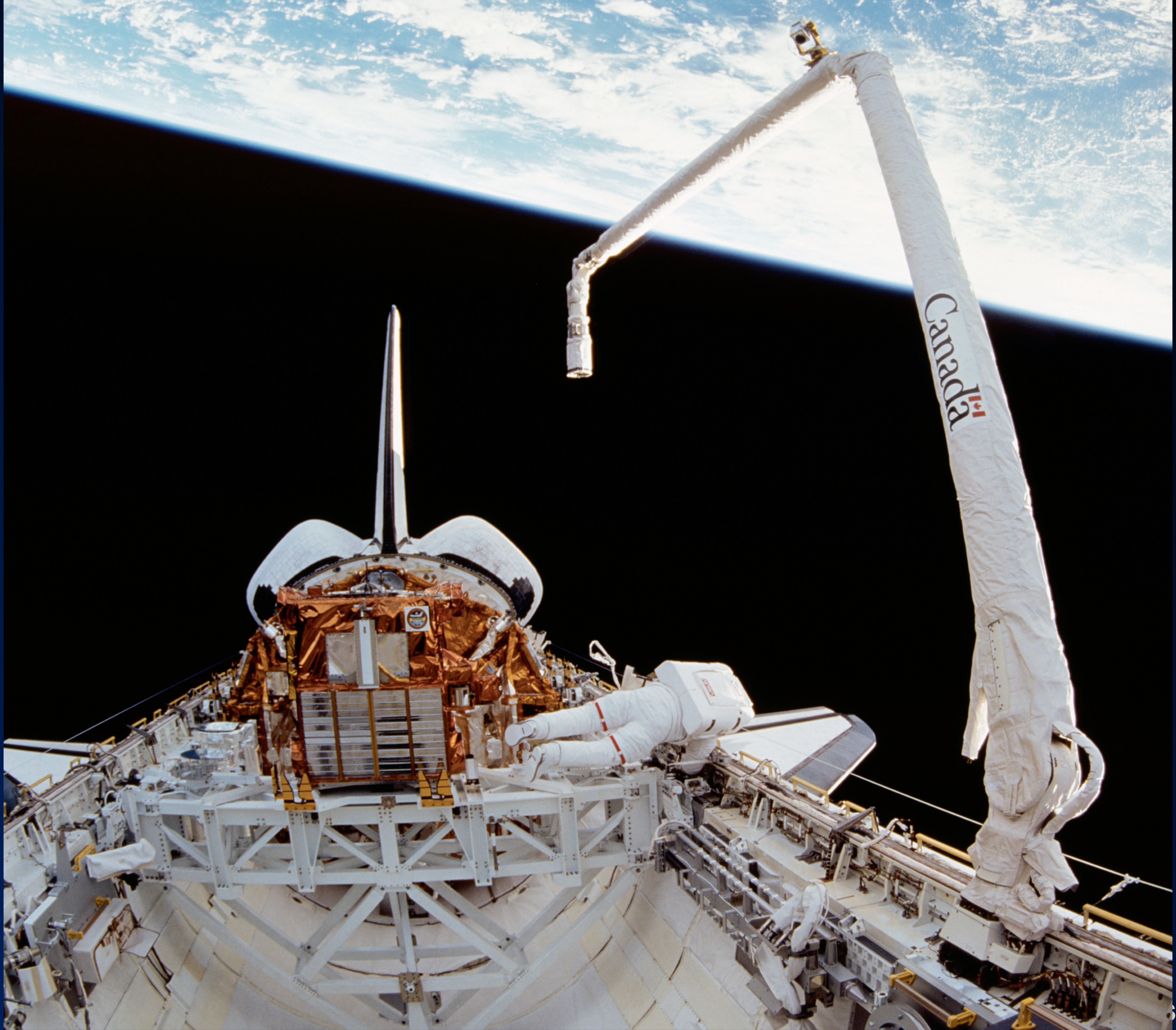
Inverse kinematics: how to solve for $q = \{\theta_1, \ldots, \theta_N\}$ from T^0_N?



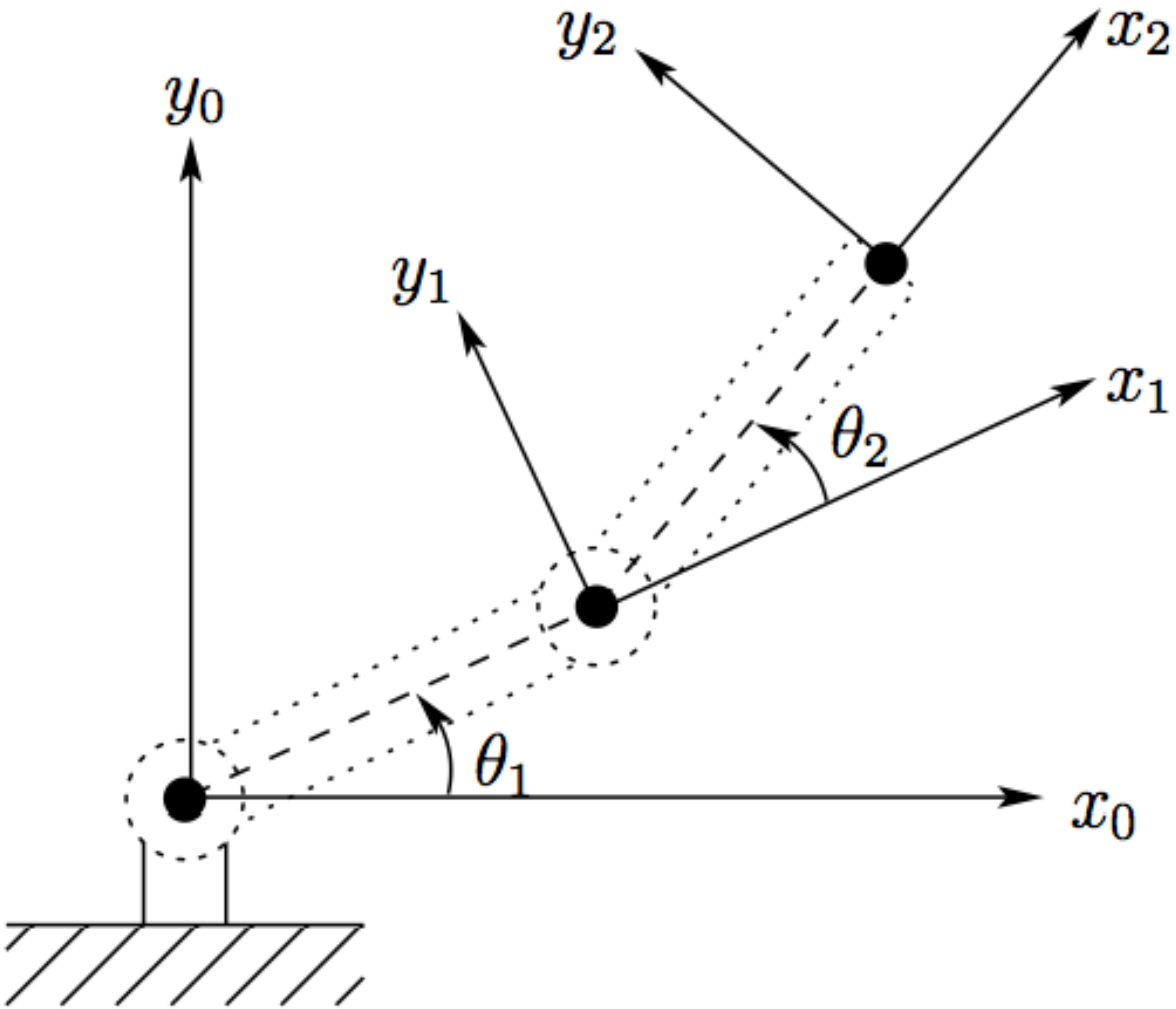
Inverse Kinematics: 2 possibilites

- **Closed-form solution**: geometrically infer satisfying configuration (Lecture 11)
  - *Speed*: solution often computed in constant time
  - *Predictability*: solution is selected in a consistent manner
- **Solve by optimization**: minimize error of endeffector to desired pose (Lecture 12)
  - often some form of Gradient Descent (a la Jacobian Transpose)
  - *Generality*: same solver can be used for many different robots

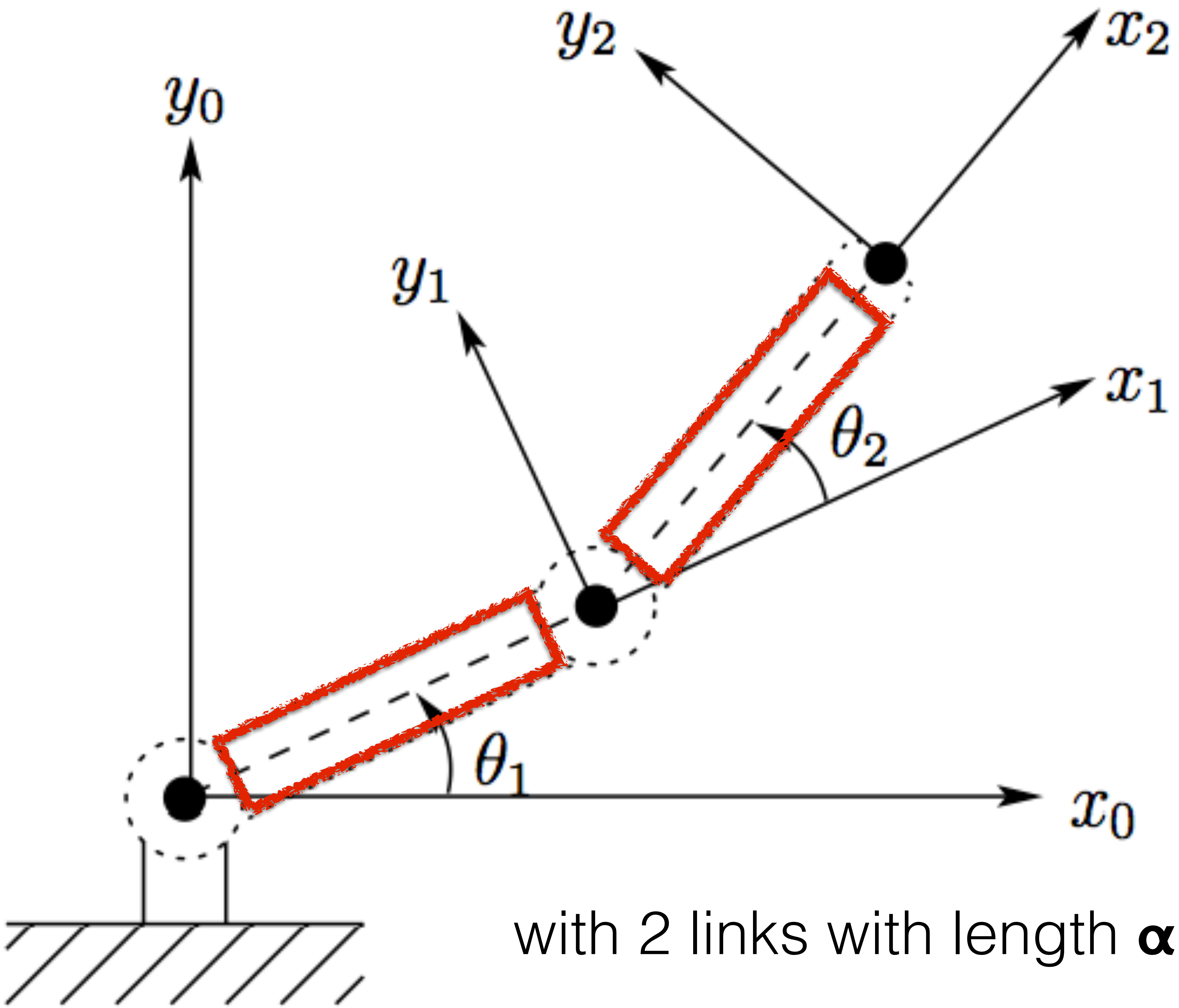
Let’s define IK starting from FK


Canada

Consider a planar 2-link arm as an example

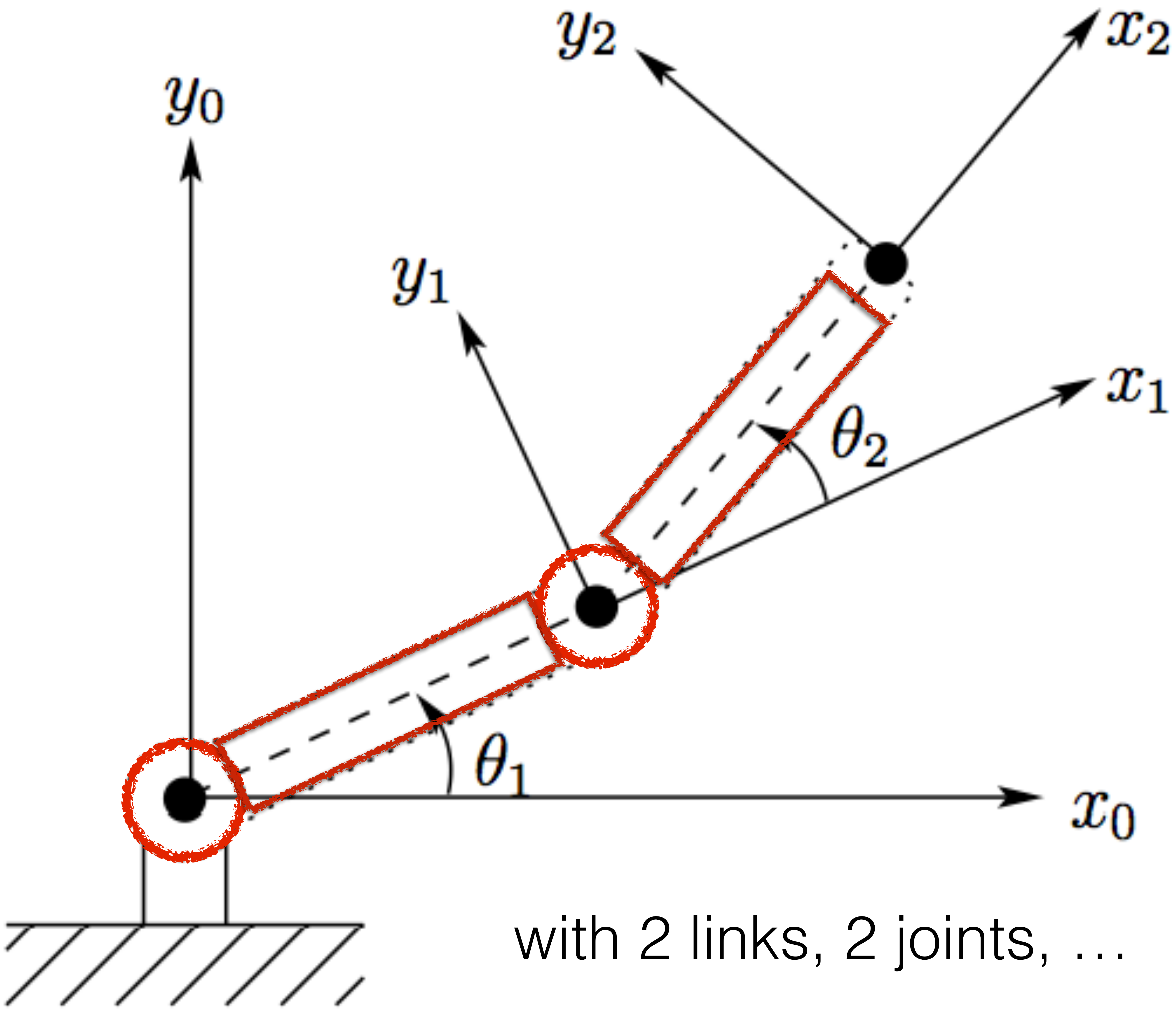


Consider a planar 2-link arm as an example



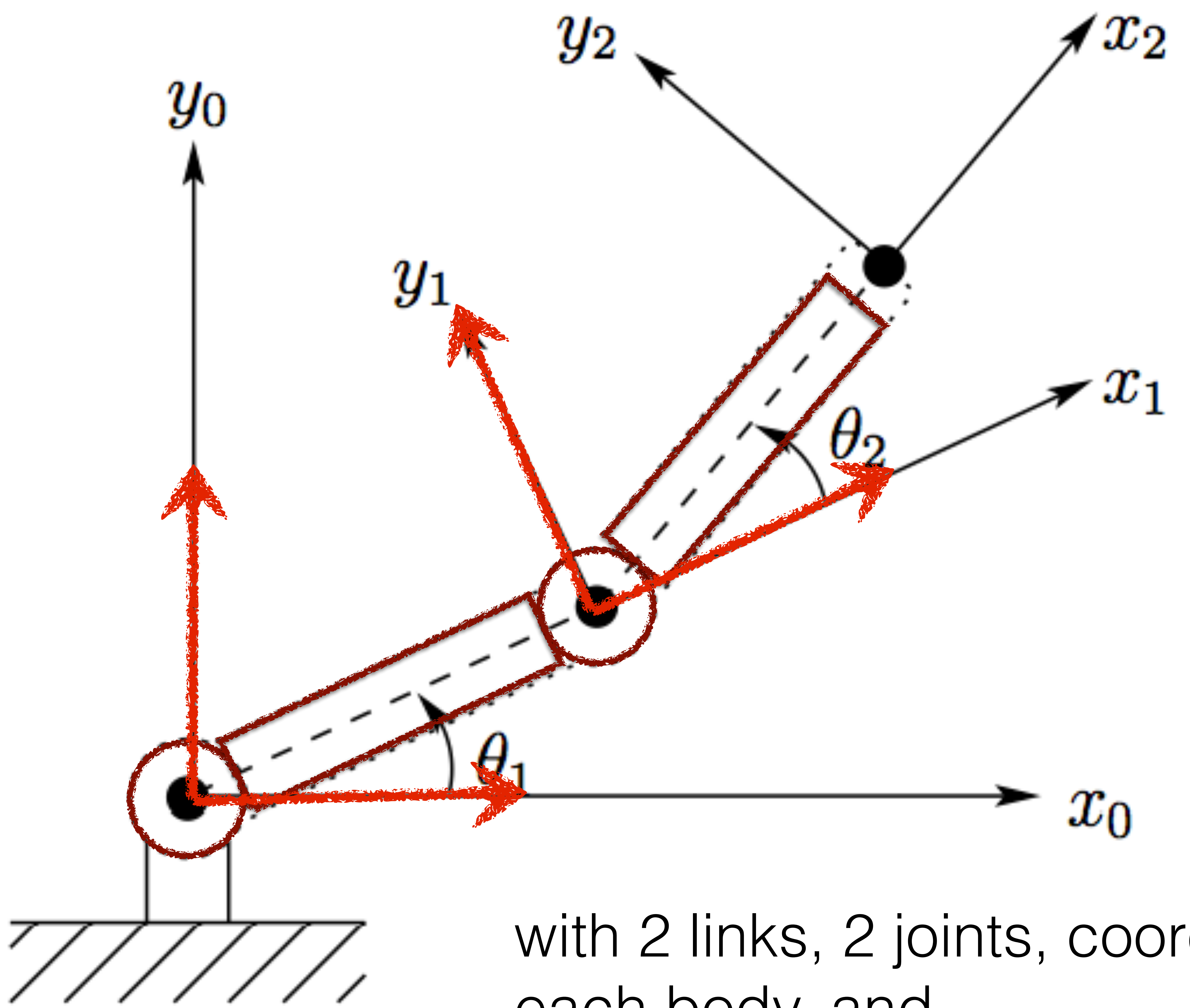
with 2 links with length $\boldsymbol{\alpha}_i$, …

Consider a planar 2-link arm as an example



with 2 links, 2 joints, …

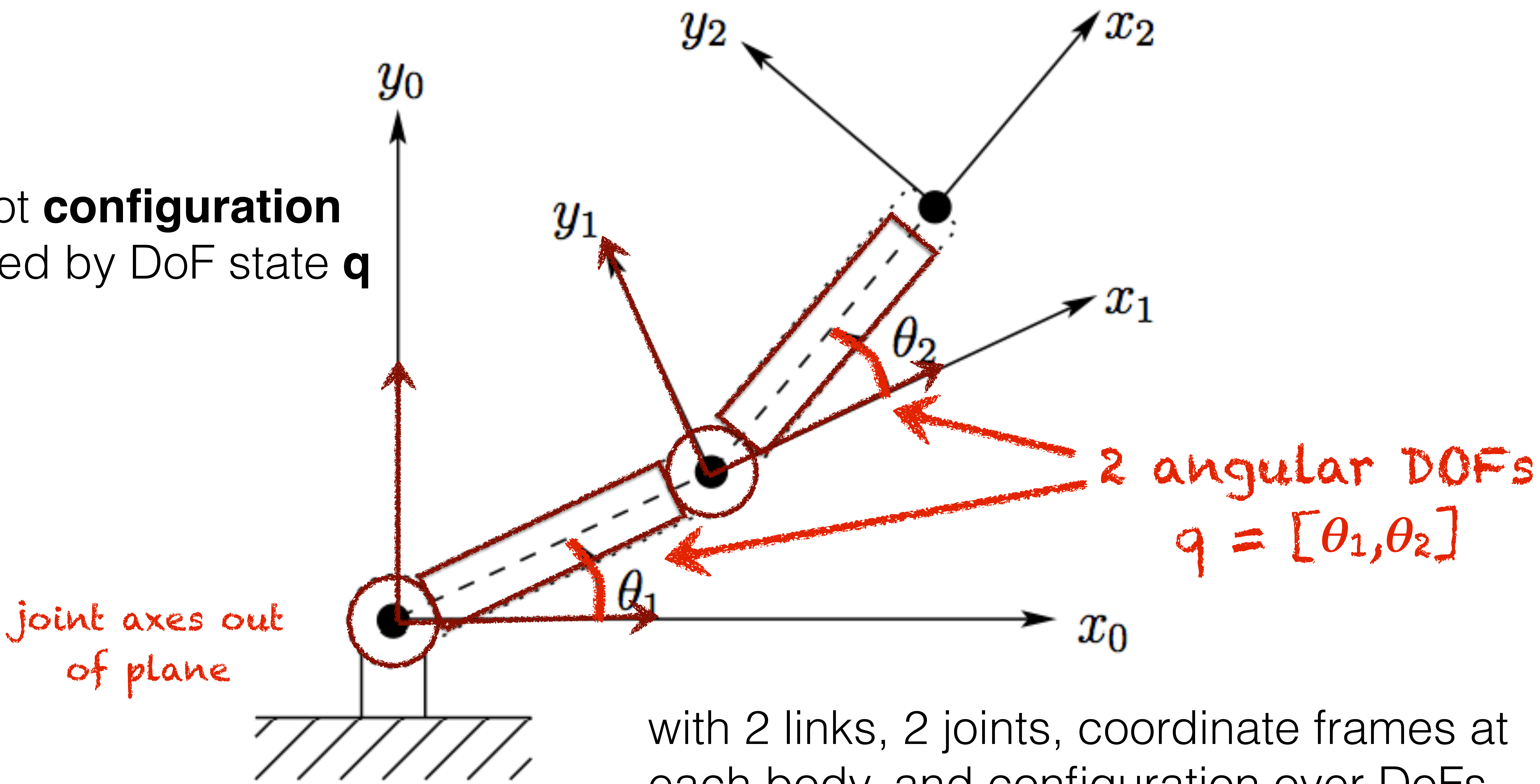
Consider a planar 2-link arm as an example



with 2 links, 2 joints, coordinate frames at each body, and …

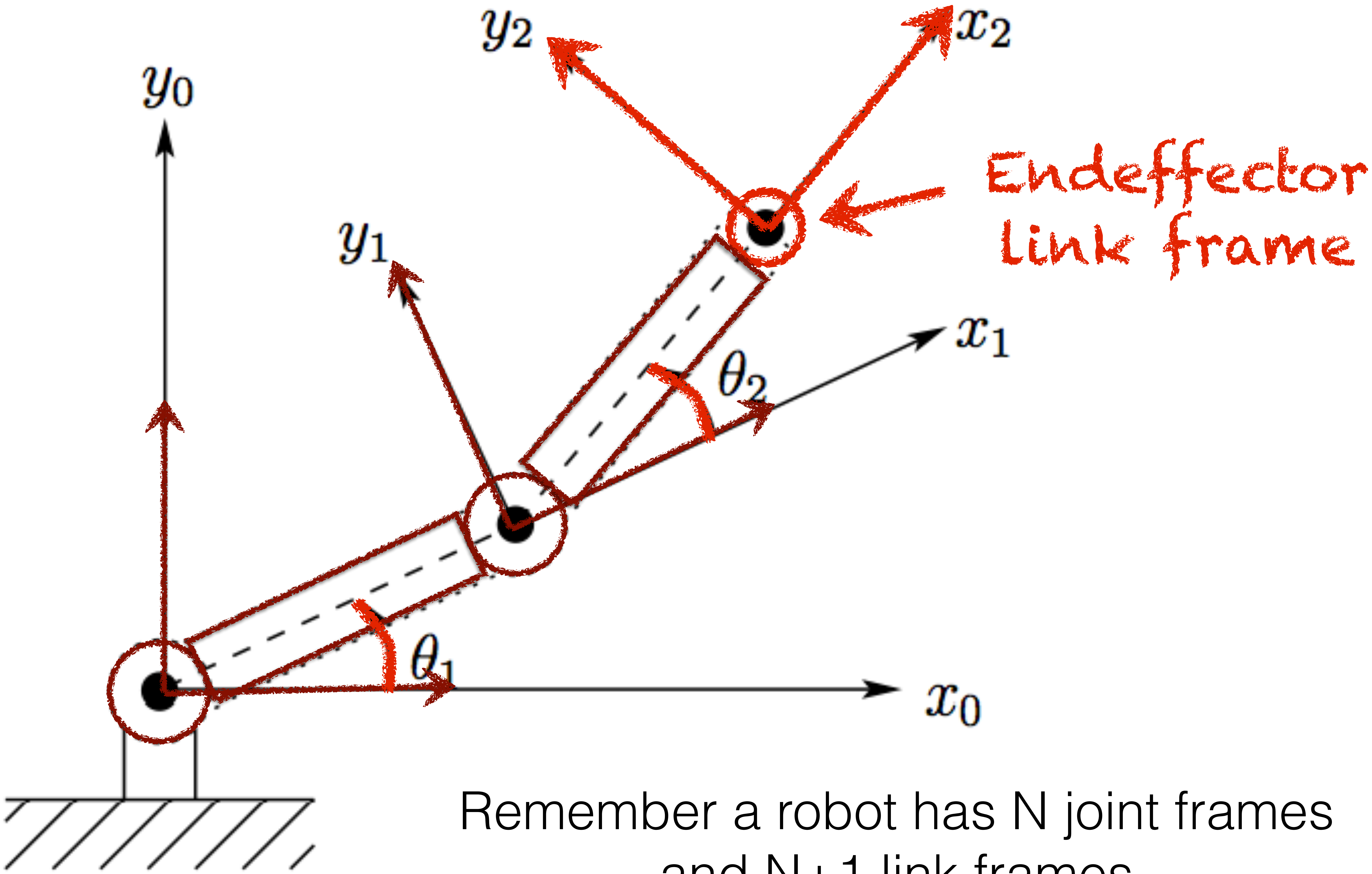
Consider a planar 2-link arm as an example

Robot **configuration** defined by DoF state **q**



with 2 links, 2 joints, coordinate frames at each body, and configuration over DoFs

Consider a planar 2-link arm as an example



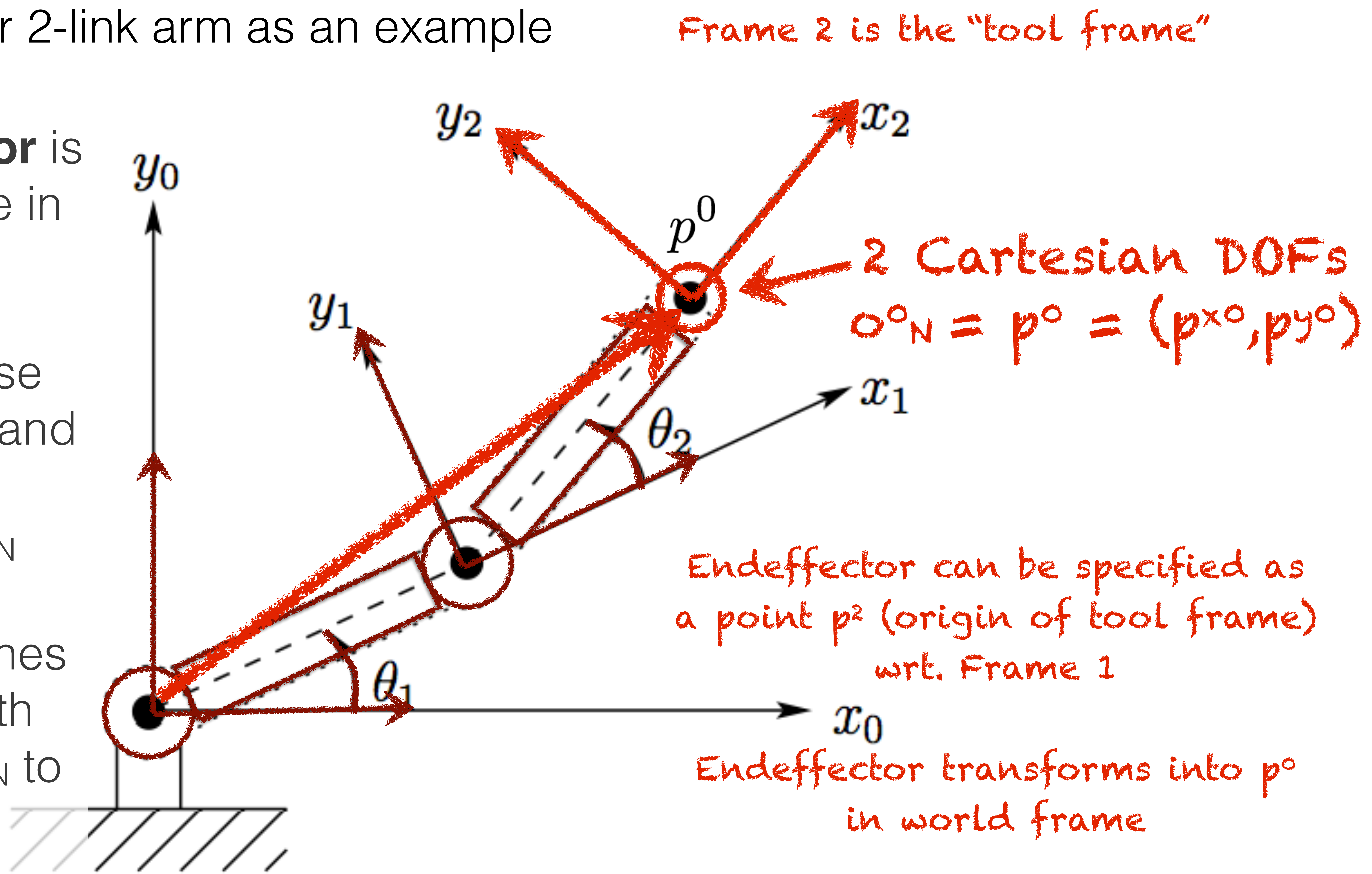
Remember a robot has N joint frames and N+1 link frames

Consider a planar 2-link arm as an example

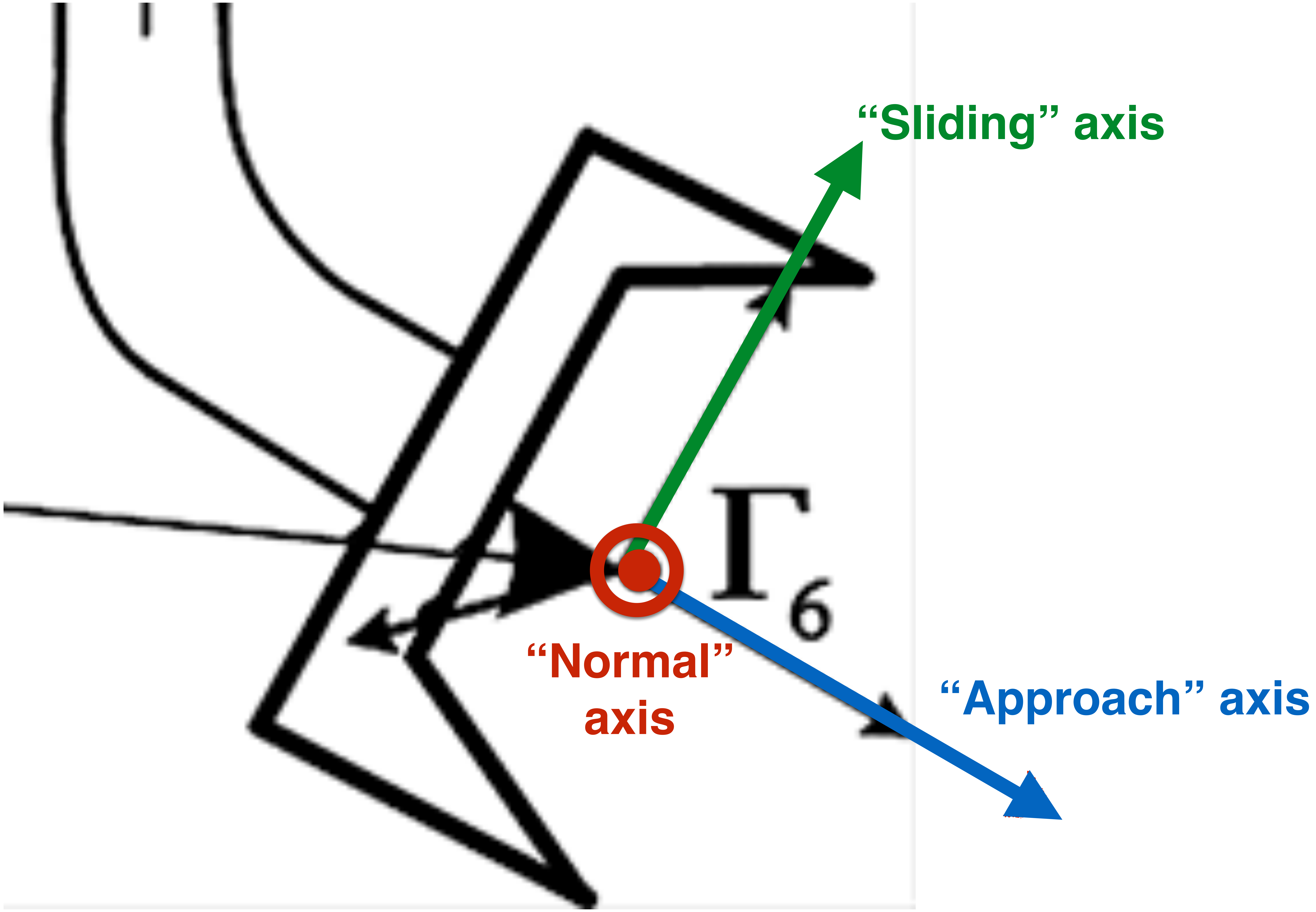
Robot **endeffector** is the gripper pose in world frame

Endeffector pose has position $\mathbf{o}^0_N$ and can consider orientation $\mathbf{R}^0_N$

Endeffector defines "tool frame" with transform $\mathbf{H}=\mathbf{T}^0_N$ to world frame

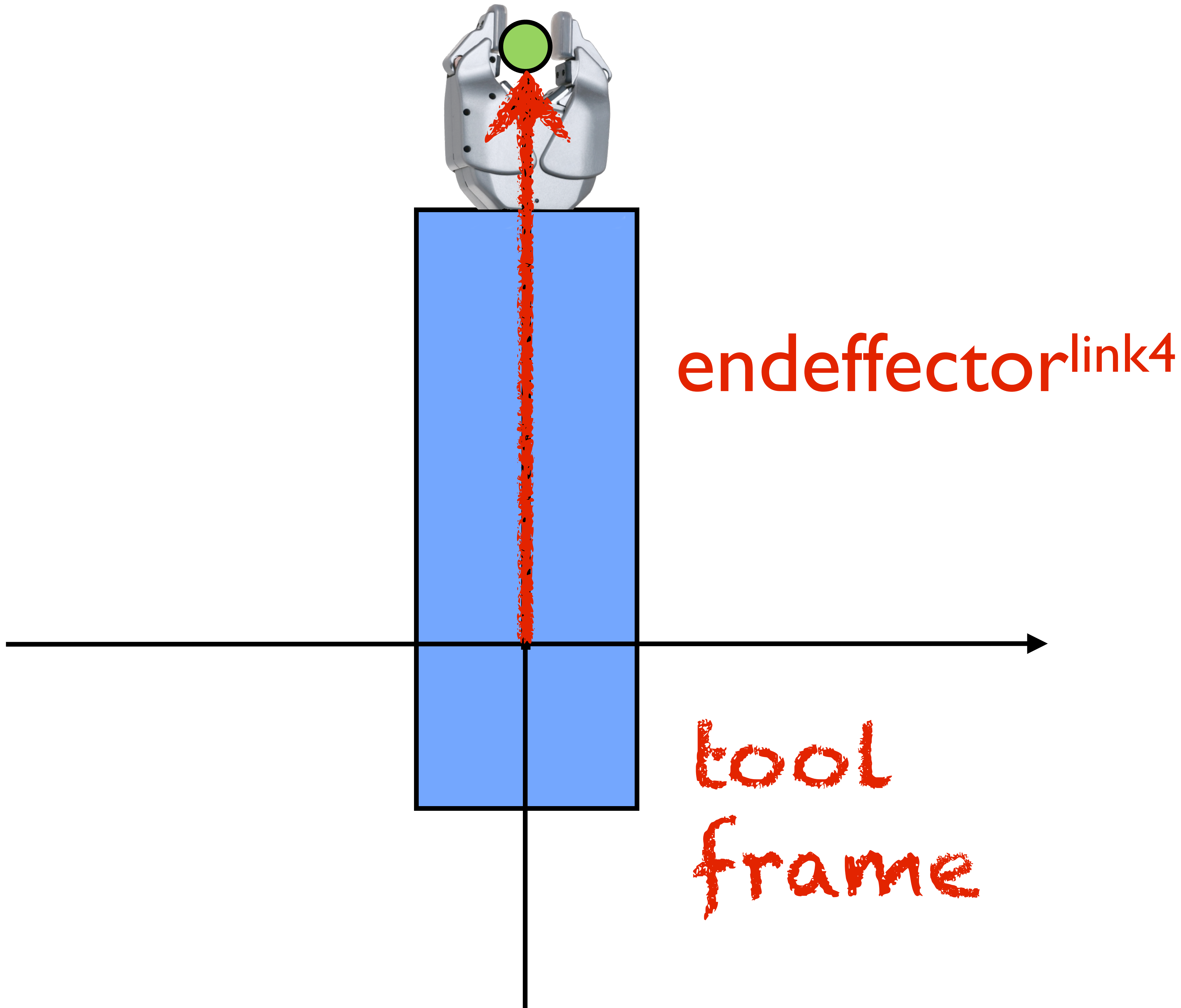


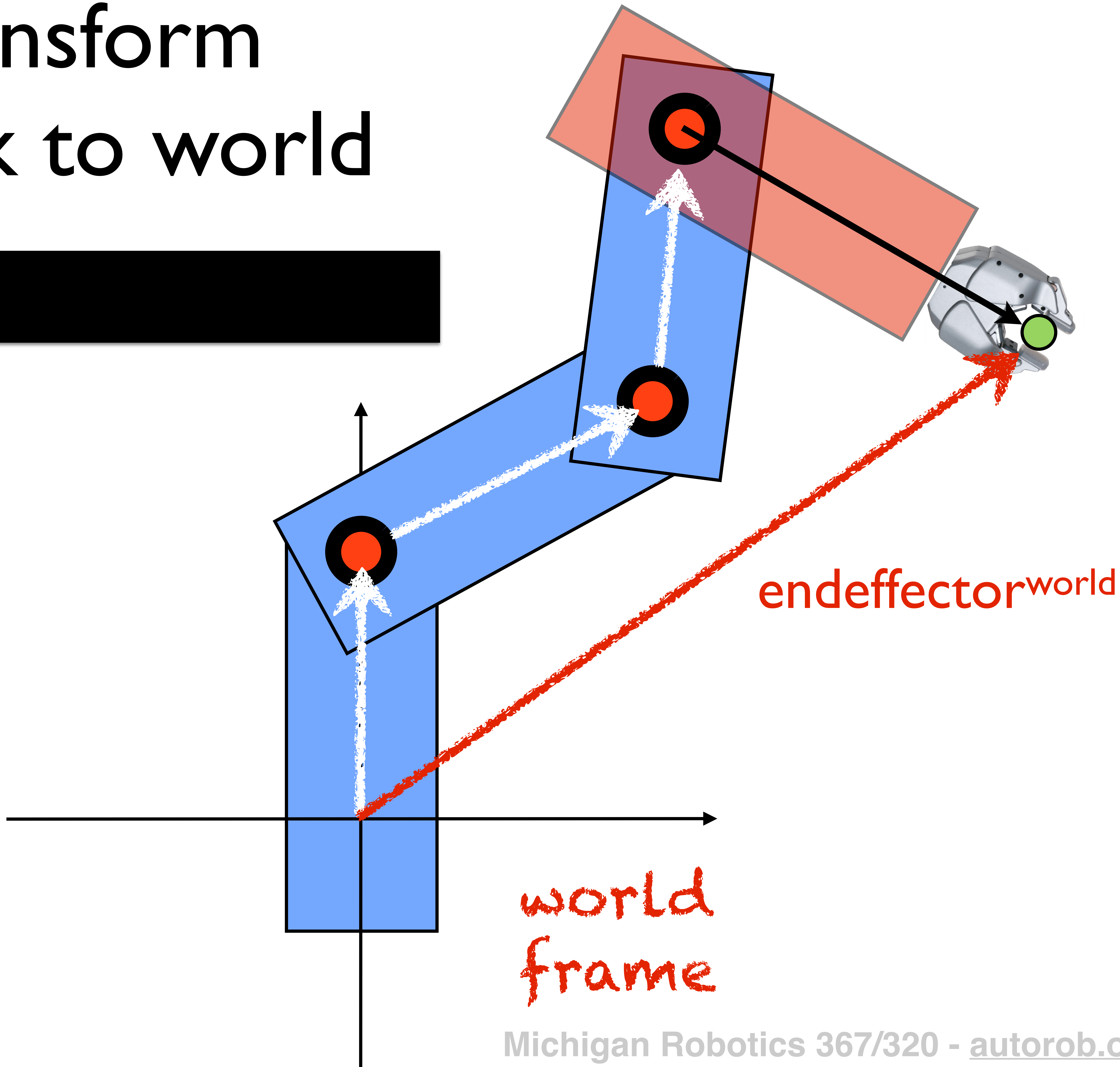
Endeffector axes



Checkpoint: Transform endeffector on link to world

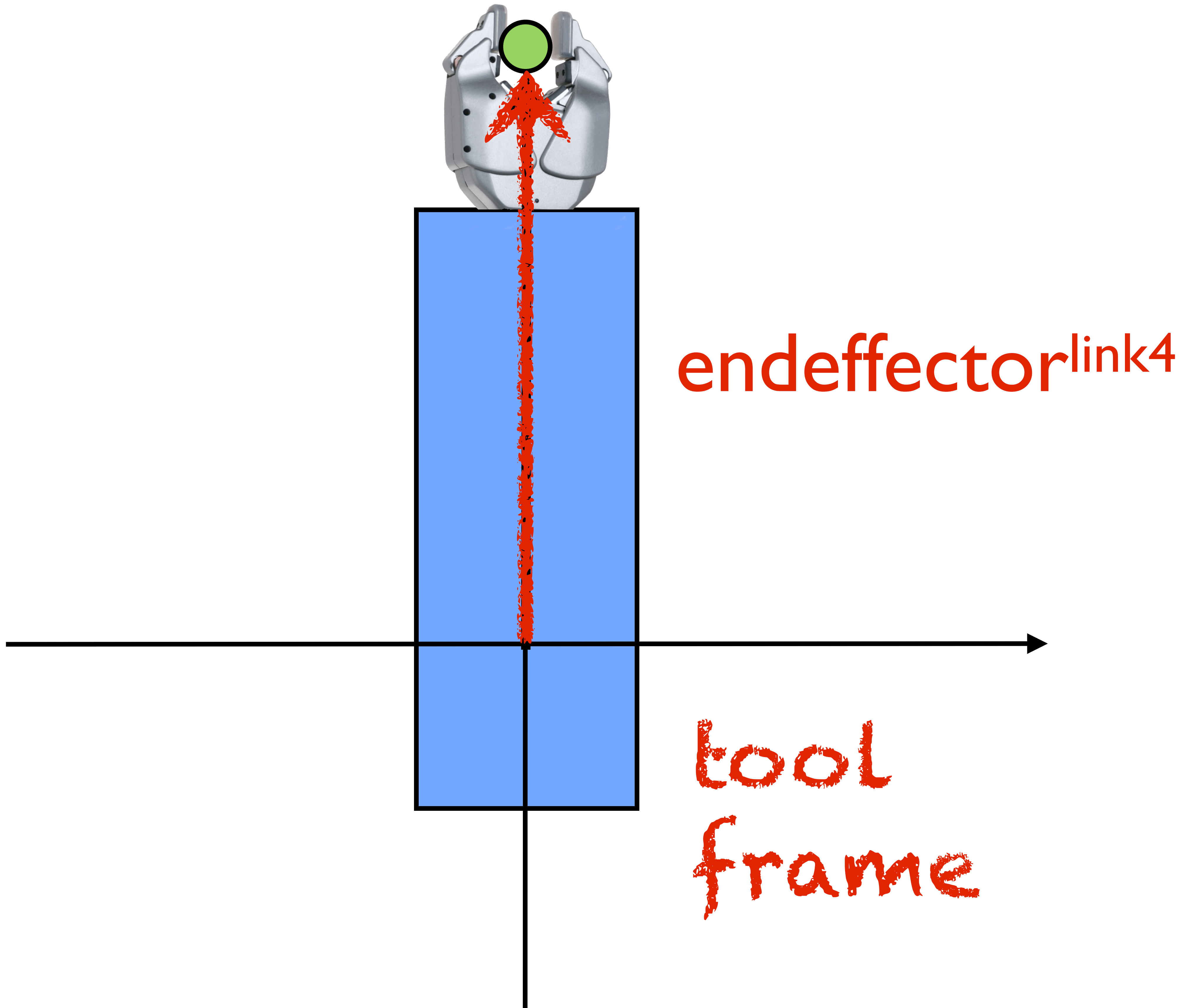
$$\text{endeffector}^{world} = $$ [redacted]

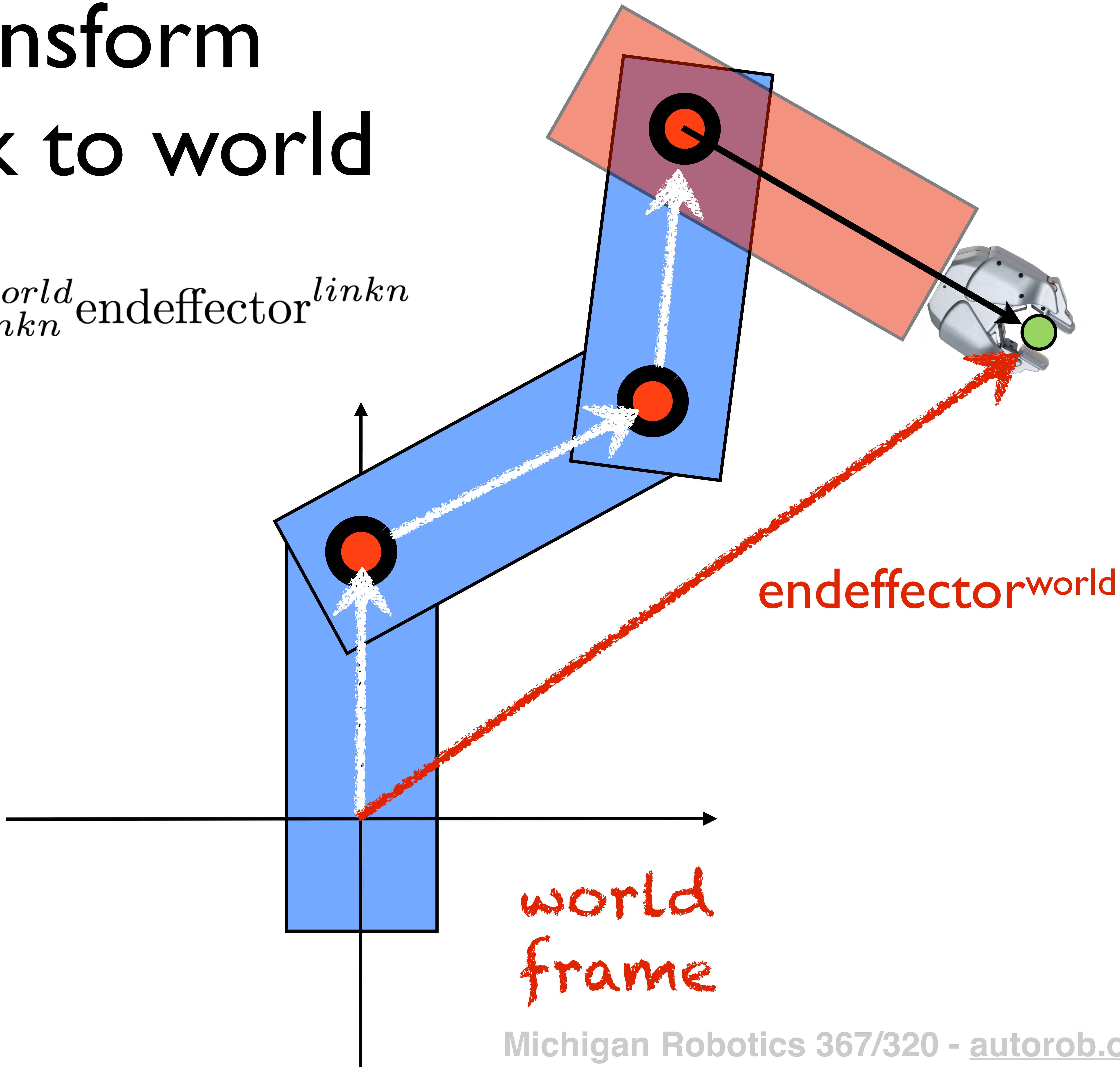




Checkpoint: Transform endeffector on link to world

$$\text{endeffector}^{world} = T_{linkn}^{world}\,\text{endeffector}^{linkn}$$



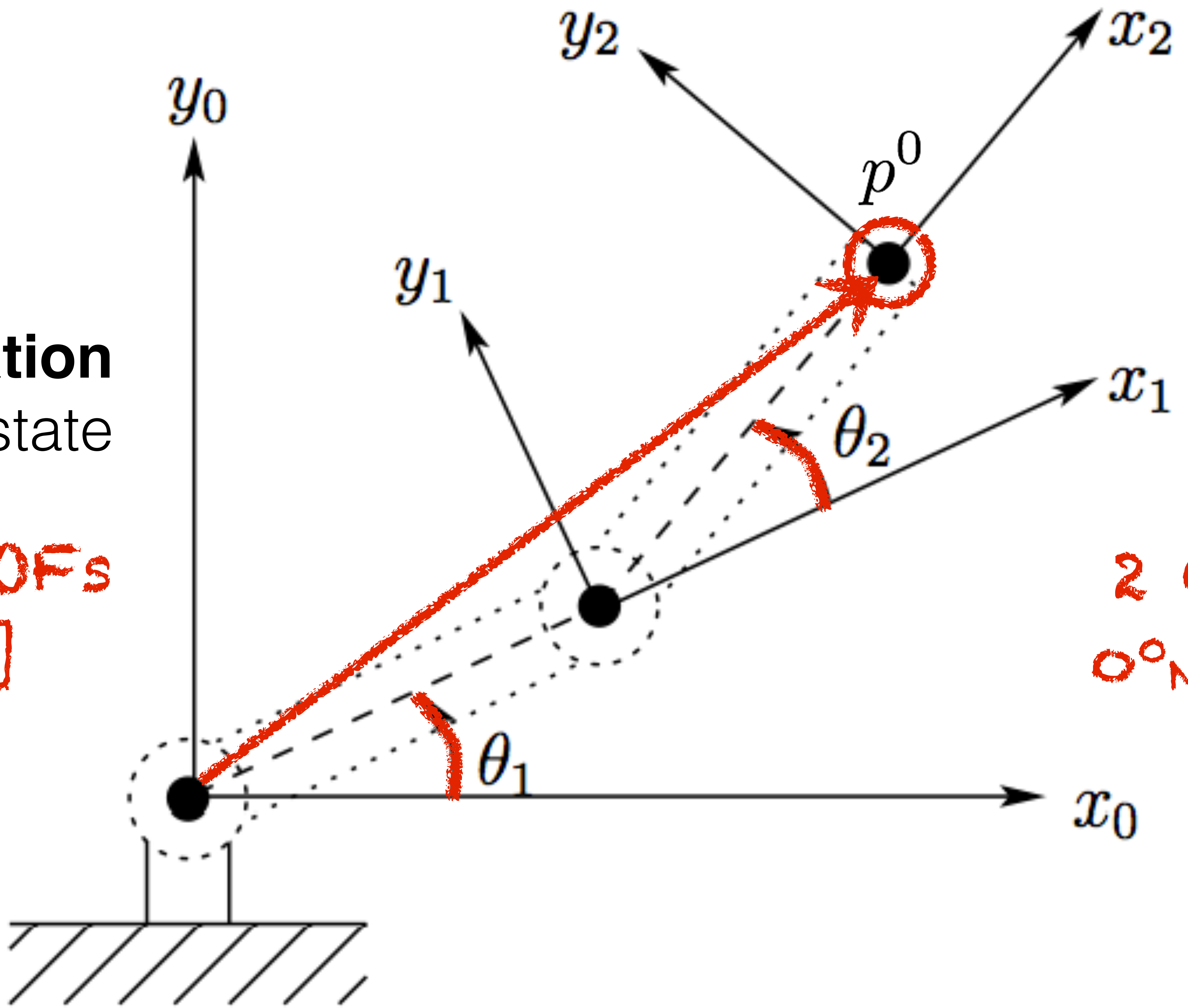


Forward kinematics: "given configuration, compute endeffector"

Robot **configuration** defined by DoF state

2 angular DOFs

$q = [\theta_1, \theta_2]$



Robot **endeffector** is the gripper pose in world frame

2 Cartesian DOFs

$o^0_N = p^0 = (p^{x0}, p^{y0})$

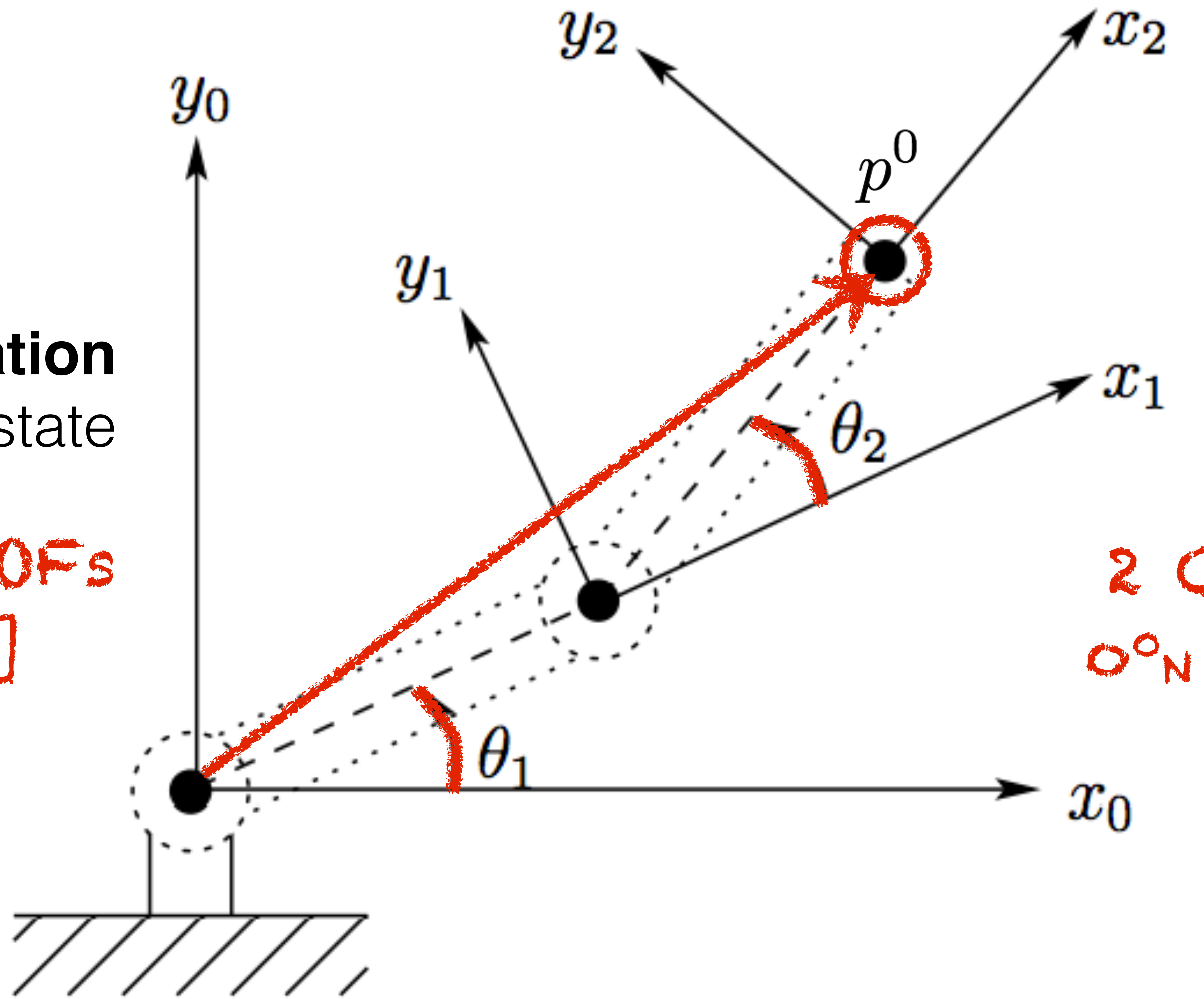
Forward kinematics: $[\mathbf{o}^0_N, \mathbf{R}^0_N] = f(\mathbf{q})$

$p^0 = f(\theta_1, \theta_2)$

Robot **configuration** defined by DoF state

2 angular DOFs

$q = [\theta_1, \theta_2]$

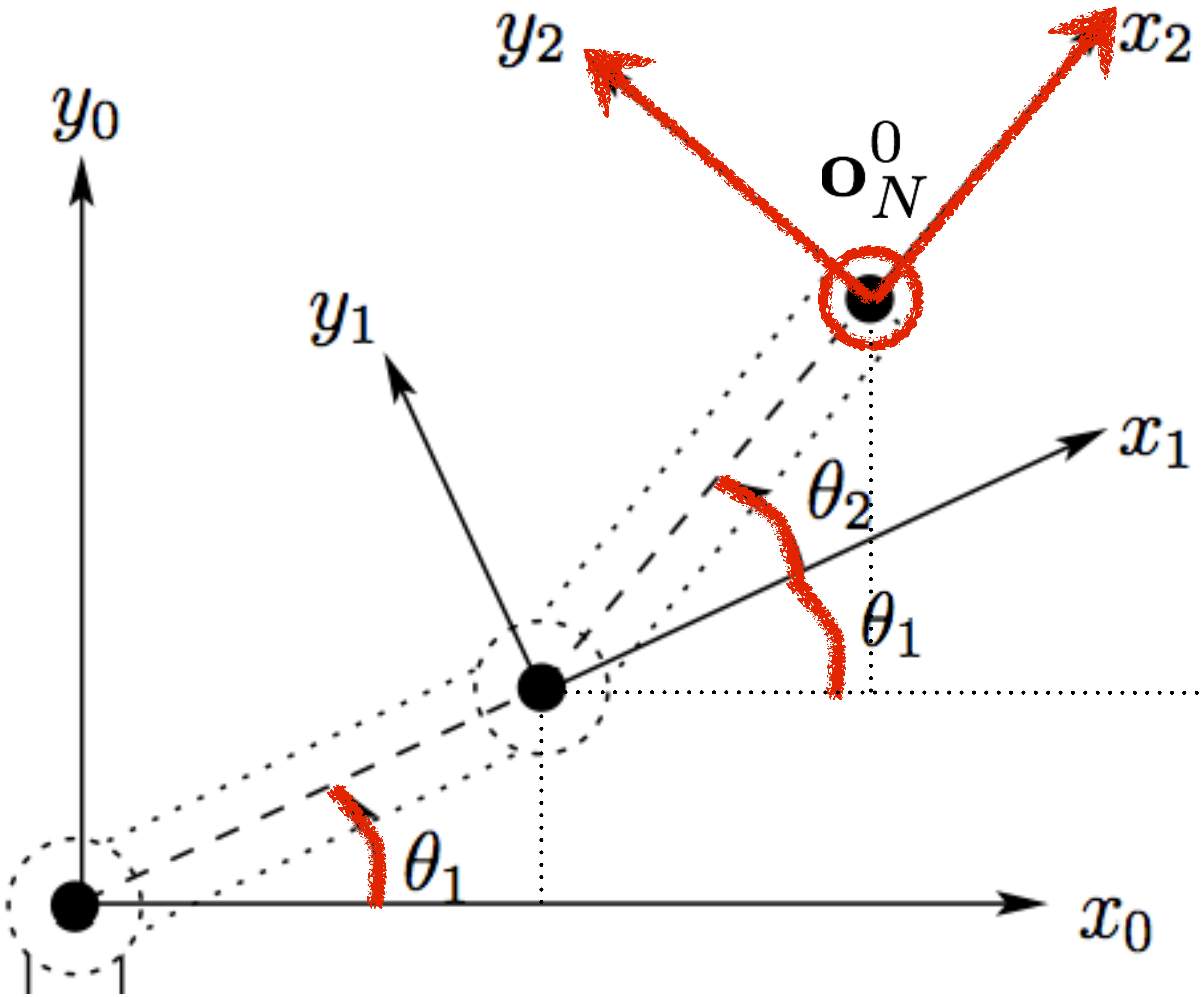


Robot **endeffector** is the gripper pose in world frame

2 Cartesian DOFs

$o^0_N = p^0 = (p_x^0, p_y^0)$

Forward kinematics: $[\mathbf{o}^0_N, \mathbf{R}^0_N] = f(\mathbf{q})$



What is the position and orientation of the tool wrt. the world?

remember:
$$p^0 = T^0_1 T^1_2 p^2$$

$\mathbf{R}^0_N = \Big[$ What are the elements of this matrix? $\Big]$

$\mathbf{o}^0_N = \Big[$ What are the elements of this vector? $\Big]$

Forward kinematics: $[\mathbf{o}^0_N, \mathbf{R}^0_N] = f(\mathbf{q})$

remember:

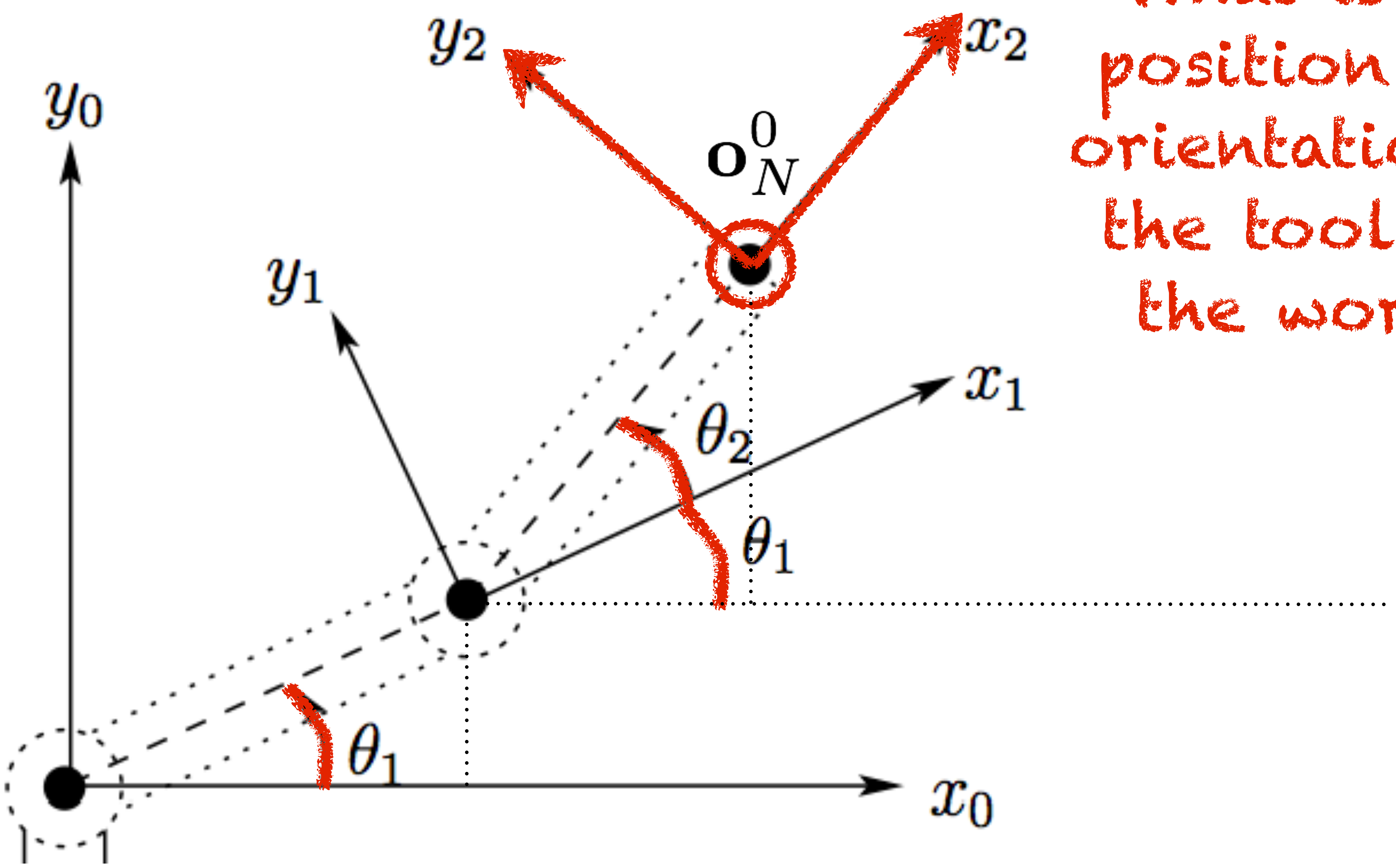
$$p^0 = T^0_1 T^1_2 p^2$$

$p^0 = R_2{}^0 p^2 + d_2{}^0$

where

$R_2{}^0 = R_1{}^0 R_2{}^1$

[redacted]



What is the position and orientation of the tool wrt. the world?

$$\mathbf{R}^0_N = \begin{bmatrix} \cos(\theta_1 + \theta_2) & -\sin(\theta_1 + \theta_2) \\ \sin(\theta_1 + \theta_2) & \cos(\theta_1 + \theta_2) \end{bmatrix}$$

$\mathbf{o}^0_N = [$ What are the elements of this vector? $]$

Start with:

$$d_2^0 = R_1^0 d_2^1 + d_1^0$$

substitute in variables then perform operations:

$$\begin{bmatrix} cos\theta_1 & -sin\theta_1 \\ sin\theta_1 & cos\theta_1 \end{bmatrix} \begin{bmatrix} \alpha_2 cos\theta_2 \\ \alpha_2 sin\theta_2 \end{bmatrix} + \begin{bmatrix} \alpha_1 cos\theta_1 \\ \alpha_1 sin\theta_1 \end{bmatrix}$$

then substitute trig identities

$$cos(x+y) = cos(x)cos(y) - sin(x)sin(y)$$

$$sin(x+y) = sin(x)cos(y) + cos(x)sin(y)$$

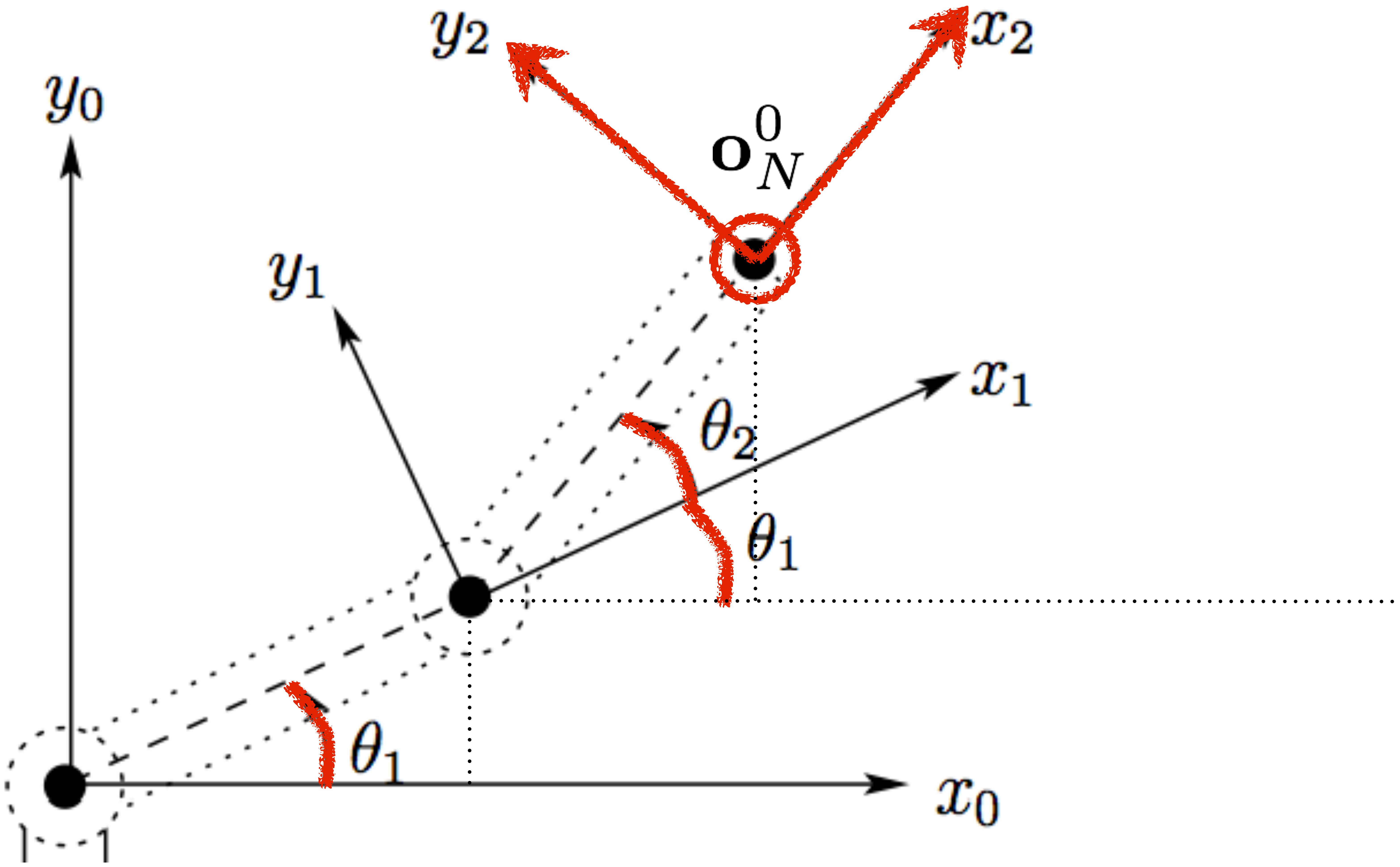
to get:

$$\mathbf{o}_N^0 = \begin{bmatrix} \quad \end{bmatrix}$$

What are the elements of this vector?

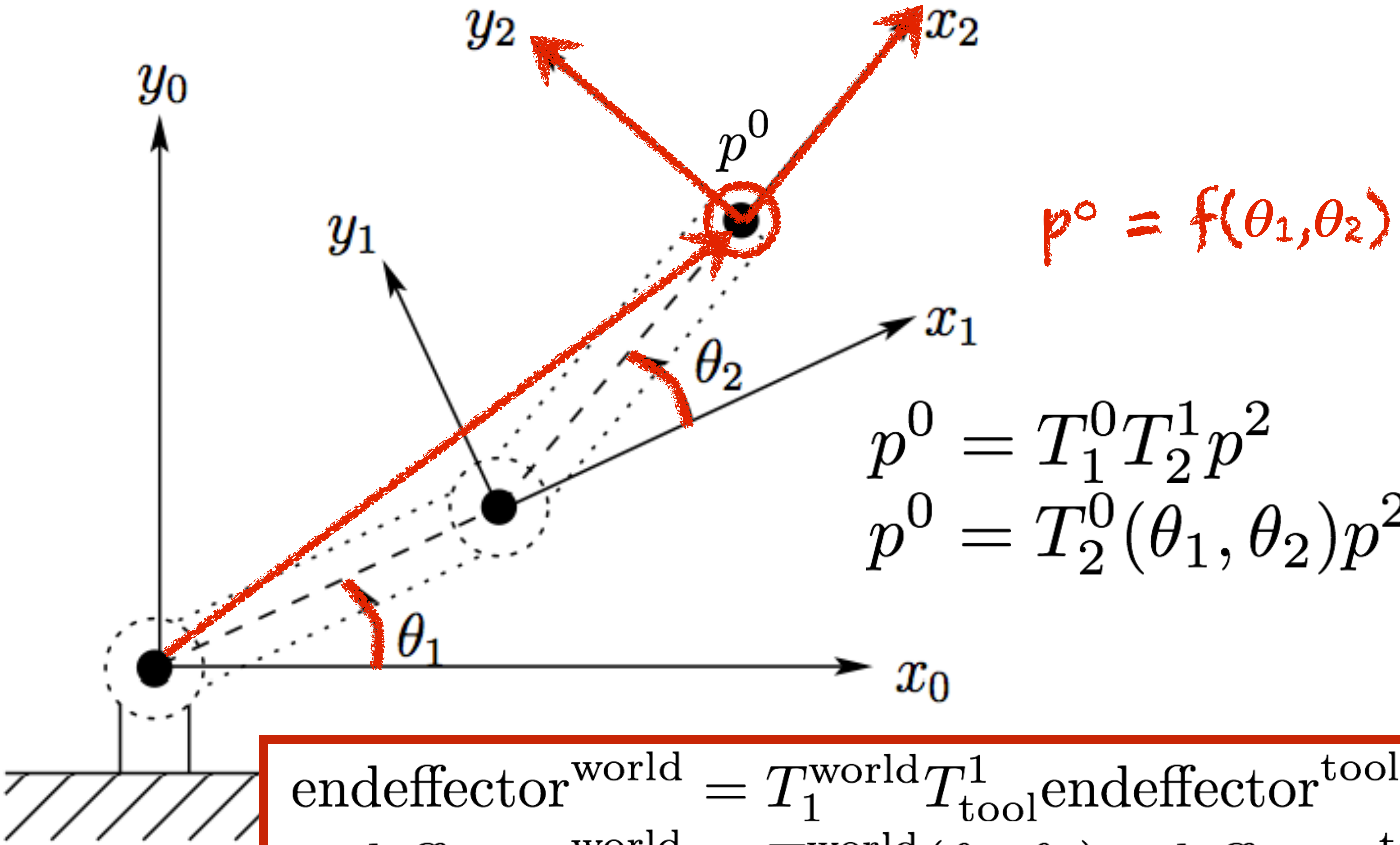
Thanks to Manan Siddiquee for catching my trig errors

Forward kinematics: $[\mathbf{o}^0_N, \mathbf{R}^0_N] = f(\mathbf{q})$



$$\mathbf{R}^0_N = \begin{bmatrix} \cos(\theta_1+\theta_2) & -\sin(\theta_1+\theta_2) \\ \sin(\theta_1+\theta_2) & \cos(\theta_1+\theta_2) \end{bmatrix} \quad \mathbf{o}^0_N = \begin{bmatrix} \alpha_1\cos\theta_1 + \alpha_2\cos(\theta_1+\theta_2) \\ \alpha_1\sin\theta_1 + \alpha_2\sin(\theta_1+\theta_2) \end{bmatrix}$$

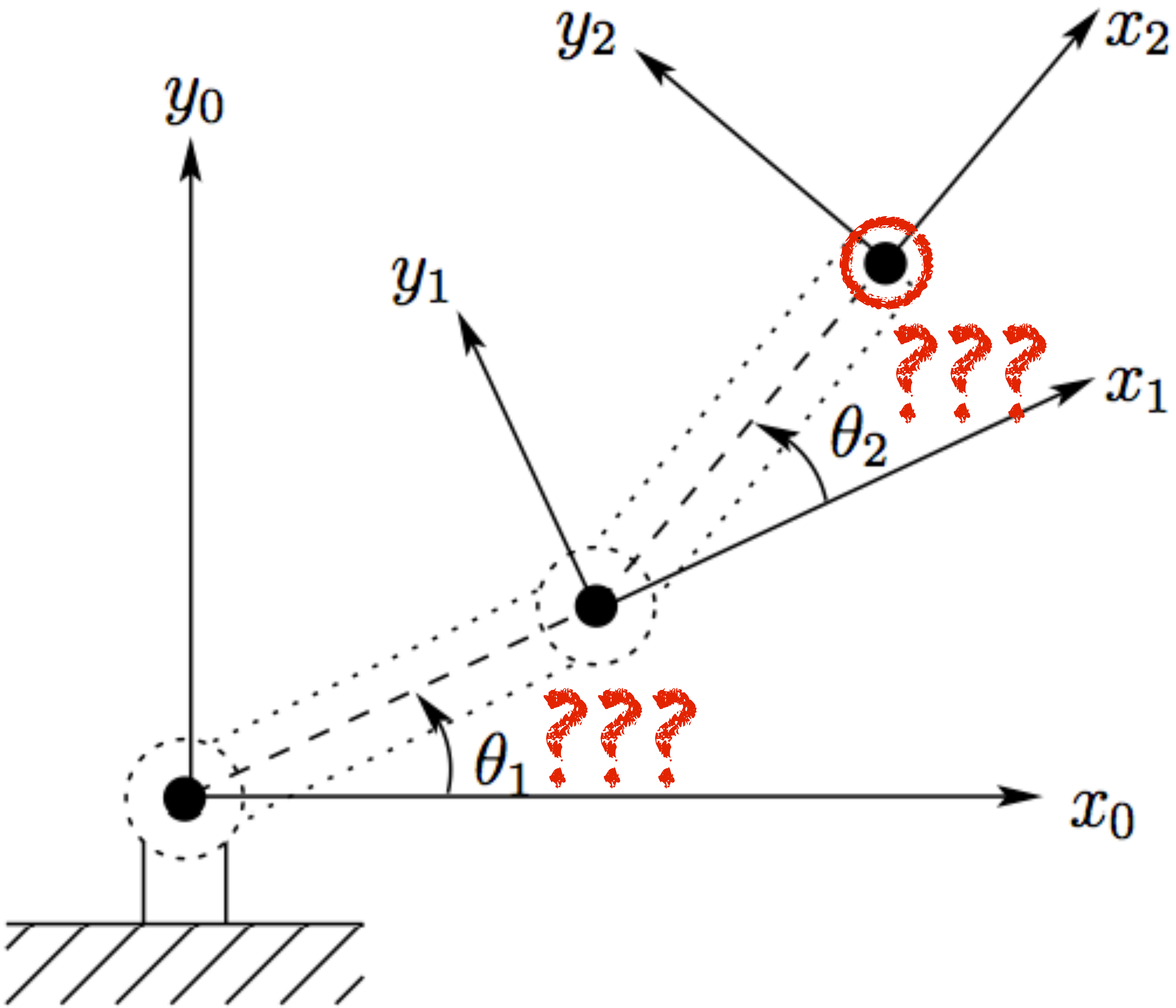
Forward kinematics: $[\mathbf{o}^0_N, \mathbf{R}^0_N] = f(\mathbf{q})$



$$p^0 = T^0_1 T^1_2 p^2$$
$$p^0 = T^0_2(\theta_1, \theta_2) p^2$$

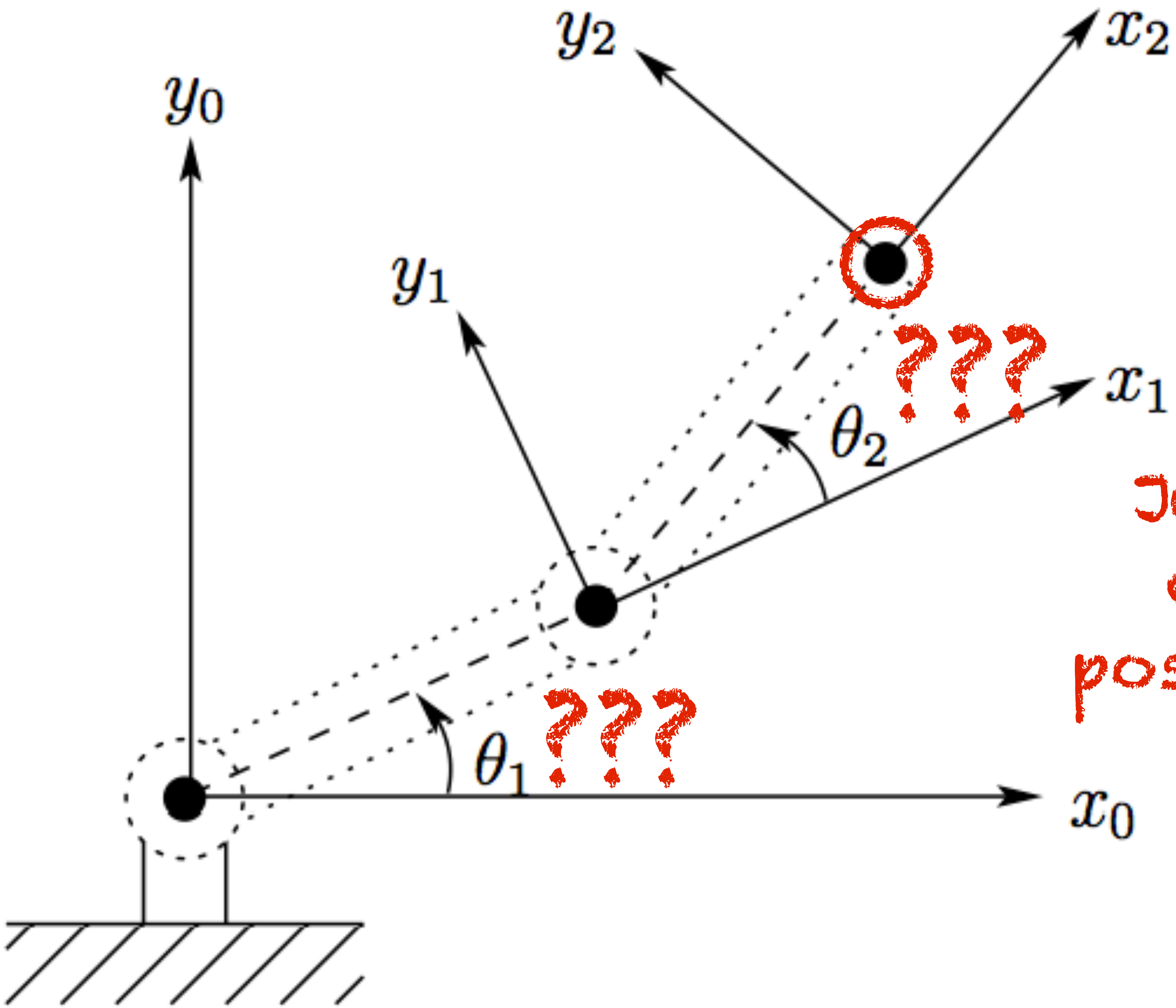
$$\text{endeffector}^{\text{world}} = T^{\text{world}}_1 T^1_{\text{tool}} \text{endeffector}^{\text{tool}}$$
$$\text{endeffector}^{\text{world}} = T^{\text{world}}_{\text{tool}}(\theta_1, \theta_2) \text{endeffector}^{\text{tool}}$$

Inverse kinematics: "given endeffector, compute configuration"



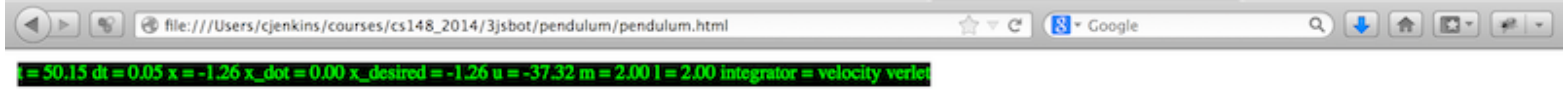
Inverse kinematics: $\mathbf{q} = f^{-1}([\mathbf{o}^0_N, \mathbf{R}^0_N])$

$[\theta_1, \theta_2] = f^{-1}(p^0)$



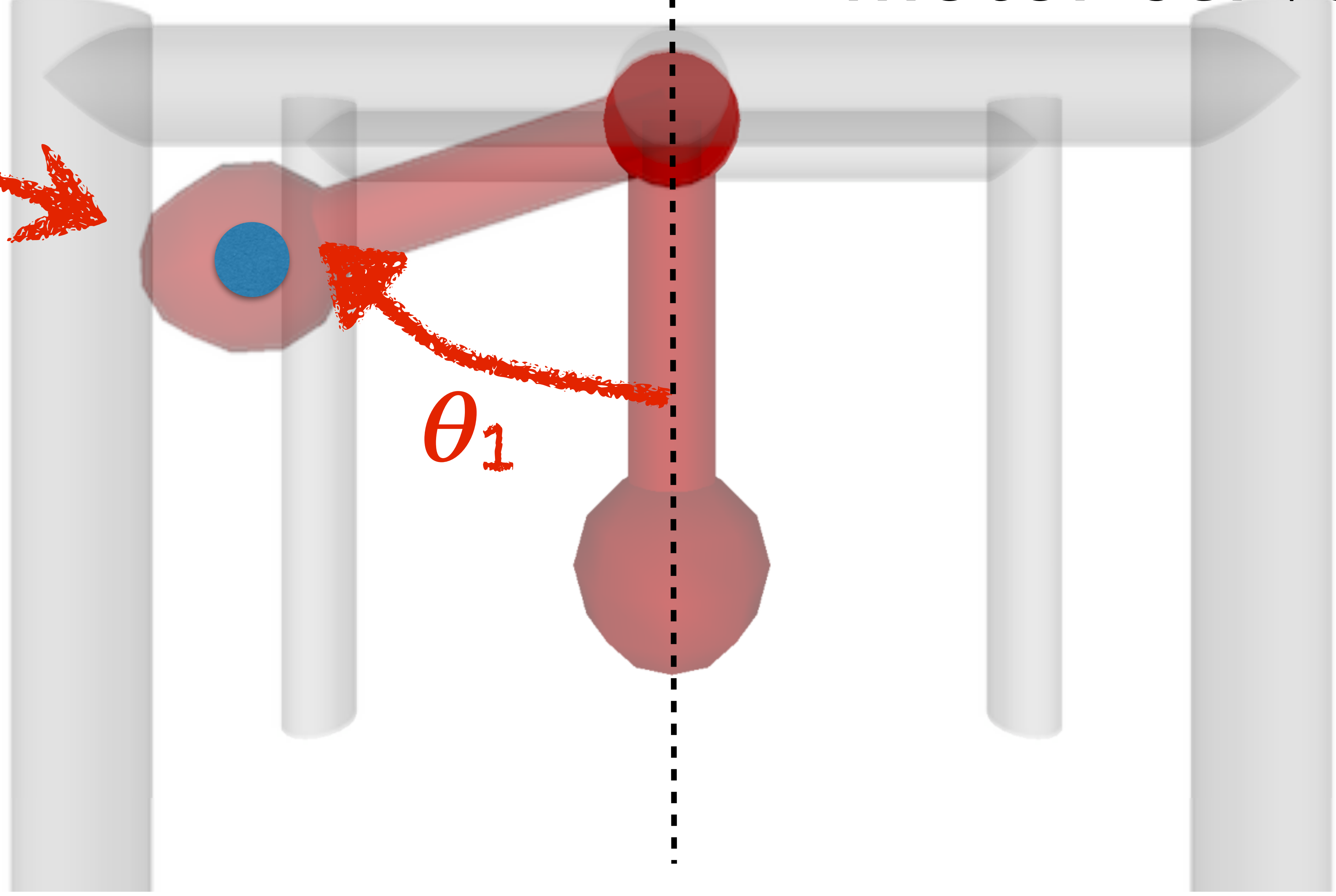
Just consider endeffector position for now

1DOF pendulum example



desired endeffector position ($\mathbf{o}^0_N$) given as an x,y location

assume:
1DOF motor at pendulum axis,
motor servo moves arm to angle θ_1



what is θ_1?

[redacted]

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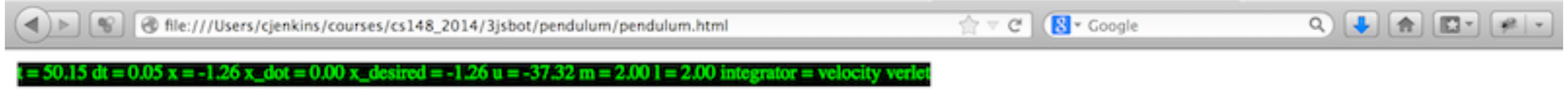

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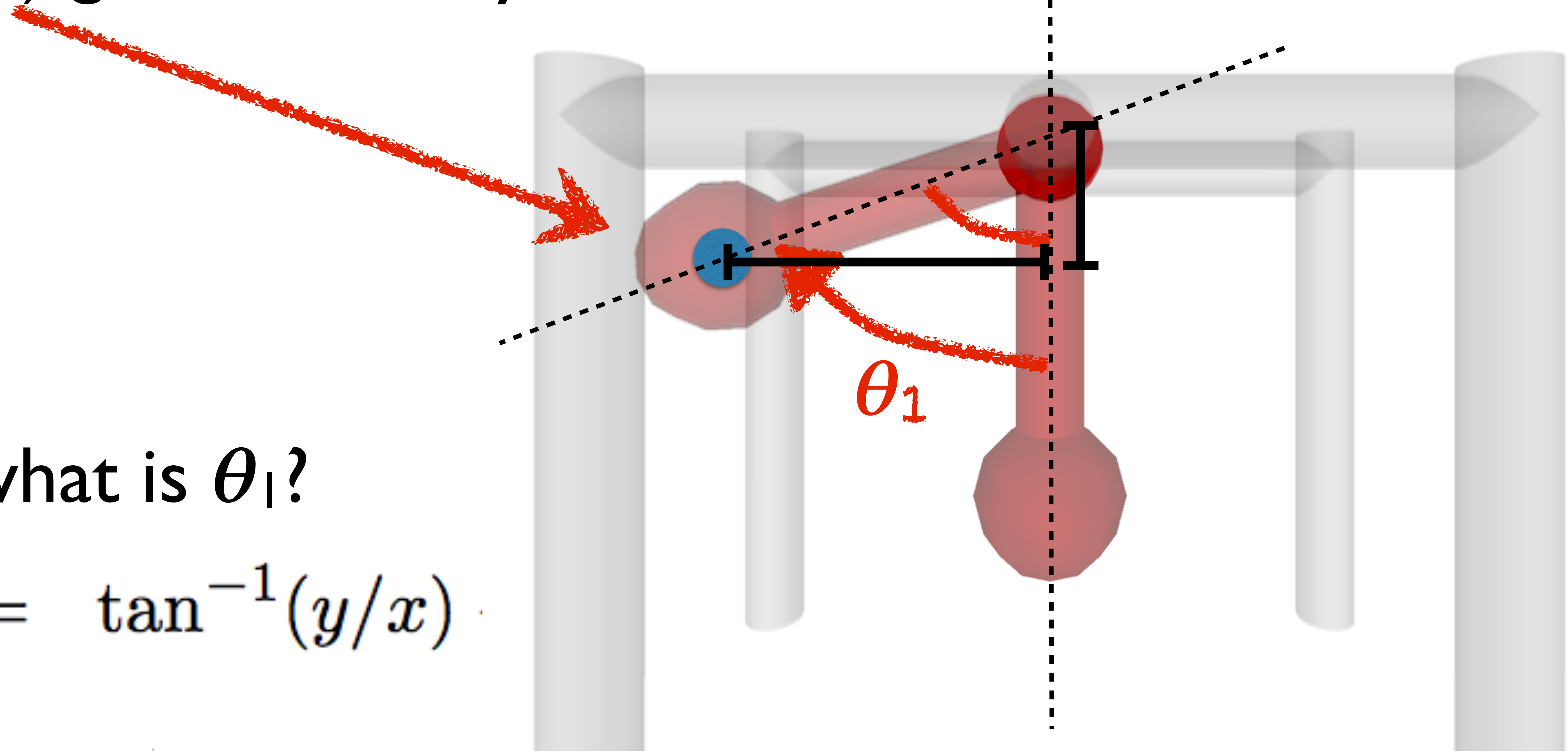
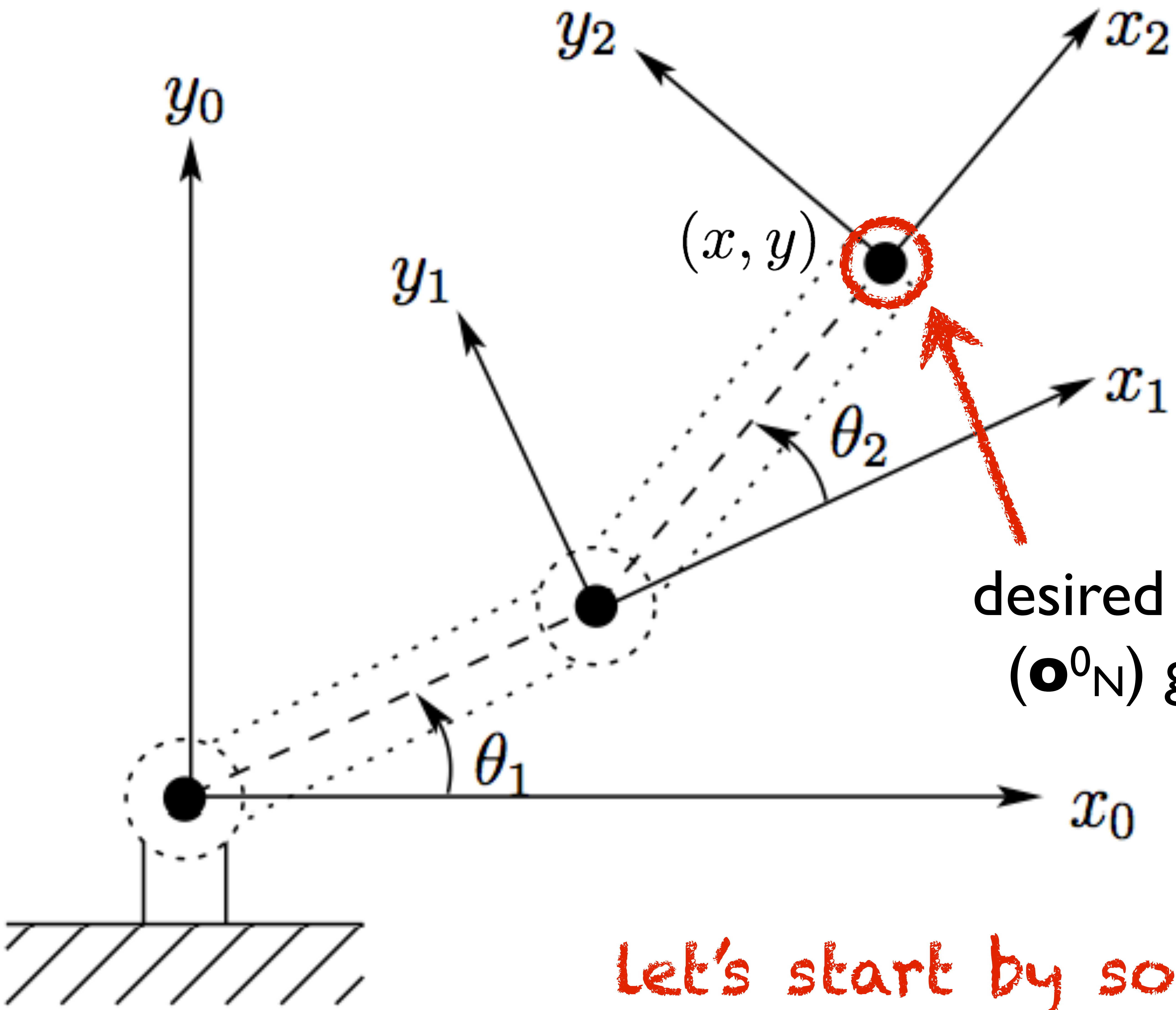


what is θ_1?

$$\theta_1 = \tan^{-1}(y/x)$$

Inverse kinematics: $\mathbf{q} = f^{-1}([\mathbf{o}^0_N, \mathbf{R}^0_N])$ $[\theta_1, \theta_2] = f^{-1}(x, y)$

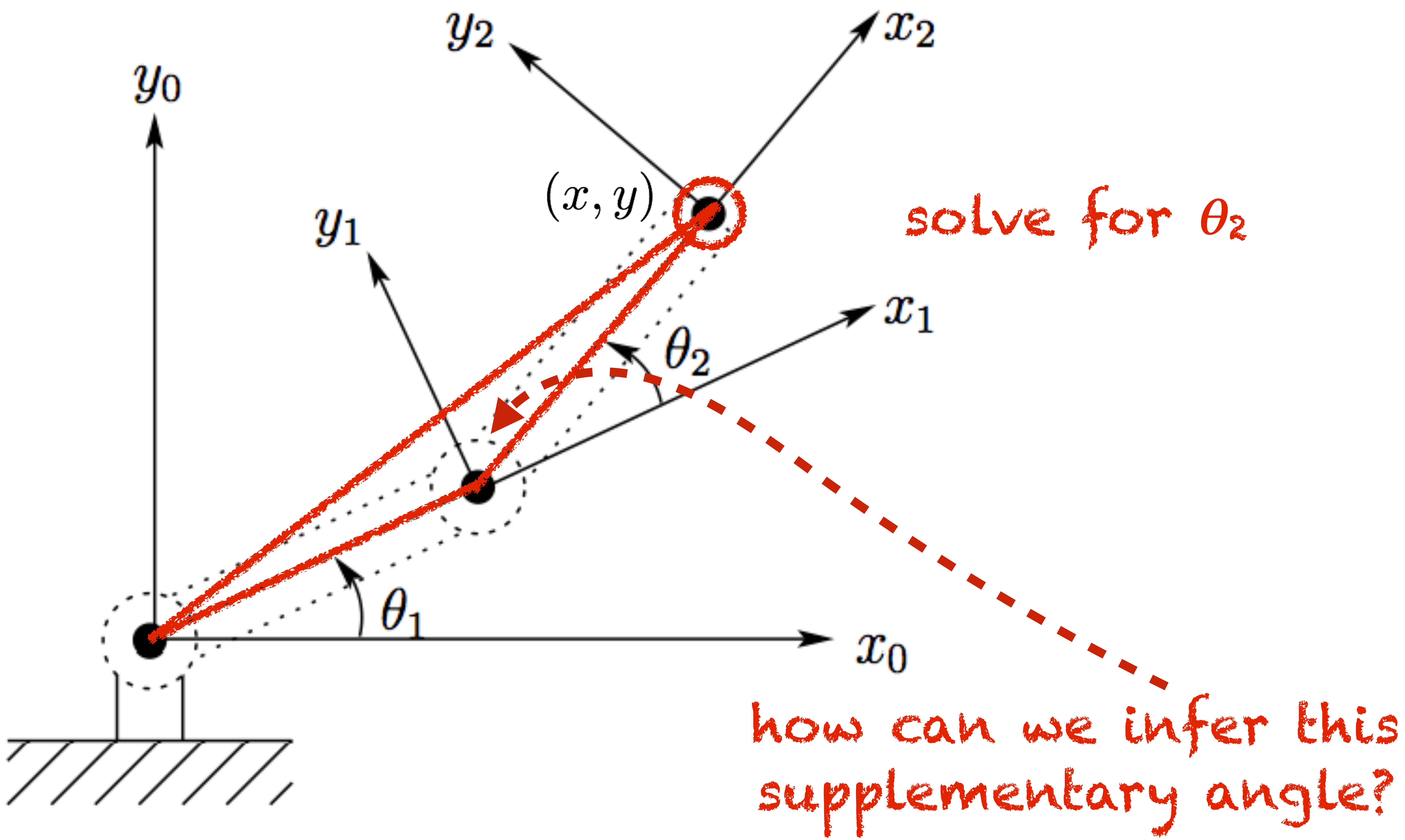


desired endeffector position ($\mathbf{o}^0_N$) given as location *x,y*

let's start by solving for θ_2

Inverse kinematics: $\mathbf{q} = f^{-1}([\mathbf{o}^0_N, \mathbf{R}^0_N])$

$[\theta_1, \theta_2] = f^{-1}(x,y)$



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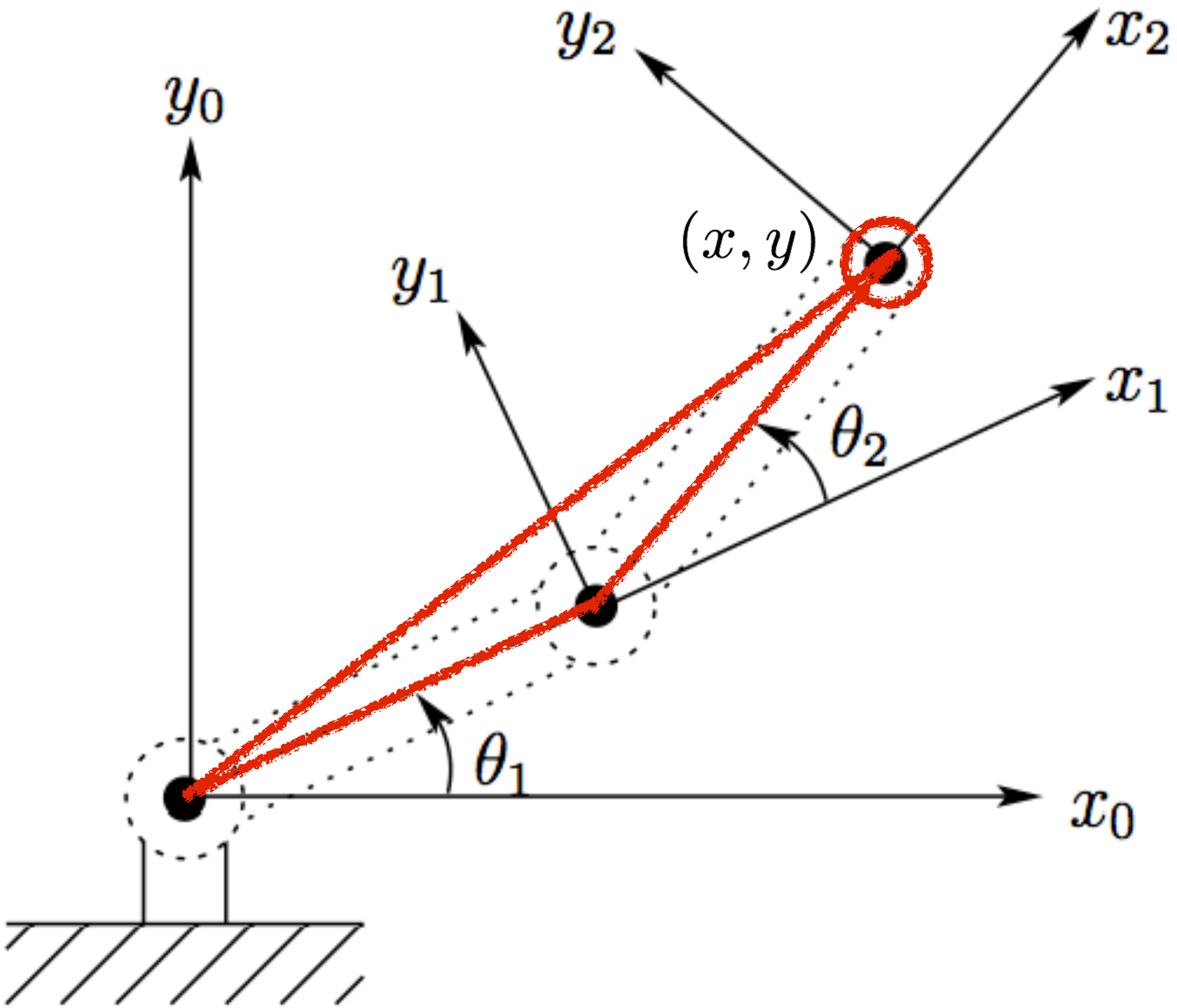
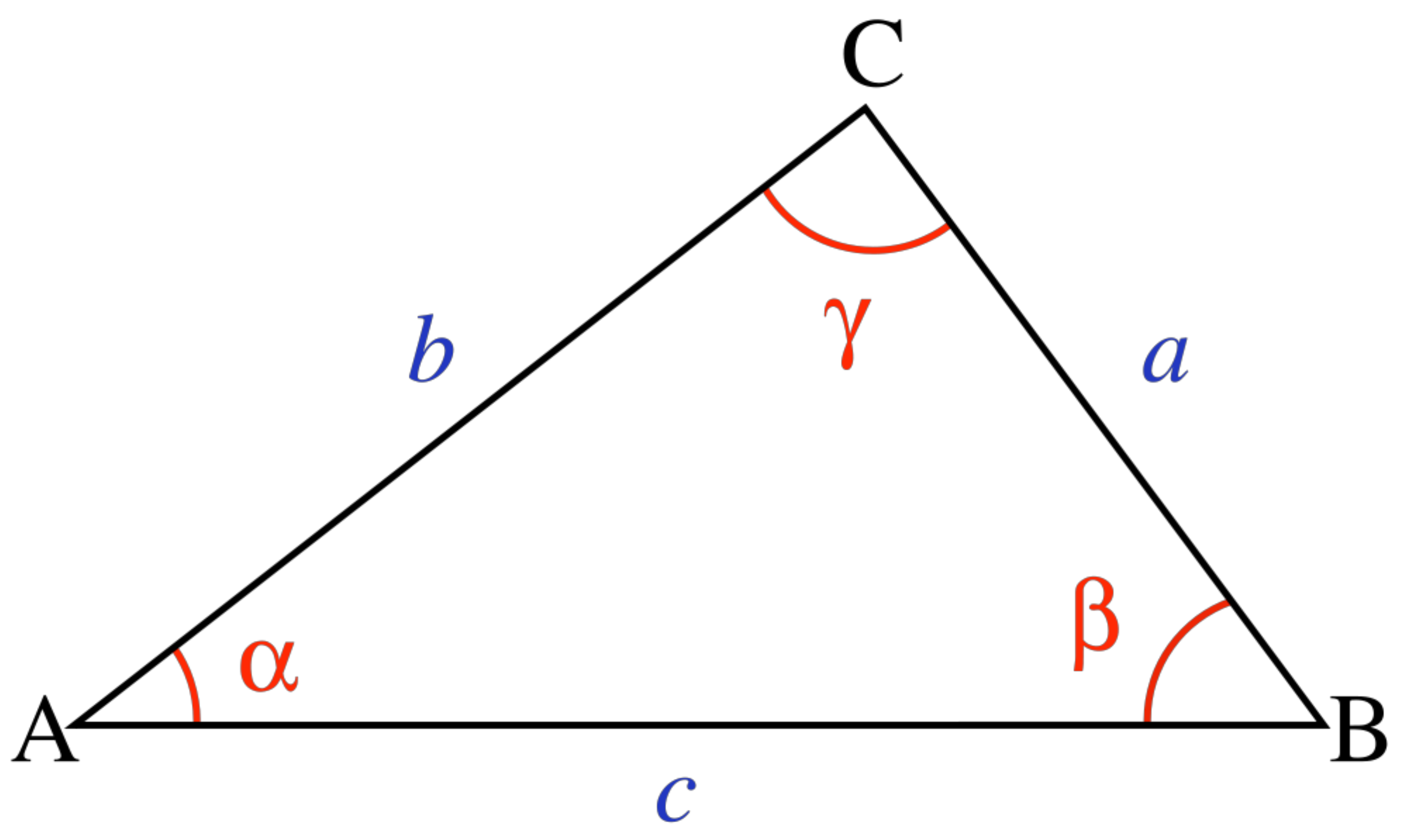


solve for θ_2

Law of Cosines

$$\gamma = \arccos\left(\frac{a^2 + b^2 - c^2}{2ab}\right)$$



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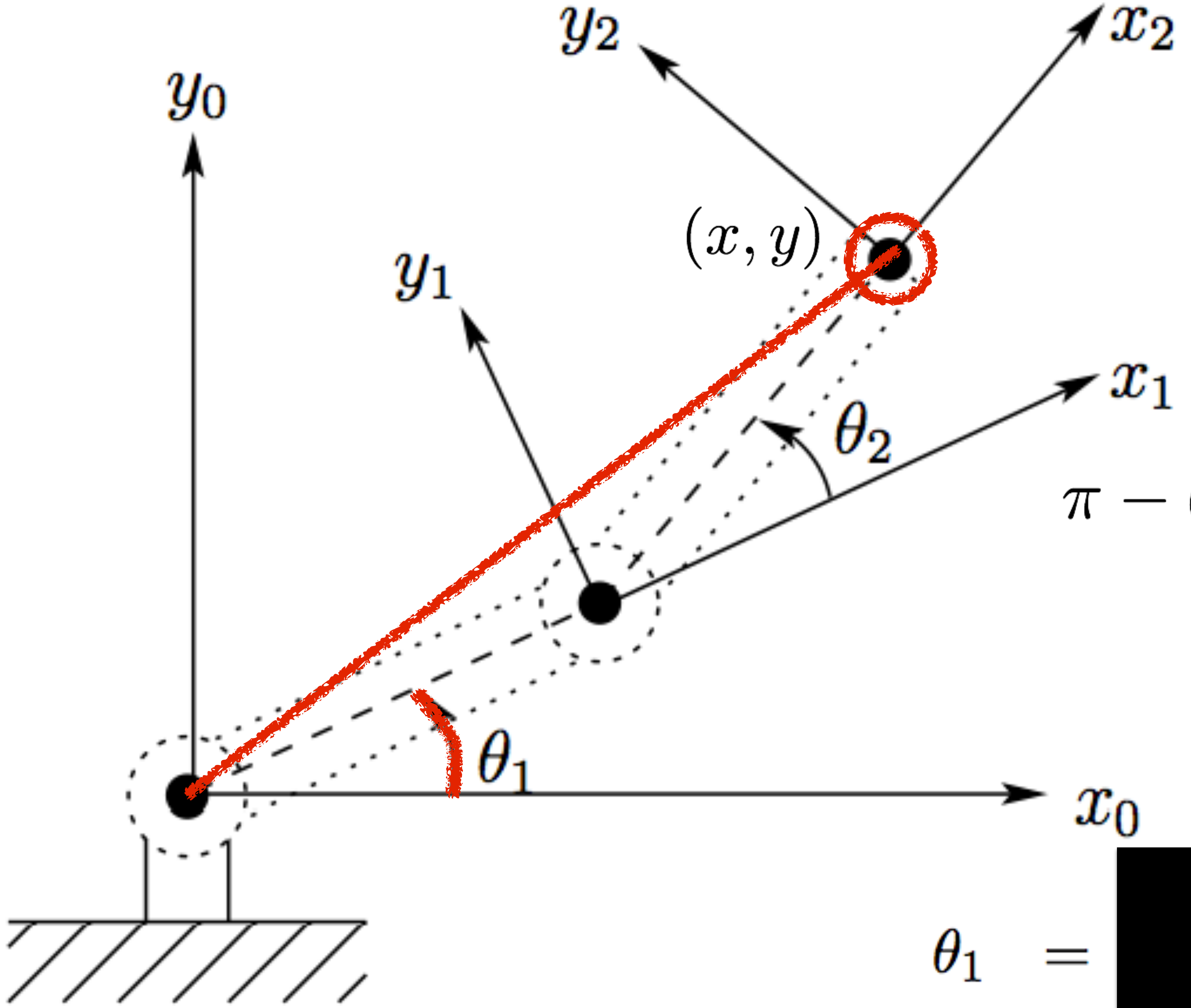


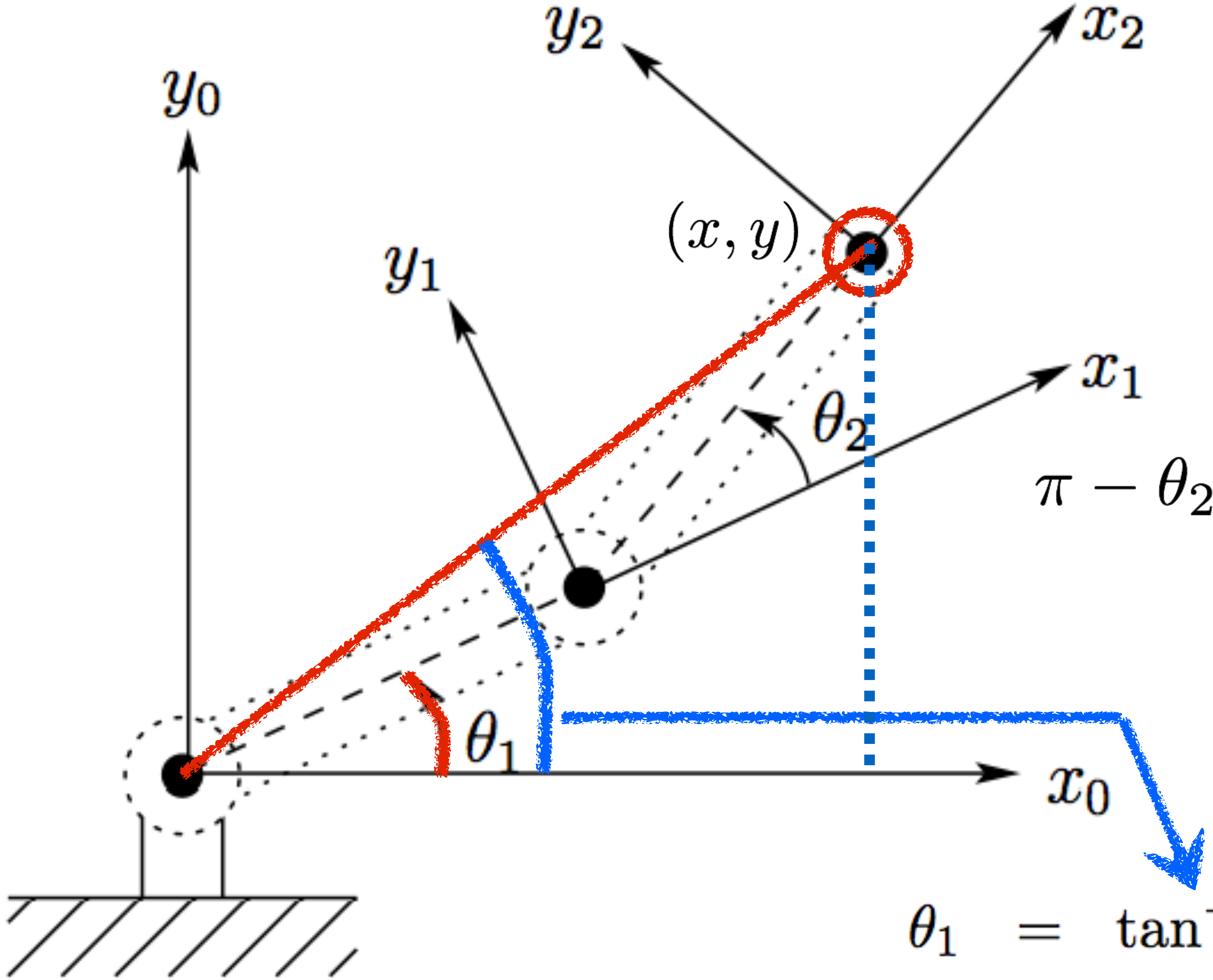
solve for θ_2

$$\pi - \theta_2 = cos^{-1}\left(\frac{\sqrt{x^2+y^2} - \alpha_1^2 - \alpha_2^2}{2\alpha_1\alpha_2}\right)$$

solve for θ_1

$\theta_1 =$ Consider two triangles

Inverse kinematics: $\mathbf{q} = f^{-1}([\mathbf{o}^0_N, \mathbf{R}^0_N])$ $[\theta_1, \theta_2] = f^{-1}(x, y)$



solve for θ_2

$$\pi - \theta_2 = cos^{-1}\left(\frac{\sqrt{x^2 + y^2} - \alpha_1^2 - \alpha_2^2}{2\alpha_1\alpha_2}\right)$$

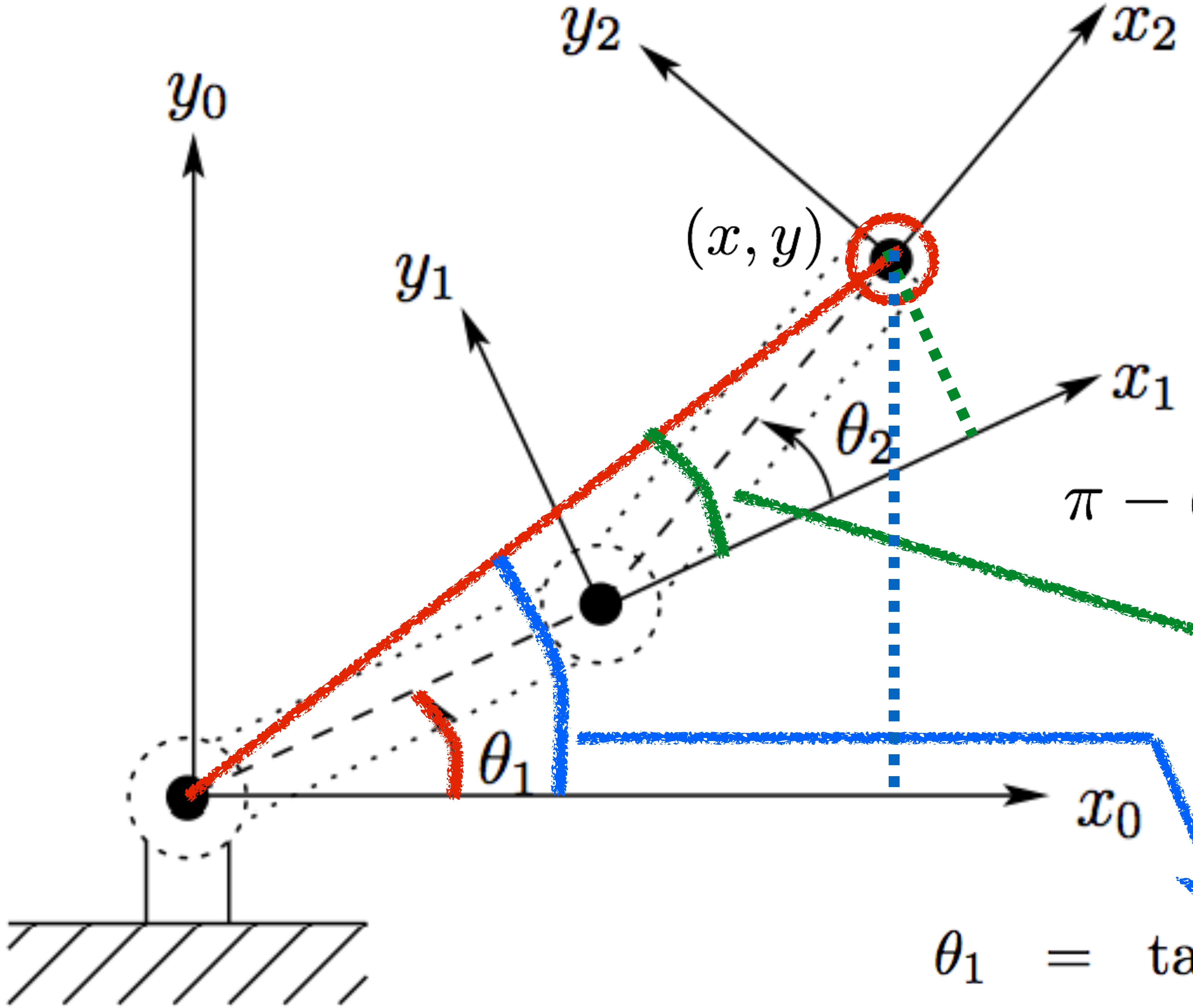
solve for θ_1

$$\theta_1 = \tan^{-1}(y/x) -$$

Consider two trian

Inverse kinematics: $\mathbf{q} = f^{-1}([\mathbf{o}^0_N, \mathbf{R}^0_N])$

$[\theta_1, \theta_2] = f^{-1}(x,y)$



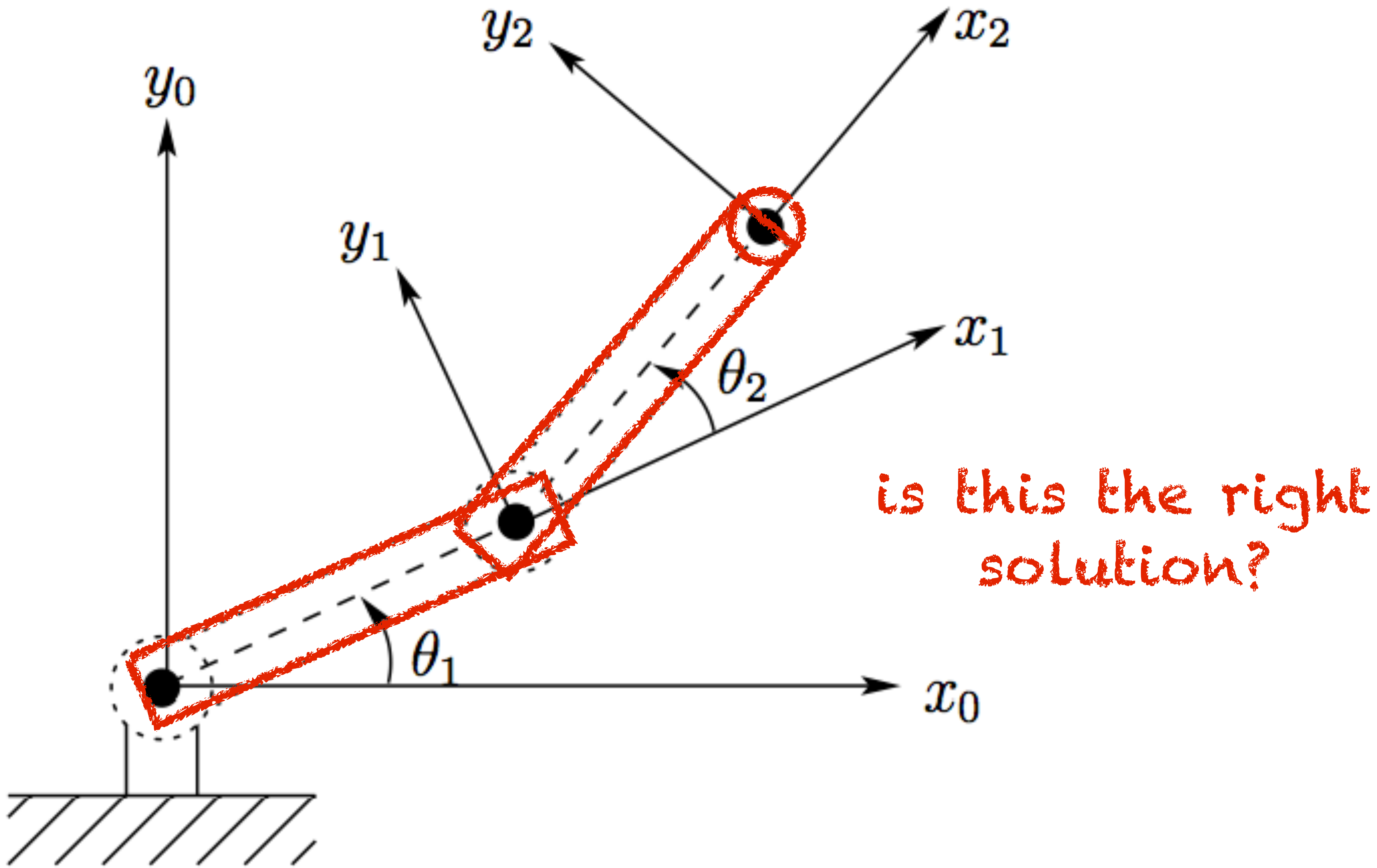
solve for θ_2

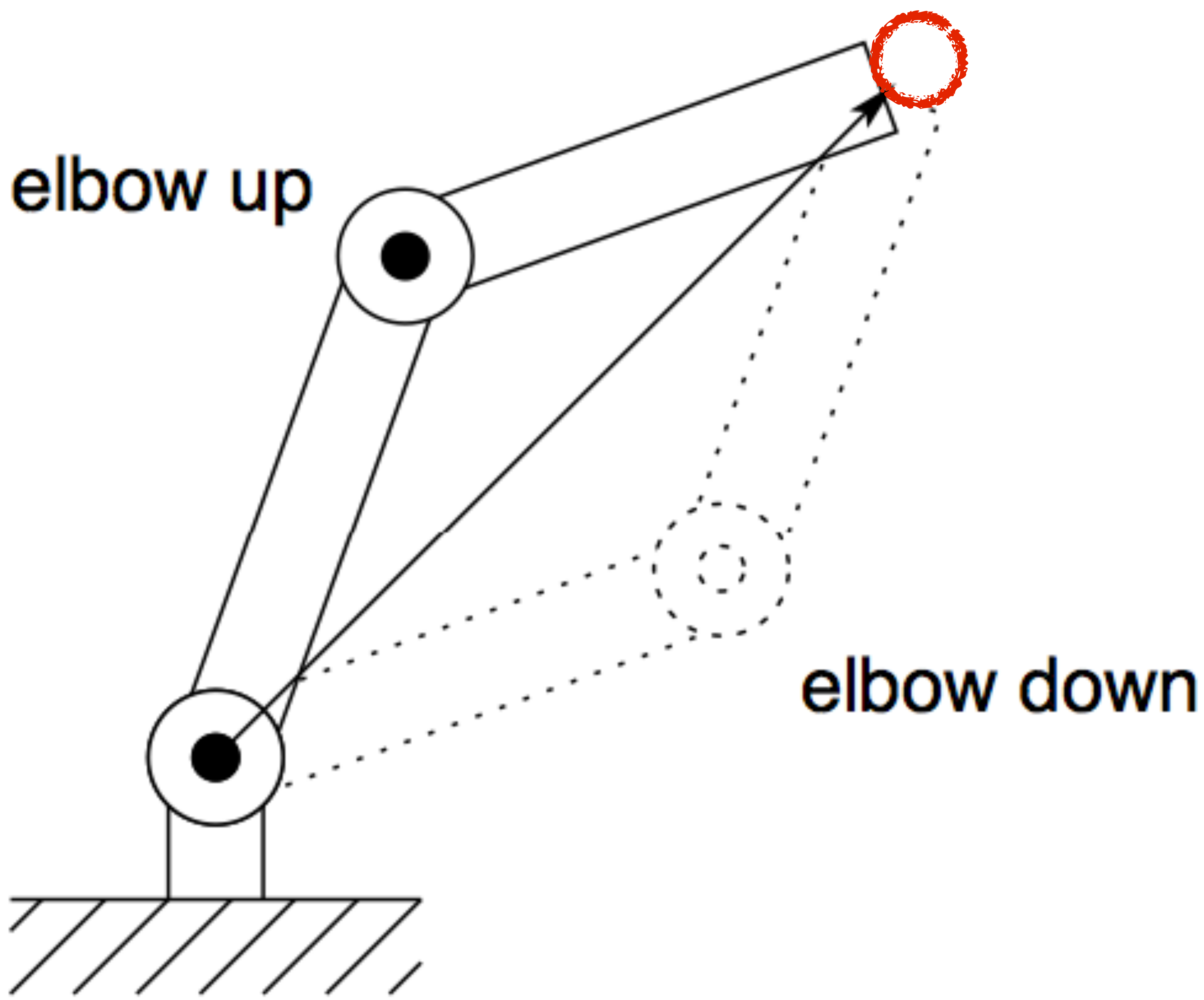
$$\pi - \theta_2 = cos^{-1}\left(\frac{\sqrt{x^2+y^2} - \alpha_1^2 - \alpha_2^2}{2\alpha_1\alpha_2}\right)$$

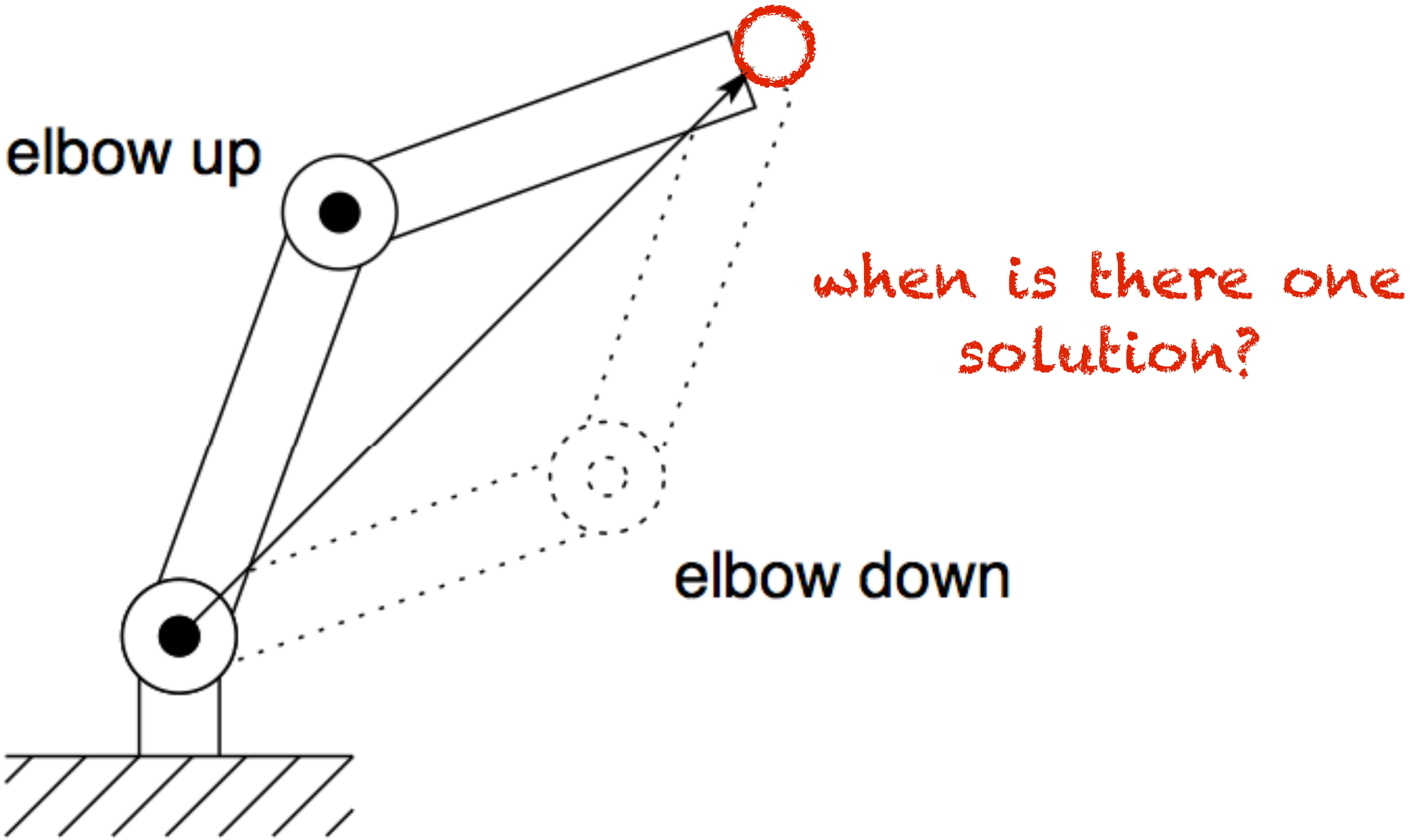
solve for θ_1

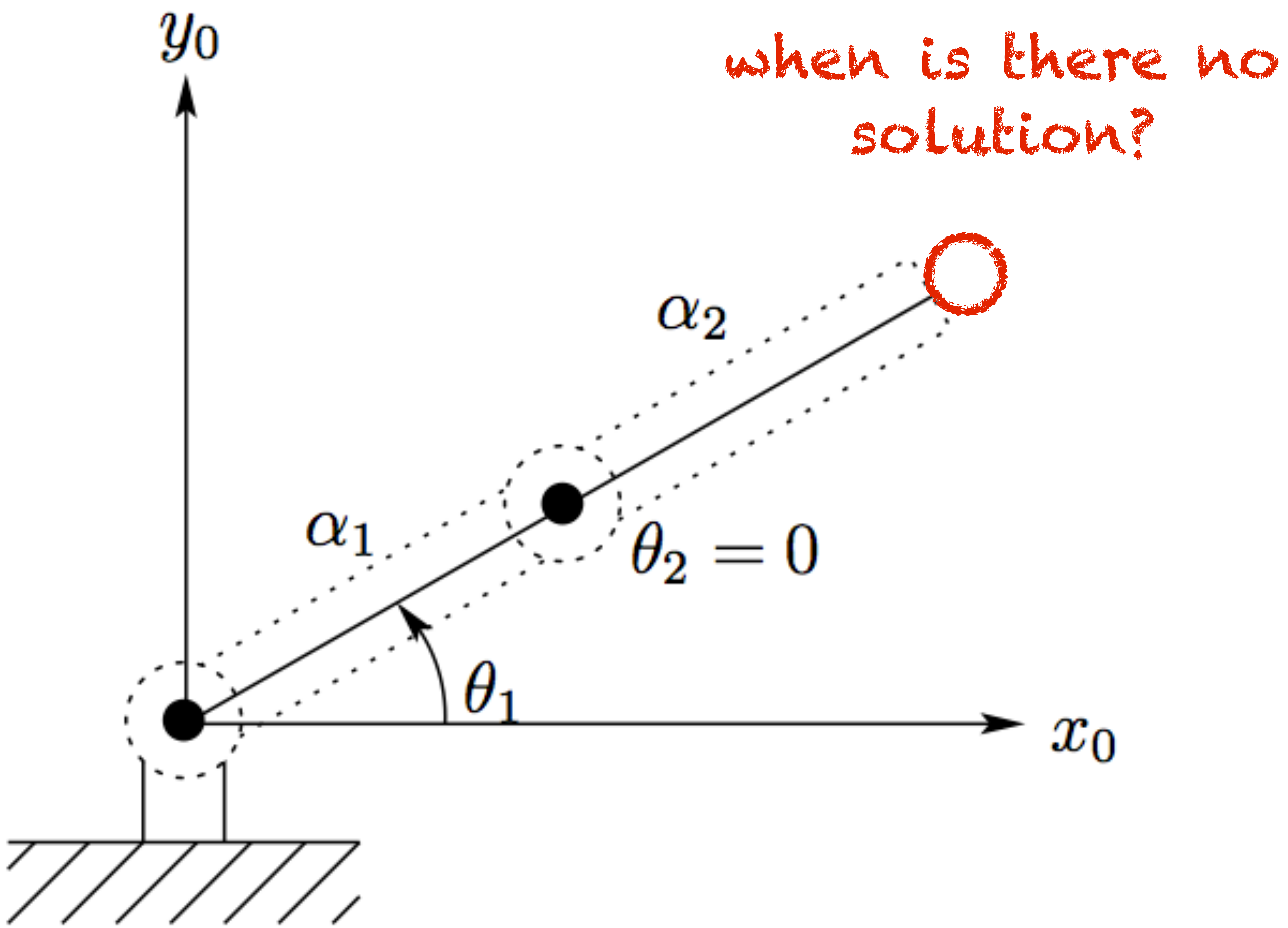
$$\theta_1 = \tan^{-1}(y/x) - \tan^{-1}\left(\frac{\alpha_2 \sin\theta_2}{\alpha_1 + \alpha_2\cos\theta_2}\right)$$

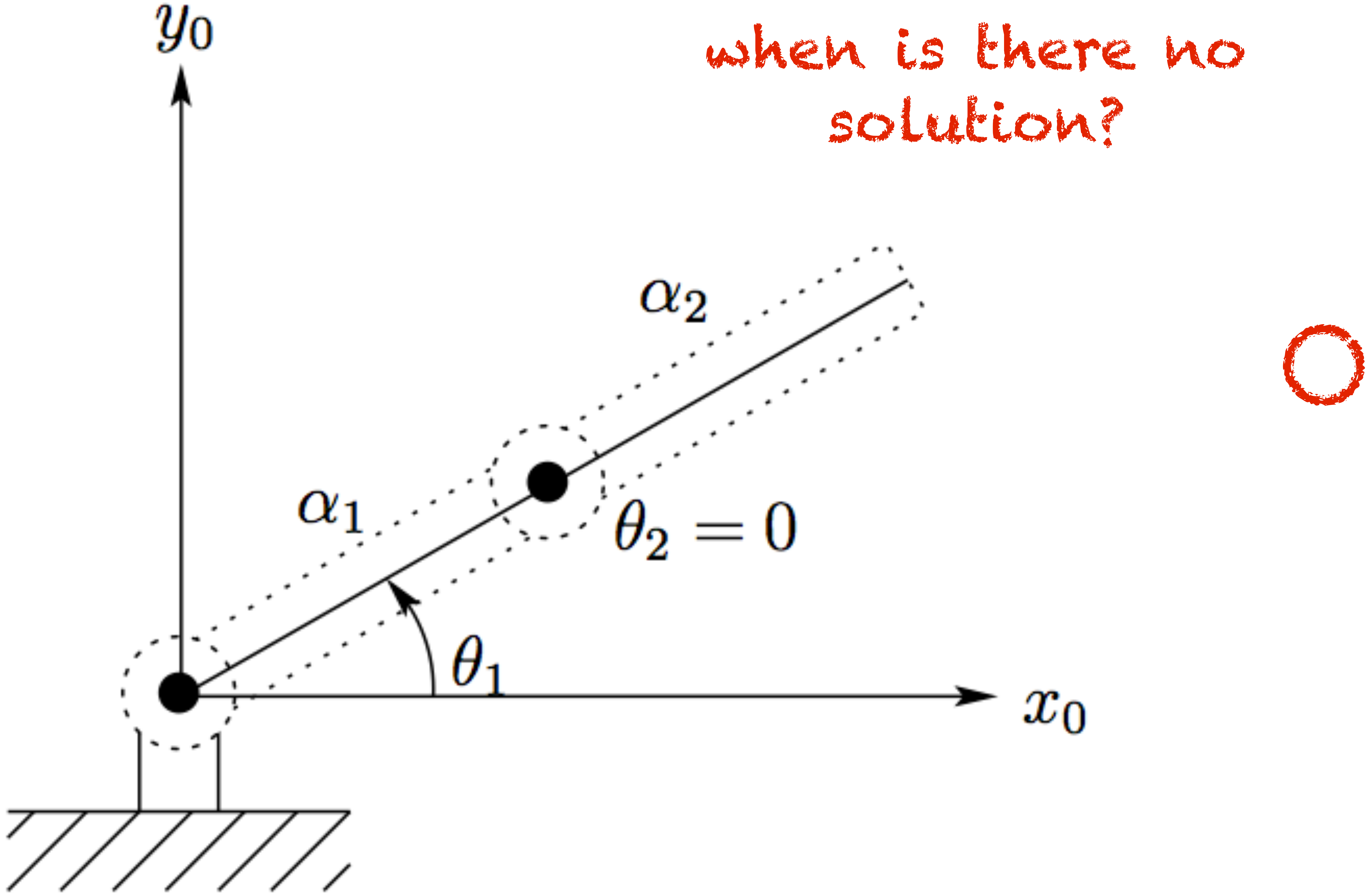
inverse kinematics: $(\theta_1,\theta_2) = f^{-1}(x,y)$




elbow up
elbow down


elbow up
elbow down
when is there one solution?


when is there no solution?
y_0
x_0
α_1
α_2
θ_1
$\theta_2 = 0$



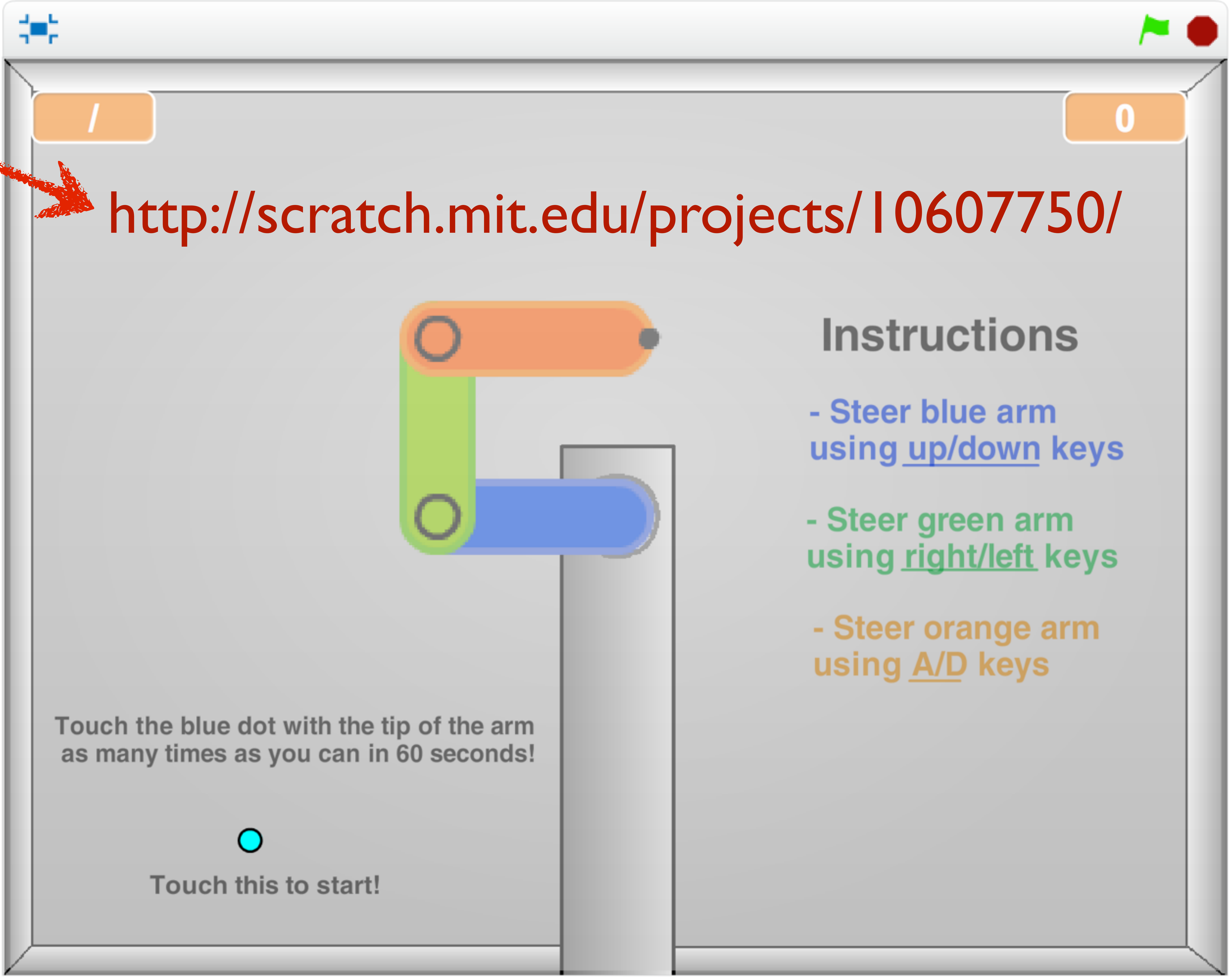
when is there no solution?

Can we do IK for 3 links?

SHALL WE PLAY A GAME?

Try this

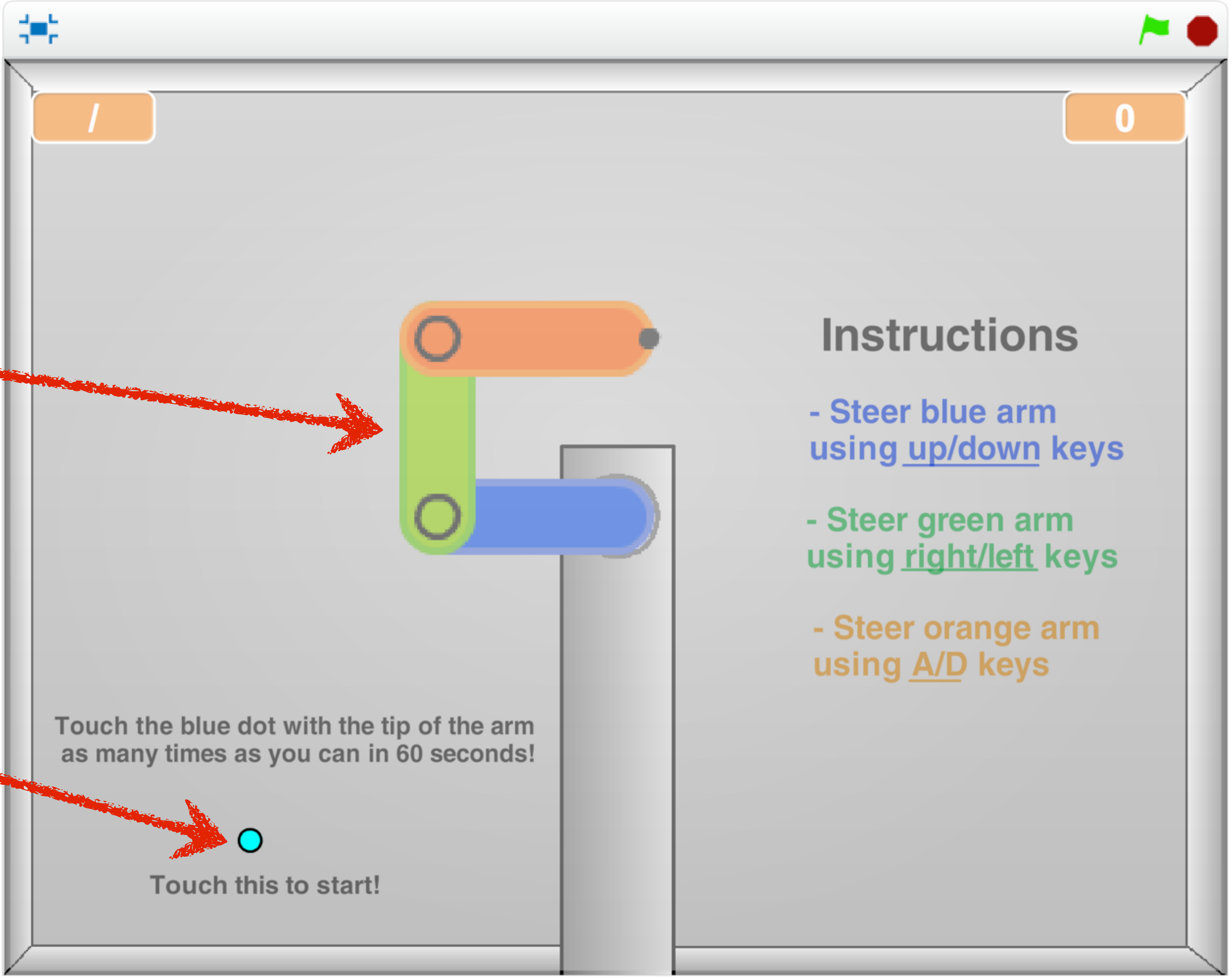
http://scratch.mit.edu/projects/10607750/



How many solutions for this arm?

3 unknowns

2 constraints



Remember: Ax=b

Inverse Kinematics: 2D

$$T_n^0(q_1, \ldots, q_n) \quad = \quad H$$

Inverse Kinematics: 2D

Configuration

$$T_n^0(q_1, \ldots, q_n) \quad = \quad H$$

Transform from endeffector frame to world frame

$$q = \begin{bmatrix} q_1 \\ q_2 \\ \ldots \\ q_n \end{bmatrix}$$

$$H \quad = \quad \begin{bmatrix} R & o \\ 0 & 1 \end{bmatrix}$$

$$H \quad = \quad \begin{bmatrix} r_{11} & r_{12} & o_x \\ r_{21} & r_{22} & o_y \\ 0 & 0 & 1 \end{bmatrix}$$

Inverse Kinematics: 2D

Configuration

$$T_n^0(q_1, \ldots, q_n) = H$$

Transform from endeffector frame to world frame

$$q = \begin{bmatrix} q_1 \\ q_2 \\ \ldots \\ q_n \end{bmatrix}$$

$$H = \begin{bmatrix} R & o \\ 0 & 1 \end{bmatrix}$$

Inverse orientation

$$R_n^0(q_1, \ldots, q_n) = R$$

$$o_n^0(q_1, \ldots, q_n) = o$$

Inverse position

$$H = \begin{bmatrix} r_{11} & r_{12} & o_x \\ r_{21} & r_{22} & o_y \\ 0 & 0 & 1 \end{bmatrix}$$

Inverse Kinematics: 2D

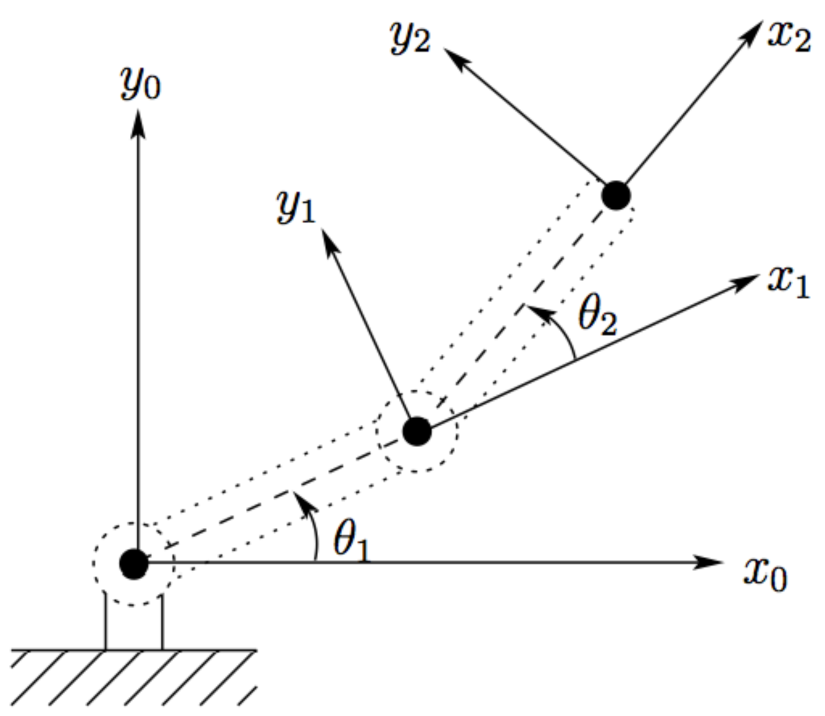
Configuration

$$T_n^0(q_1, \ldots, q_n) = H$$

Transform from endeffector

$$q = \begin{bmatrix} q_1 \\ q_2 \end{bmatrix}$$

$$H = \begin{bmatrix} R & o \\ 0 & 1 \end{bmatrix}$$



Closed form solution

$$H = \begin{bmatrix} r_{11} & r_{12} & o_x \\ r_{21} & r_{22} & o_y \\ 0 & 0 & 1 \end{bmatrix}$$

Inverse Kinematics: 2D

Configuration

$$T_n^0(q_1, \ldots, q_n) = H$$

Transform from endeffector

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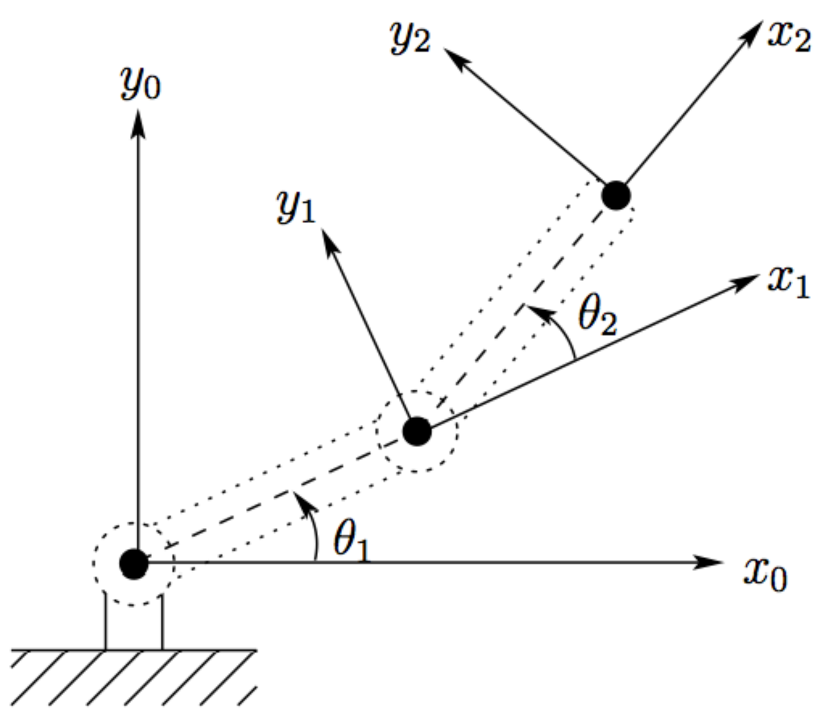


Closed form solution

$$\theta_2 = cos^{-1}\left(\frac{x^2 + y^2 - \alpha_1^2 - \alpha_2^2}{2\alpha_1\alpha_2}\right)$$

$$\theta_1 = \tan^{-1}(y/x) - \tan^{-1}\left(\frac{\alpha_2 \sin\theta_2}{\alpha_1 + \alpha_2 \cos\theta_2}\right)$$

$$H = \begin{bmatrix} r_{11} & r_{12} & o_x \\ r_{21} & r_{22} & o_y \\ 0 & 0 & 1 \end{bmatrix}$$

Inverse Kinematics: 3D

Configuration

$$T_n^0(q_1, \ldots, q_n) = H$$

← Transform from endeffector

$$q = \begin{bmatrix} q_1 \\ q_2 \\ \ldots \\ q_n \end{bmatrix}$$

$$H = \begin{bmatrix} R & o \\ 0 & 1 \end{bmatrix}$$

6 DOF position and orientation of endeffector

$$H = \begin{bmatrix} r_{11} & r_{12} & r_{13} & o_x \\ r_{21} & r_{22} & r_{23} & o_y \\ r_{31} & r_{32} & r_{33} & o_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Inverse Kinematics: 3D

Configuration

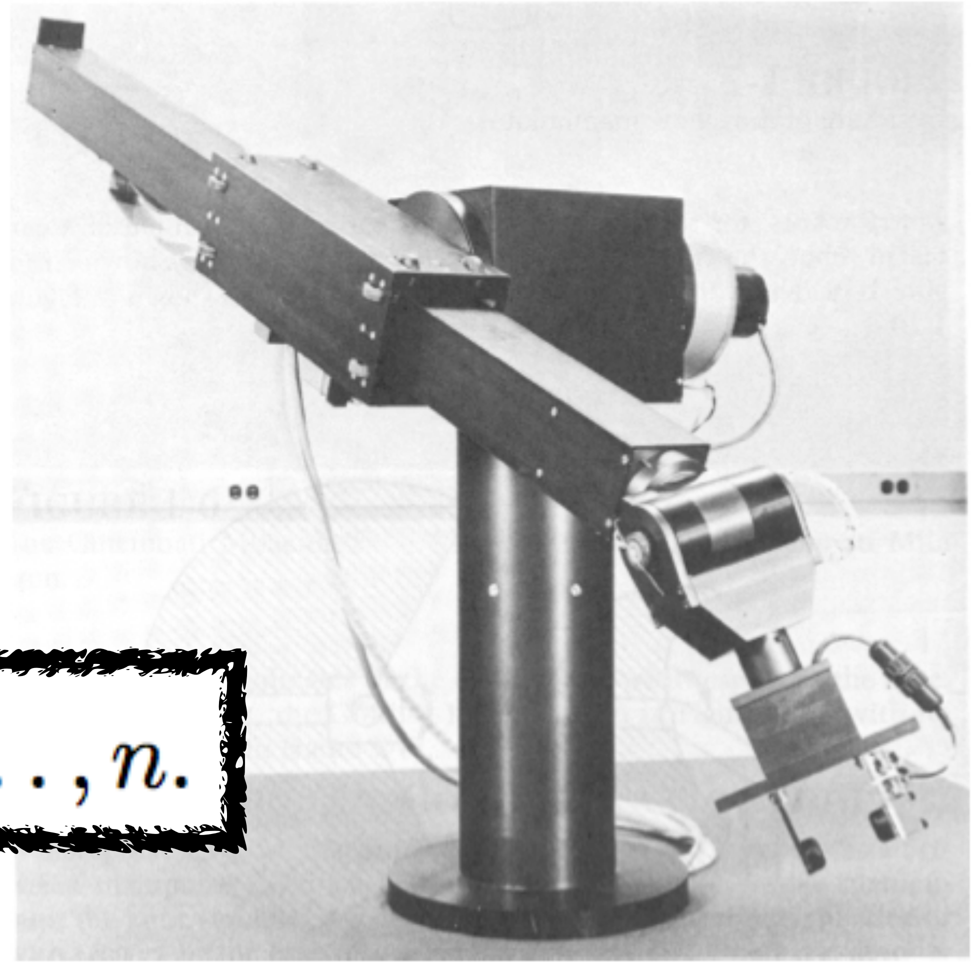
$$T_n^0(q_1, \ldots, q_n) \quad = \quad H$$

Transform from endeffector

$$q = \begin{bmatrix} q_1 \\ q_2 \\ \ldots \\ q_6 \end{bmatrix}$$

$$H \quad = \quad \begin{bmatrix} R & o \\ 0 & 1 \end{bmatrix}$$

Closed form solution?

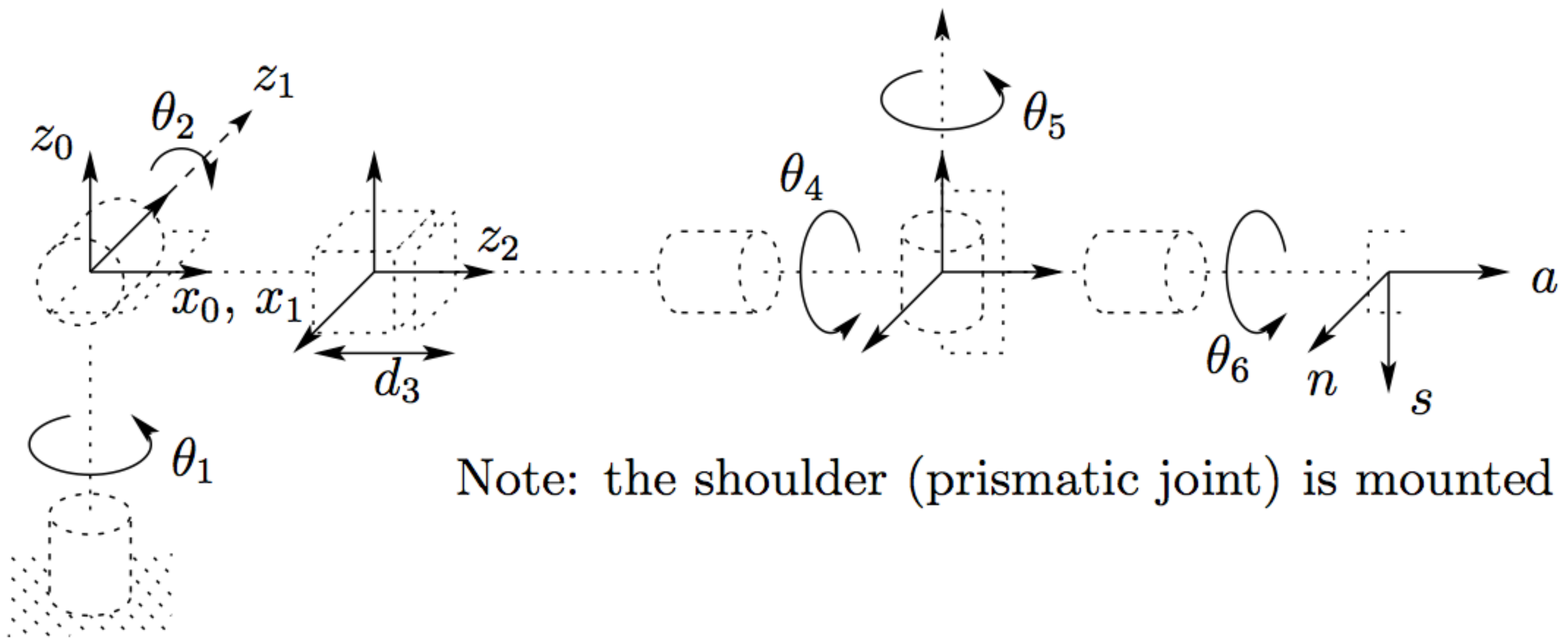


$$H \quad = \quad \begin{bmatrix} r_{11} & r_{12} & r_{13} & o_x \\ r_{21} & r_{22} & r_{23} & o_y \\ r_{31} & r_{32} & r_{33} & o_z \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

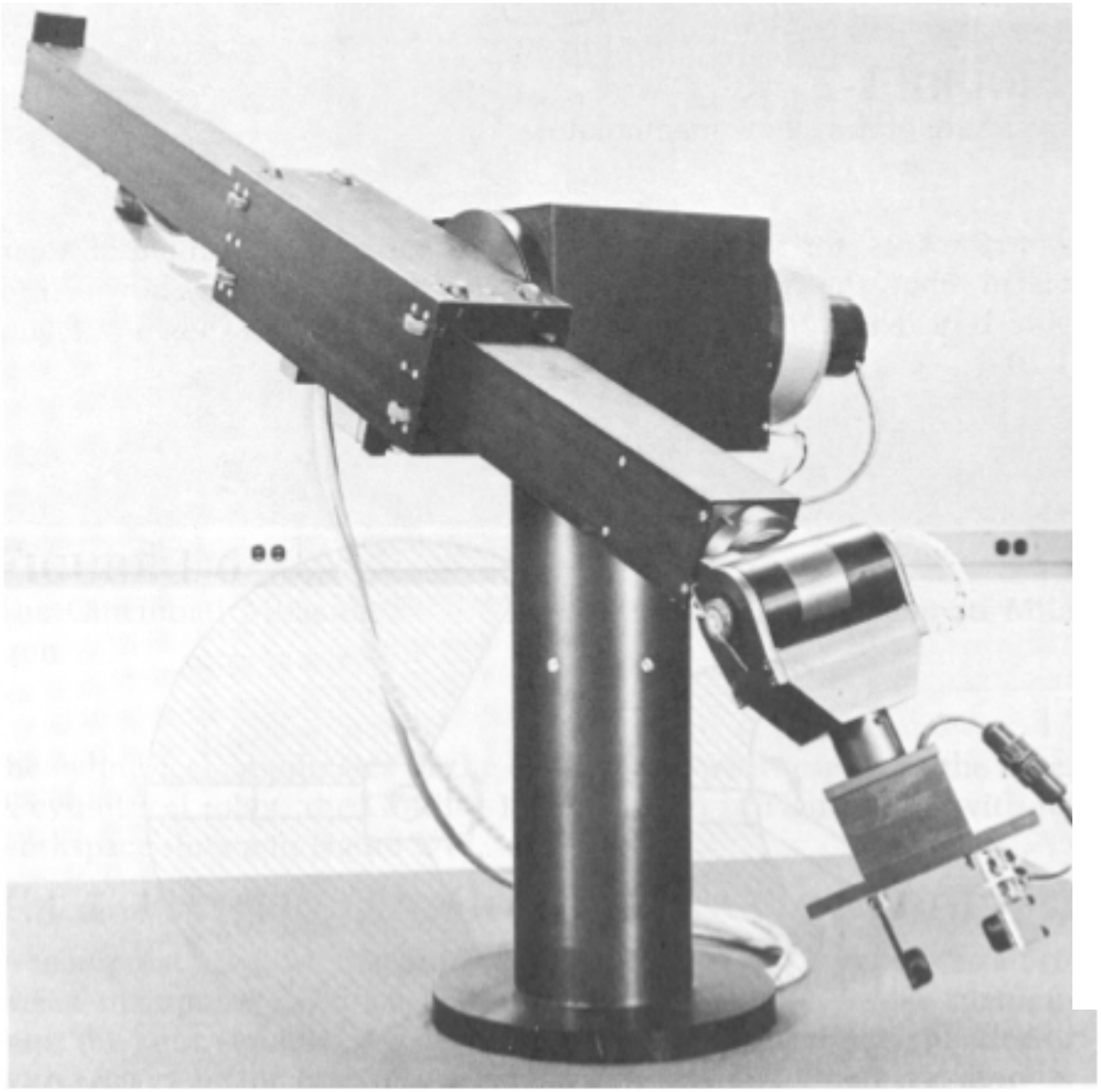
6 DOF position and orientation of endeffector

$$q_k \quad = \quad f_k(h_{11}, \ldots, h_{34}), \qquad k = 1, \ldots, n.$$

Stanford Manipulator



Note: the shoulder (prismatic joint) is mounted wrong.



$$
\begin{aligned}
c_1[c_2(c_4c_5c_6 - s_4s_6) - s_2s_5c_6] - s_1(s_4c_5c_6 + c_4s_6) &= r_{11} \\
s_1[c_2(c_4c_5c_6 - s_4s_6) - s_2s_5c_6] + c_1(s_4c_5c_6 + c_4s_6) &= r_{21} \\
-s_2(c_4c_5c_6 - s_4s_6) - c_2s_5s_6 &= r_{31} \\
c_1[-c_2(c_4c_5s_6 + s_4c_6) + s_2s_5s_6] - s_1(-s_4c_5s_6 + c_4c_6) &= r_{12} \\
s_1[-c_2(c_4c_5s_6 + s_4c_6) + s_2s_5s_6] + c_1(-s_4c_5s_6 + c_4c_6) &= r_{22} \\
s_2(c_4c_5s_6 + s_4c_6) + c_2s_5s_6 &= r_{32} \\
c_1(c_2c_4s_5 + s_2c_5) - s_1s_4s_5 &= r_{13} \\
s_1(c_2c_4s_5 + s_2c_5) + c_1s_4s_5 &= r_{23} \\
-s_2c_4s_5 + c_2c_5 &= r_{33} \\
c_1s_2d_3 - s_1d_2 + d_6(c_1c_2c_4s_5 + c_1c_5s_2 - s_1s_4s_5) &= o_x \\
s_1s_2d_3 + c_1d_2 + d_6(c_1s_4s_5 + c_2c_4s_1s_5 + c_5s_1s_2) &= o_y \\
c_2d_3 + d_6(c_2c_5 - c_4s_2s_5) &= o_z.
\end{aligned}
$$

assumes D-H frames


Recognize this robot?

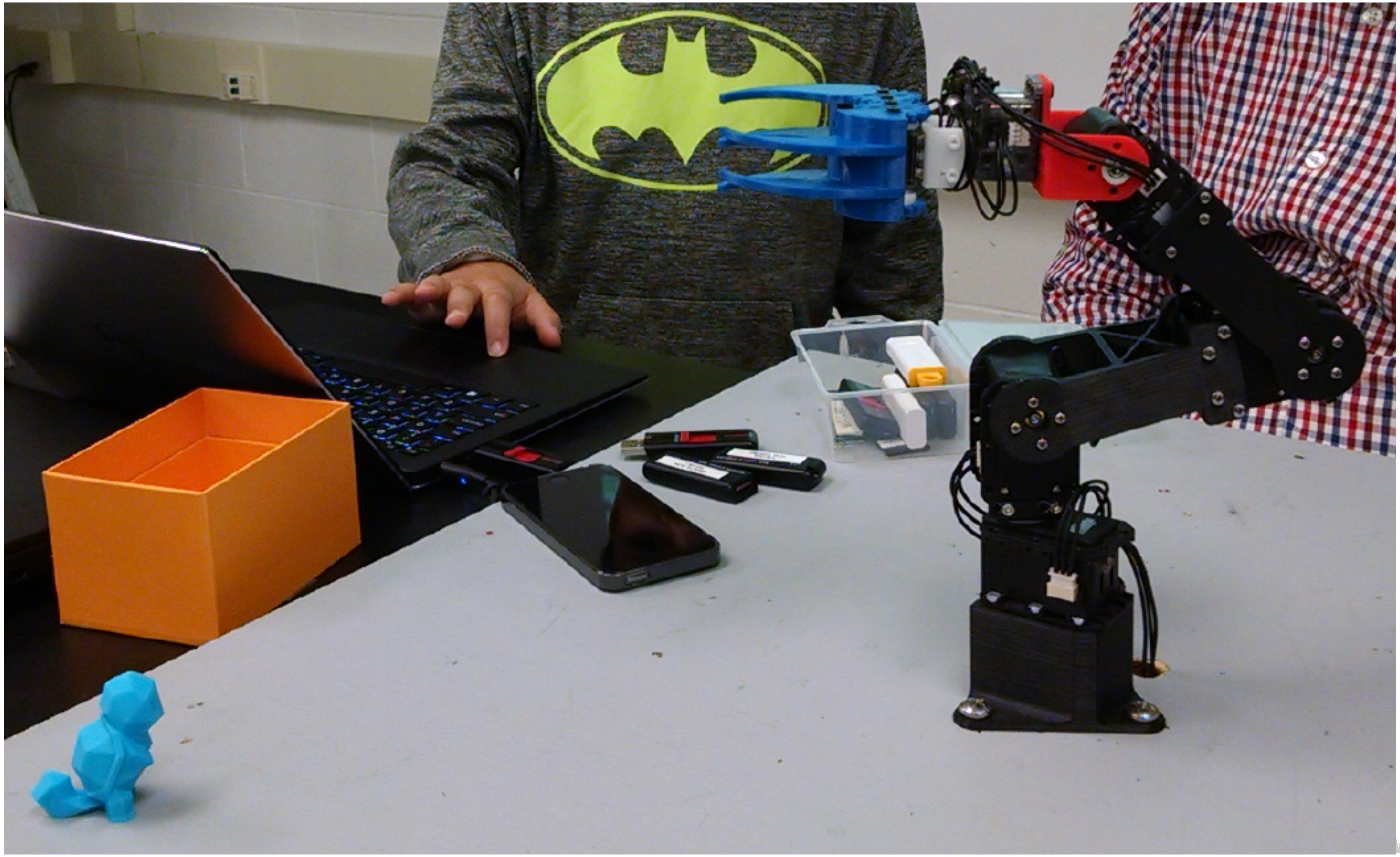

Detect, pick, and place each character
ROB 550 - Fall 2016

Robot Air Hockey - Attisha, Jiminez, Mulani - EECS 467 - Winter 2017

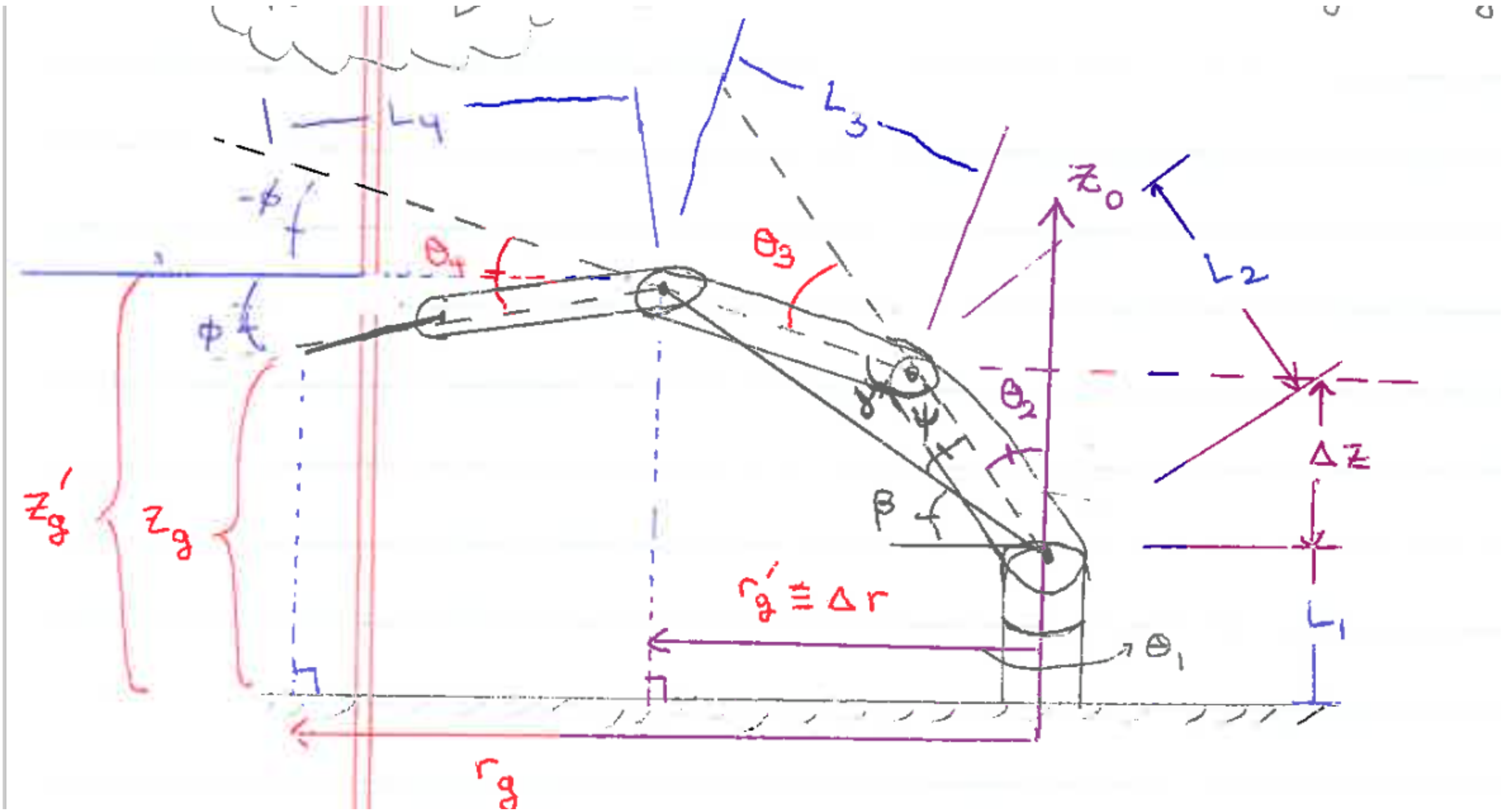
I'll Be Bach - Patric, Miller, Goswami, Bohr - EECS 467 - Winter 2017


x16
RoBob Ross - Rabideau, Ekins, Rao, Jones - EECS 467 - Winter 2017

RexArm (EECS 467 / ROB 550)



RexArm (EECS 467 / ROB 550)



Find: configuration

$\boldsymbol{q} = [\boldsymbol{\theta}_1\ \boldsymbol{\theta}_2\ \boldsymbol{\theta}_3\ \boldsymbol{\theta}_4]$

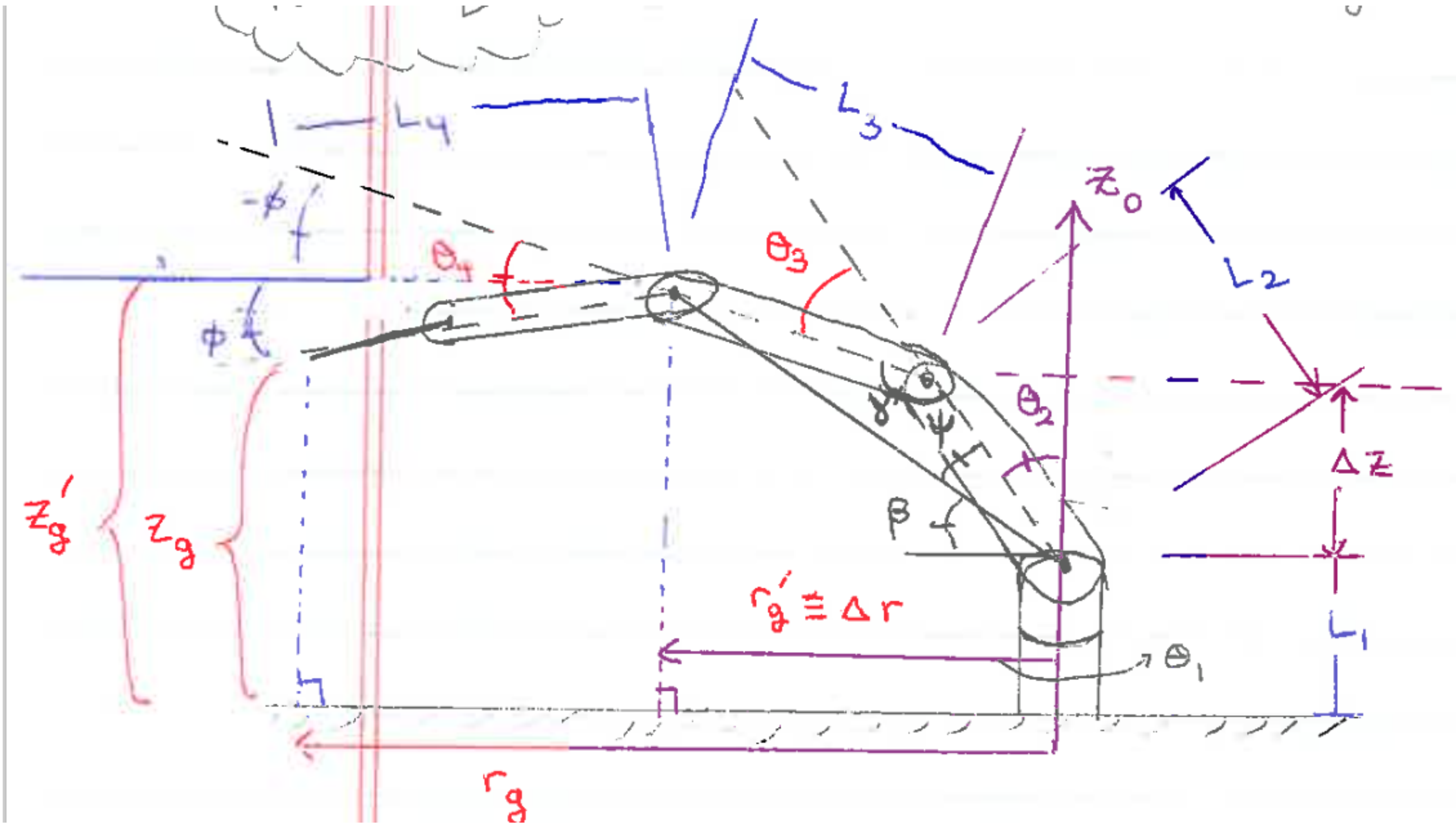
as robot joint angles

Given:

Find: configuration

$\boldsymbol{q} = [\boldsymbol{\theta}_1\ \boldsymbol{\theta}_2\ \boldsymbol{\theta}_3\ \boldsymbol{\theta}_4]$

as robot joint angles



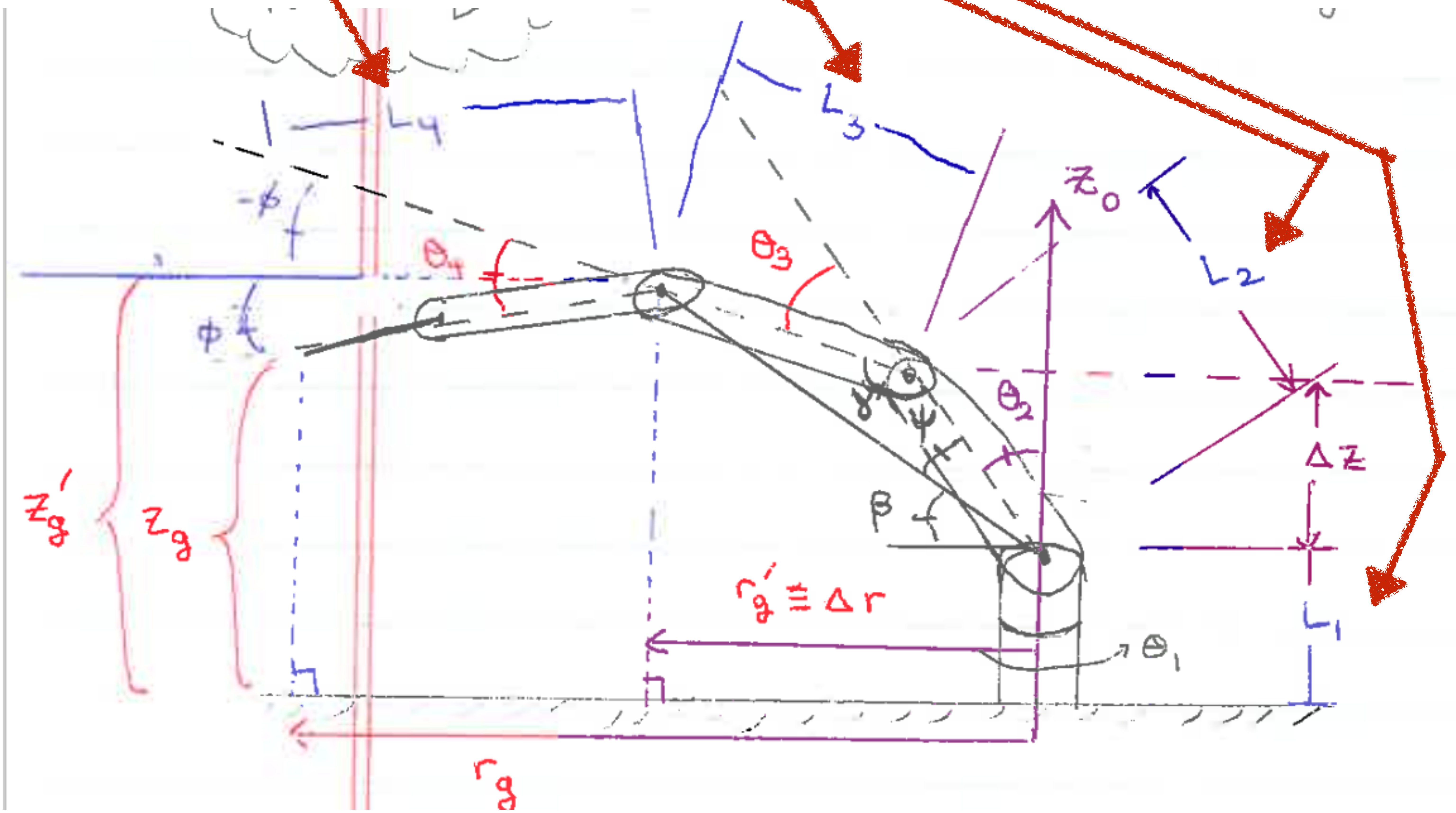
Given:

link lengths (L_4,L_3,L_2,L_1)

Find: configuration

$\boldsymbol{q} = [\boldsymbol{\theta}_1\ \boldsymbol{\theta}_2\ \boldsymbol{\theta}_3\ \boldsymbol{\theta}_4]$

as robot joint angles



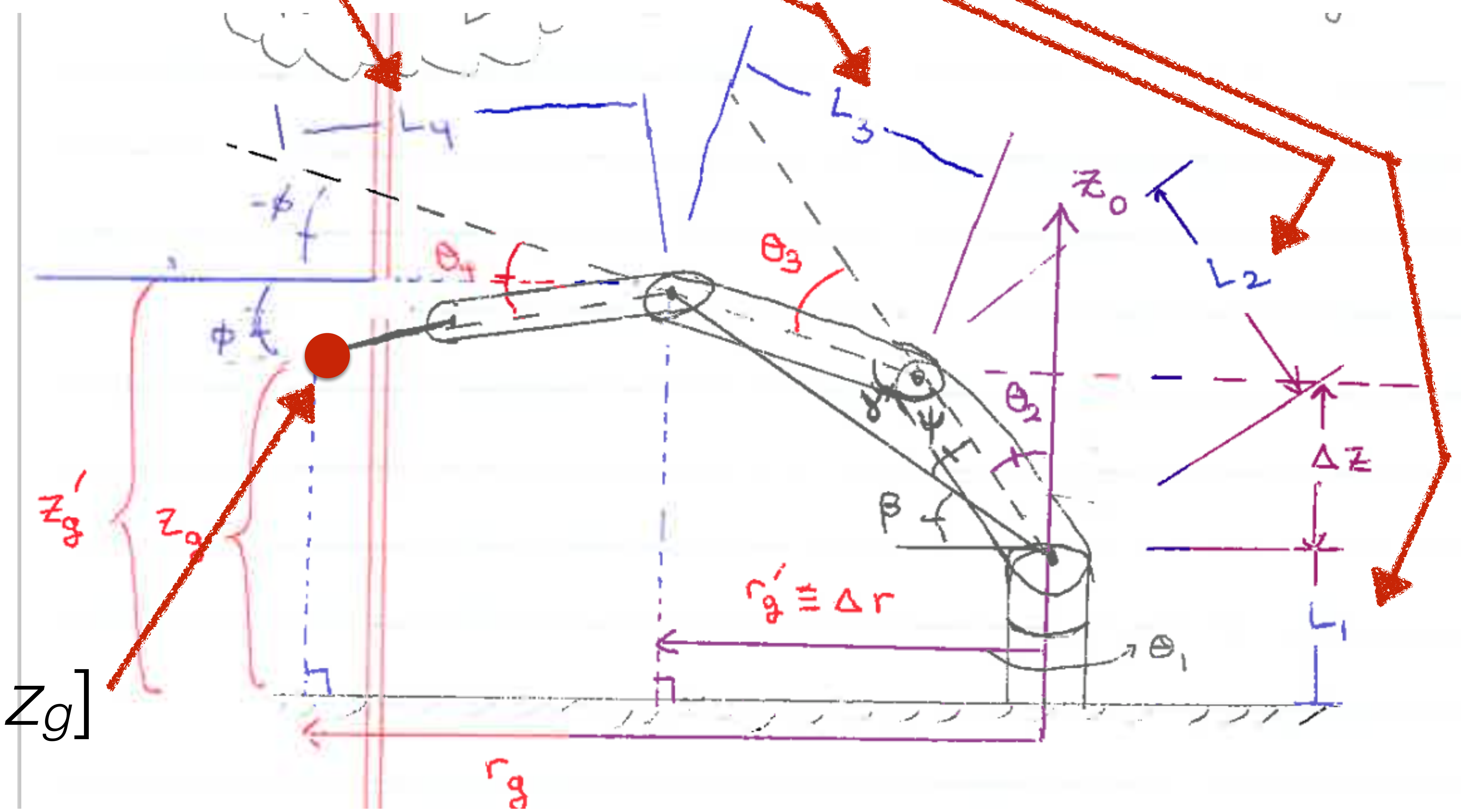
Given:

link lengths (L_4, L_3, L_2, L_1)

Find: configuration

$\boldsymbol{q} = [\boldsymbol{\theta}_1\ \boldsymbol{\theta}_2\ \boldsymbol{\theta}_3\ \boldsymbol{\theta}_4]$

as robot joint angles



endeffector position [$x_g\ y_g\ z_g$] wrt. base frame

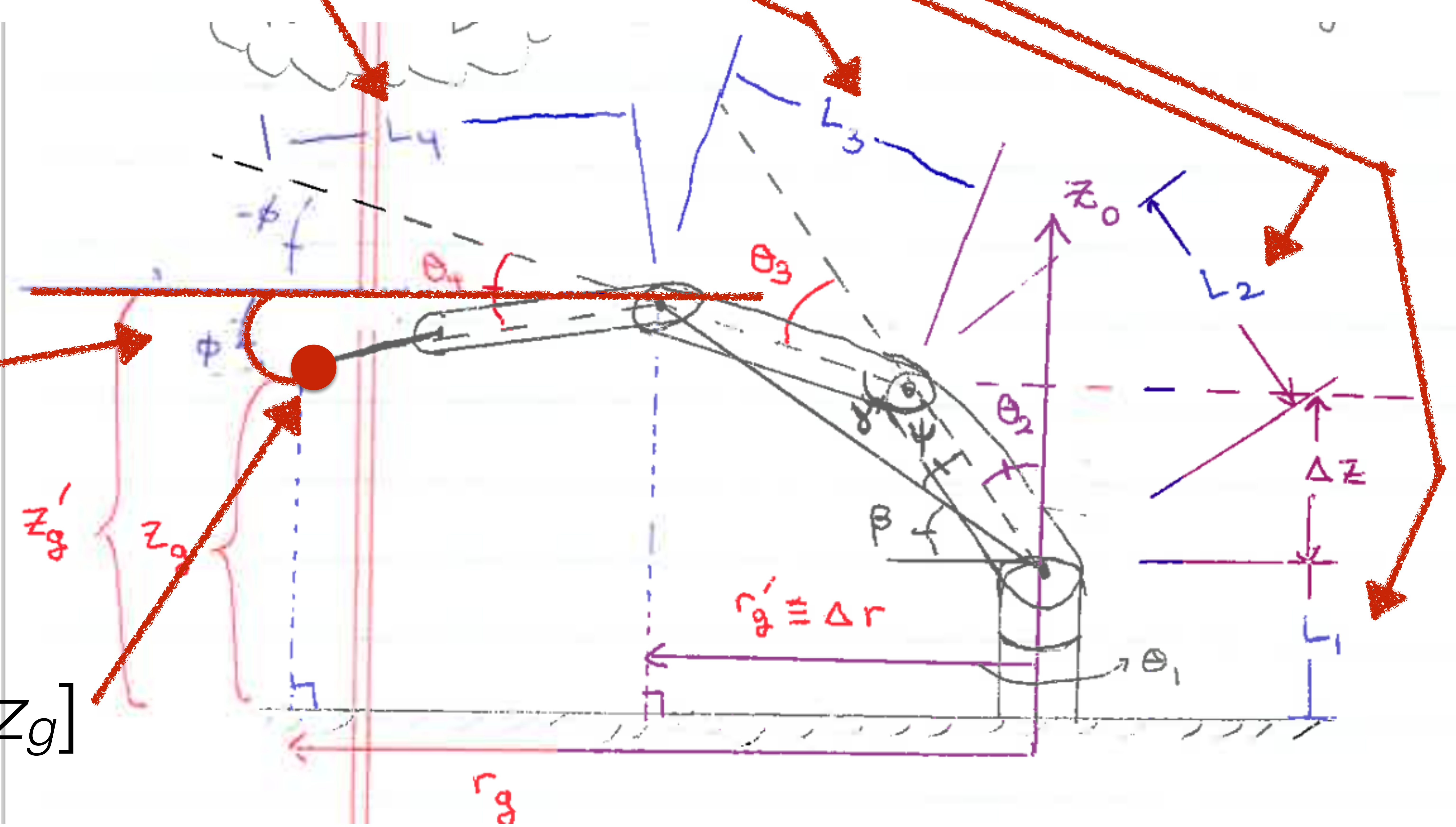
Given:

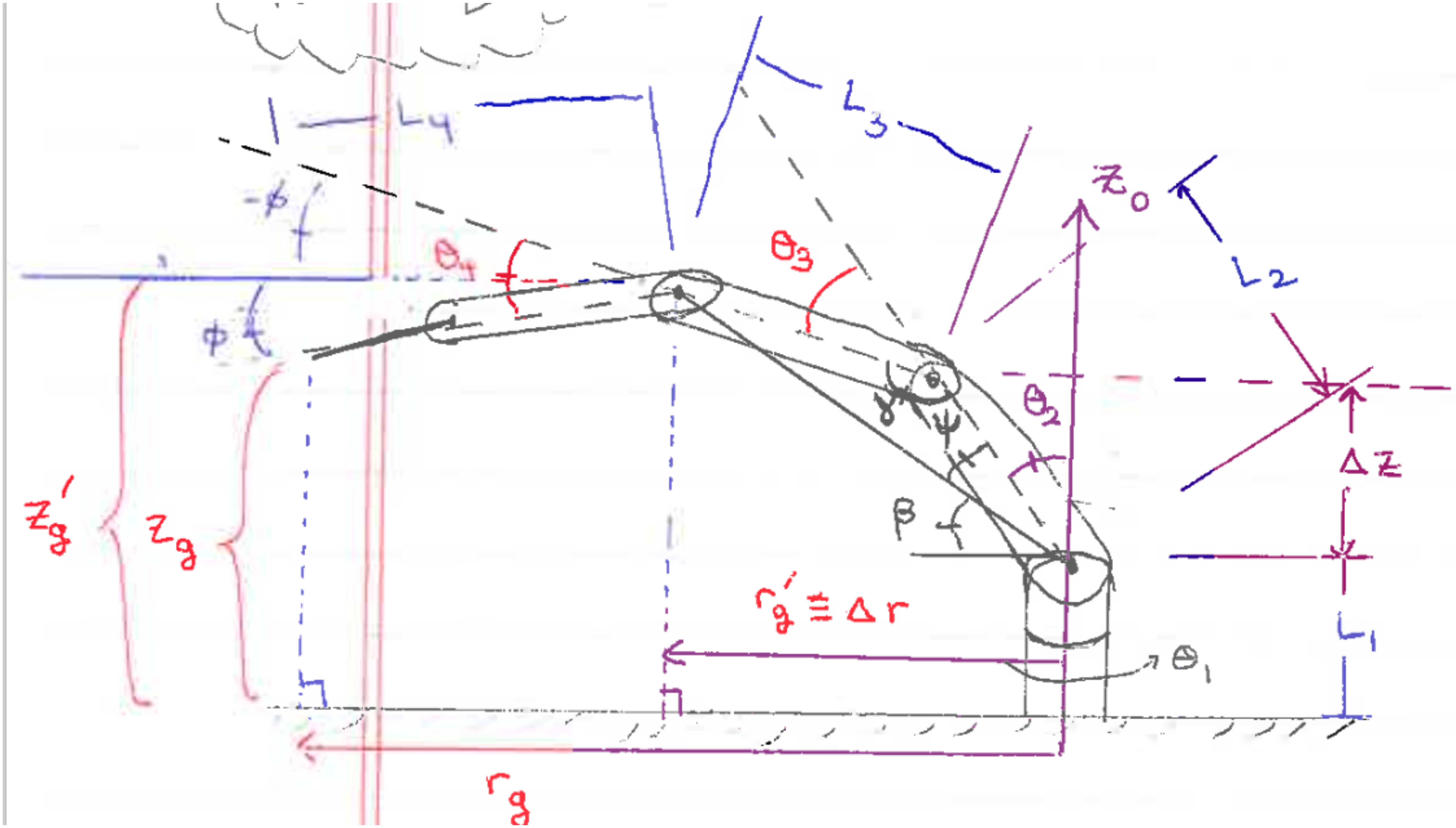
link lengths (L_4,L_3,L_2,L_1)

endeffector orientation ϕ as angle wrt. plane centered at $\boldsymbol{o_3}$ and parallel to ground plane

endeffector position [x_g y_g z_g] wrt. base frame

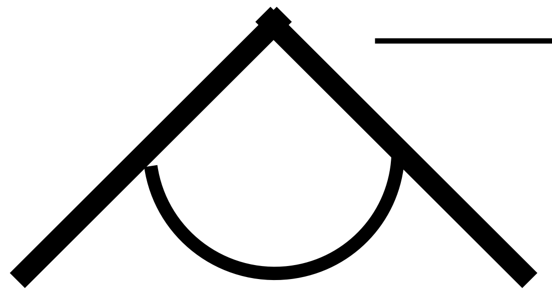
Find: configuration $\boldsymbol{q} = [\boldsymbol{\theta}_1\ \boldsymbol{\theta}_2\ \boldsymbol{\theta}_3\ \boldsymbol{\theta}_4]$ as robot joint angles

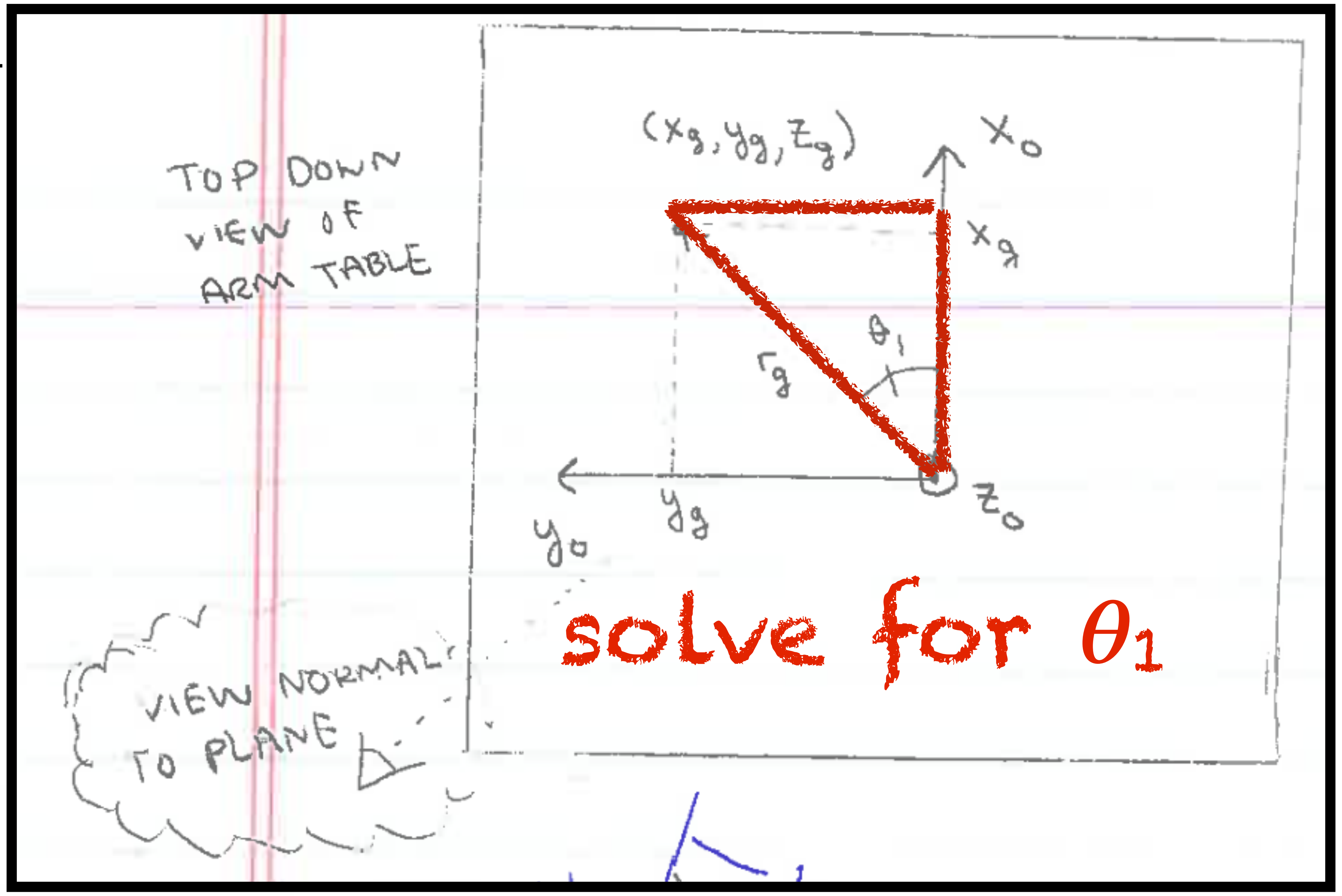


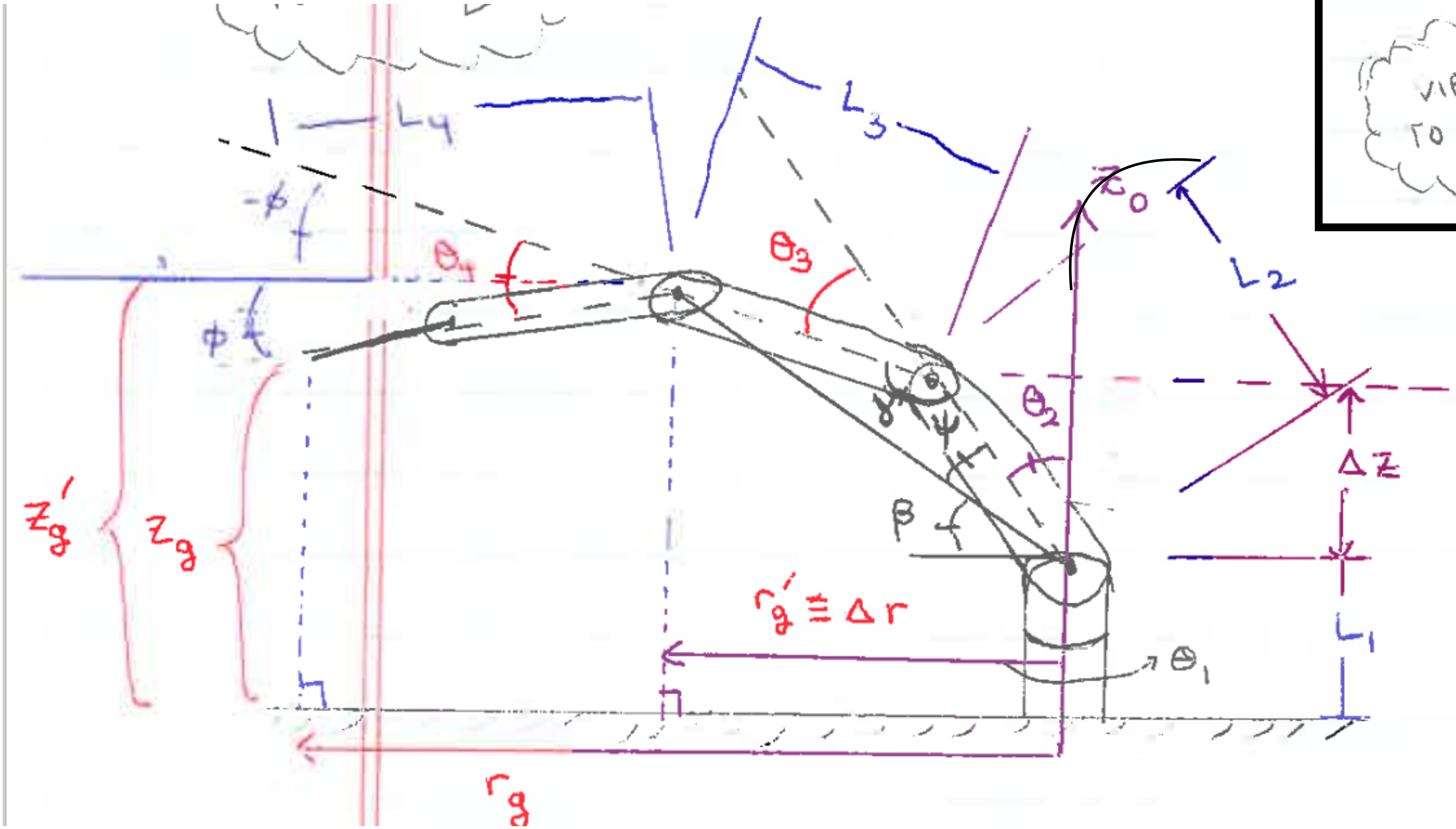


solve for θ_1

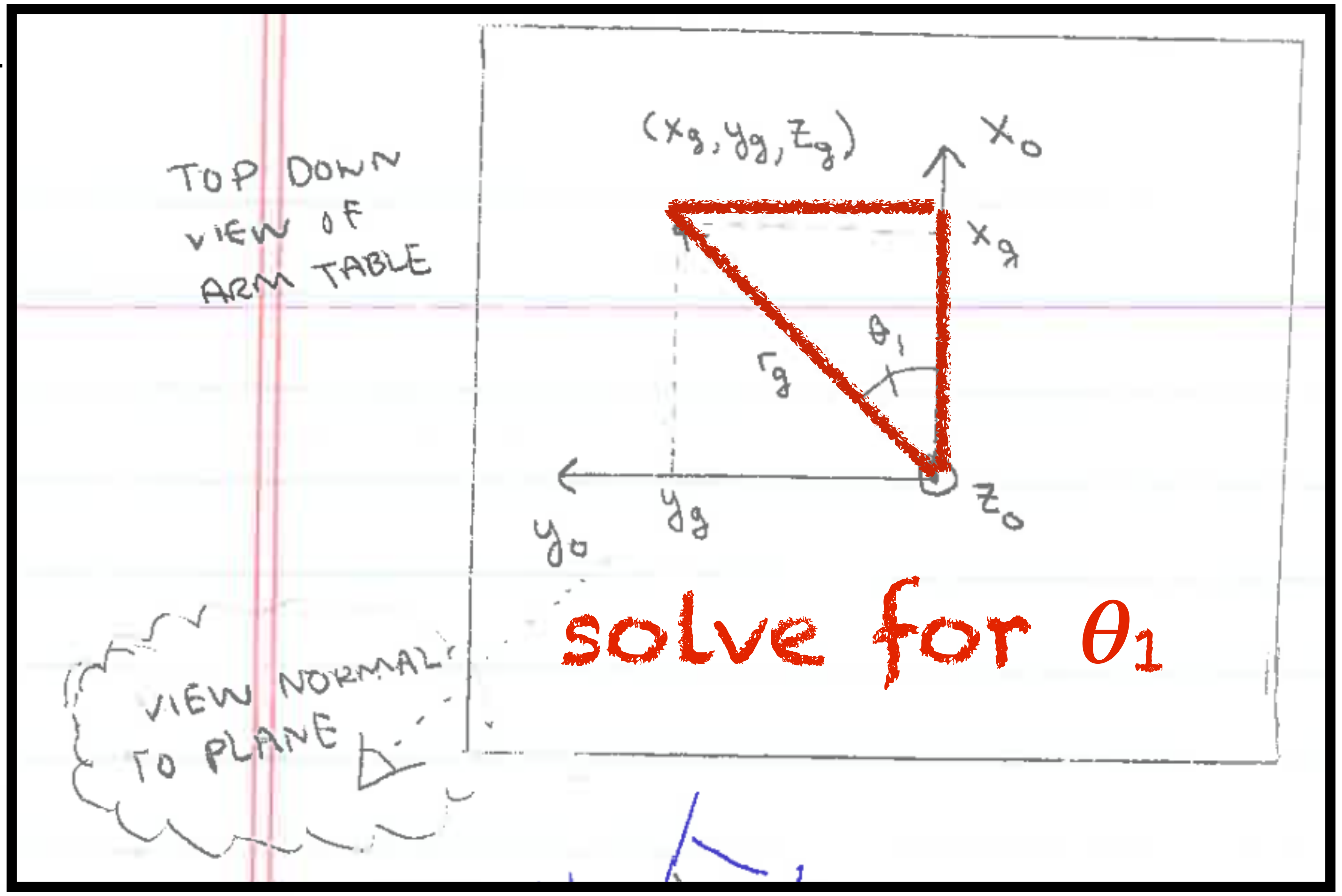
overhead view

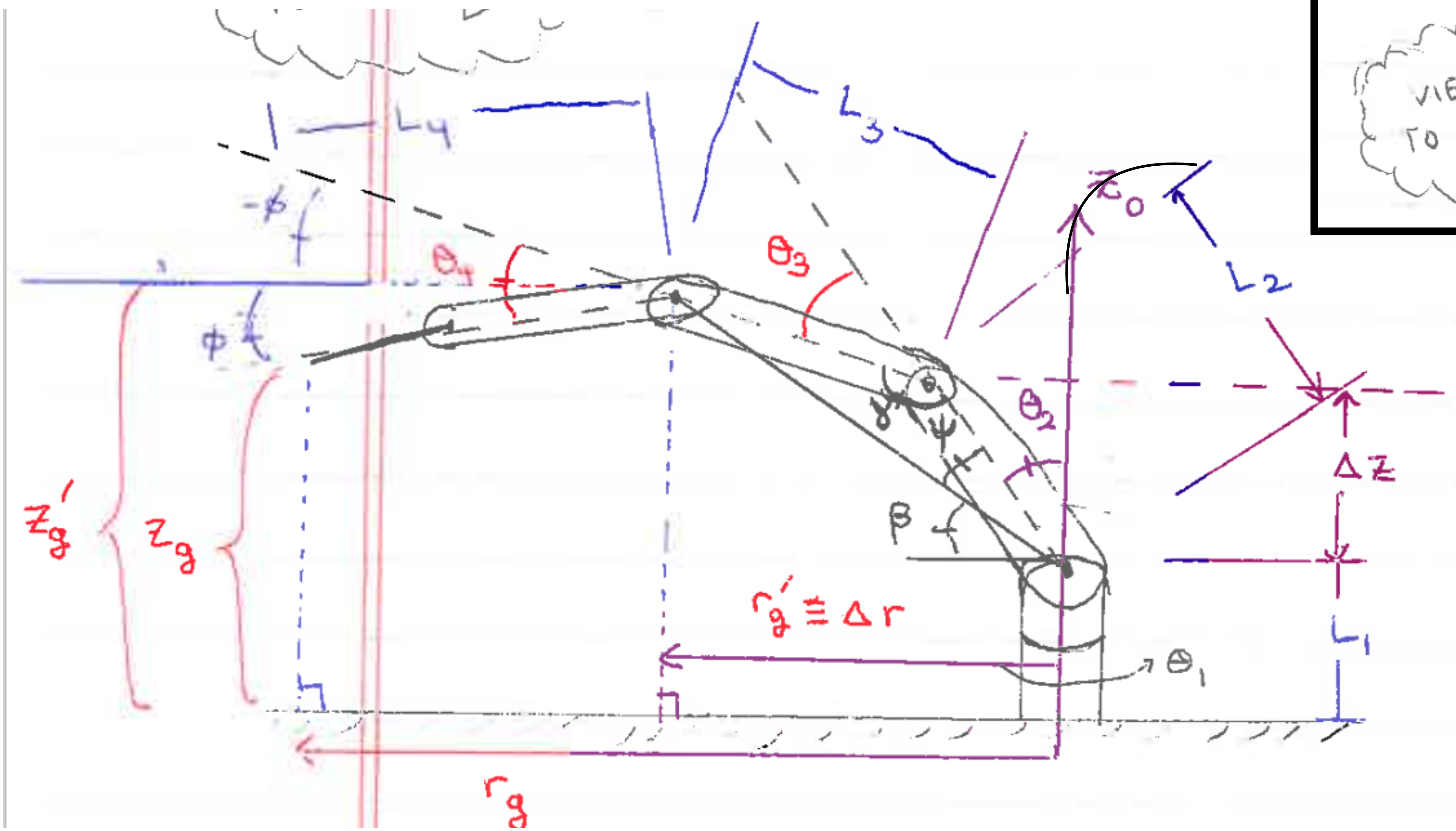






overhead view

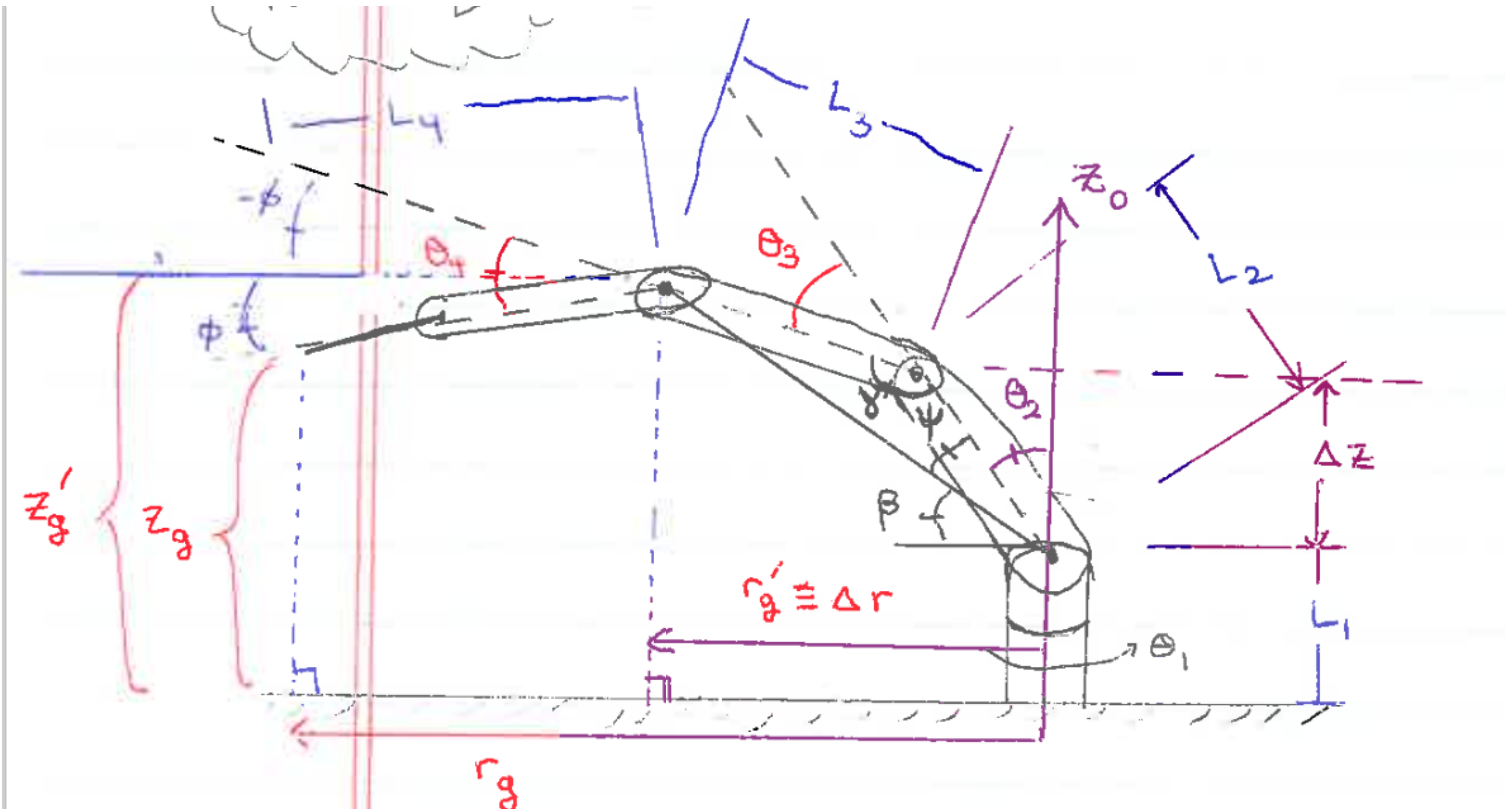




$$\theta_1 = \operatorname{atan2}(y_g, x_g)$$

solve for θ_1

$$\theta_1 = \text{atan2}(y_g, x_g)$$



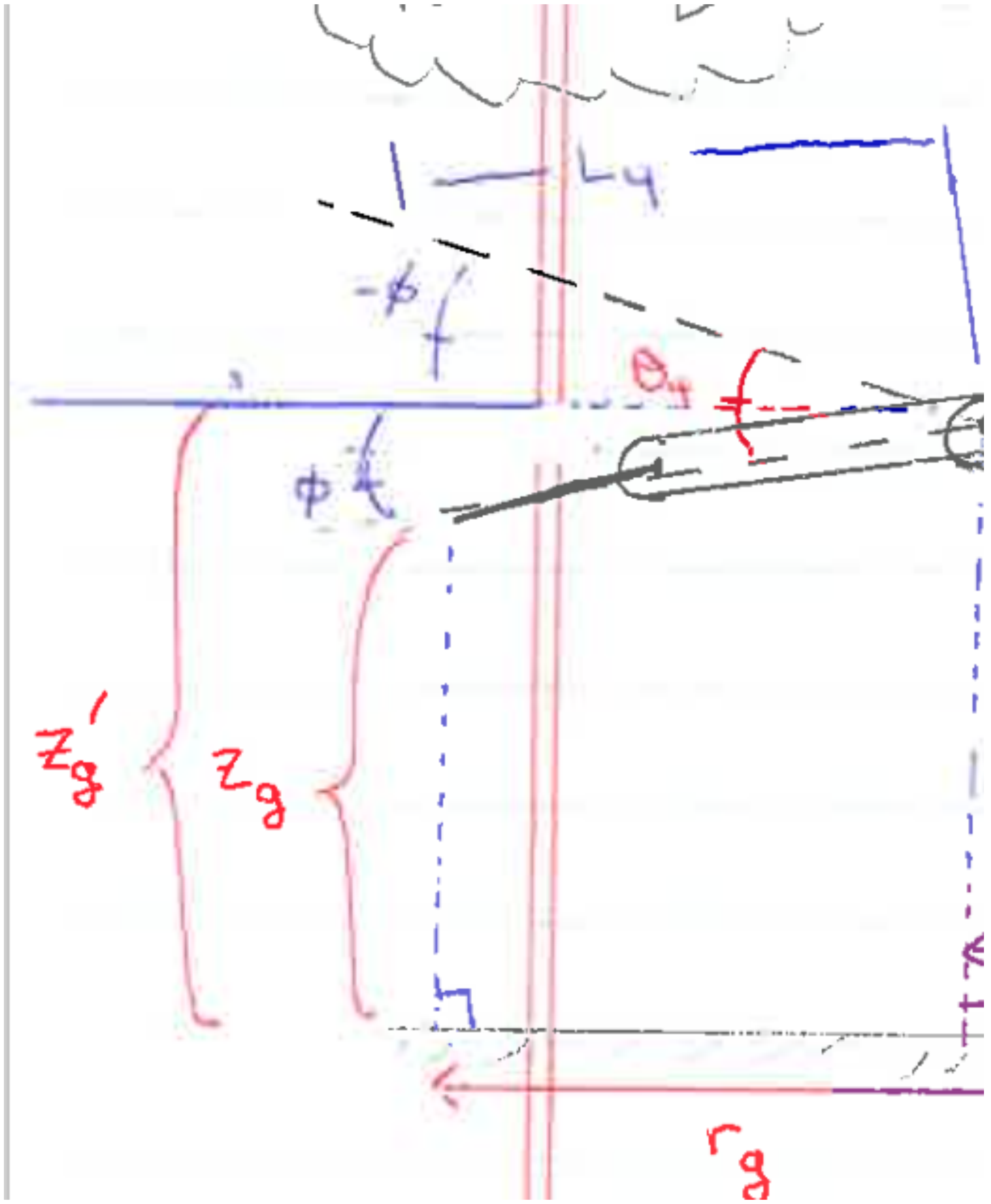
solve for θ_3

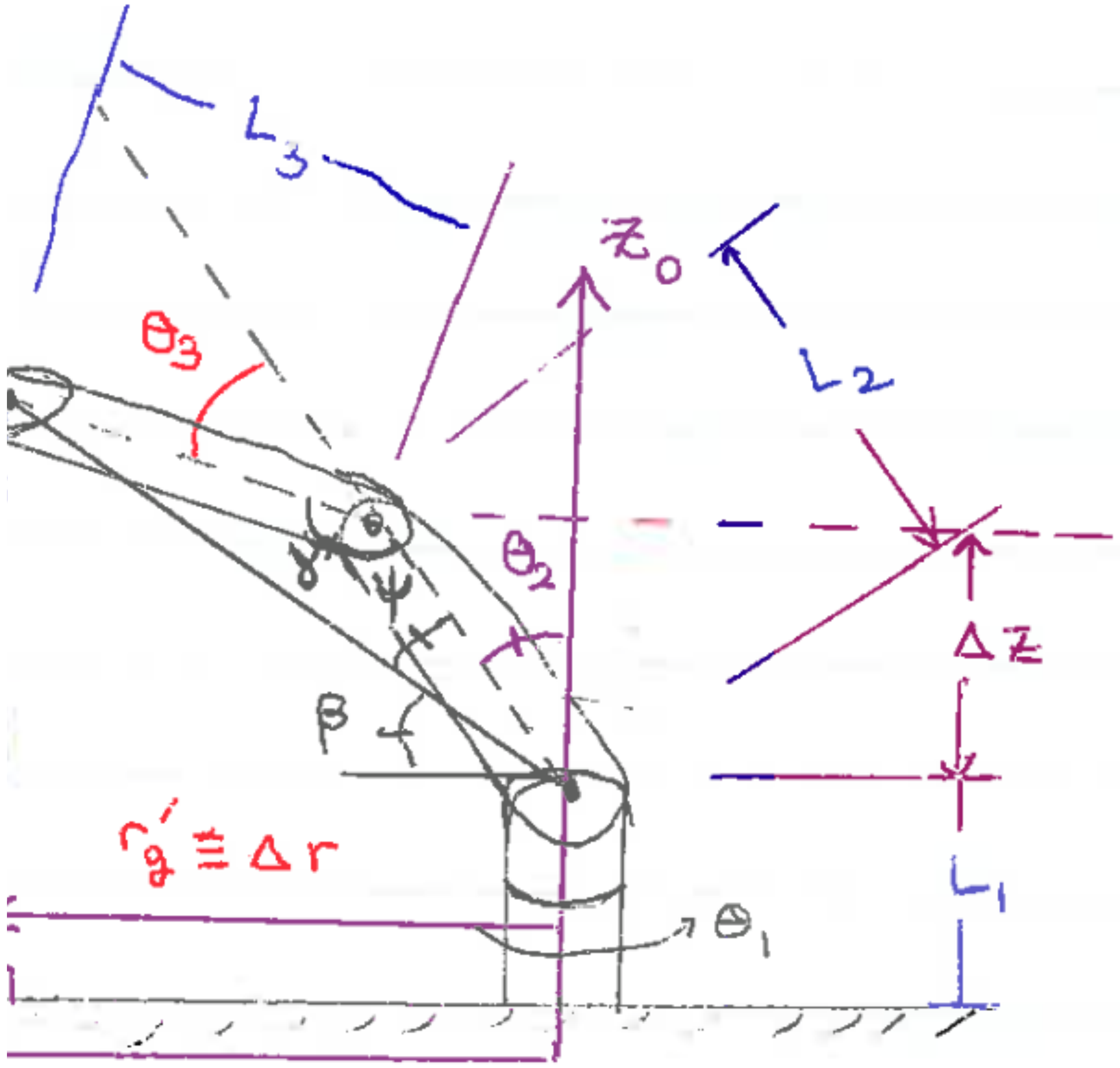
solve for θ_1

$\theta_1 = \text{atan2}(y_g, x_g)$

Decoupling:
separate endeffector from
rest of the robot at last joint

solve for θ_3



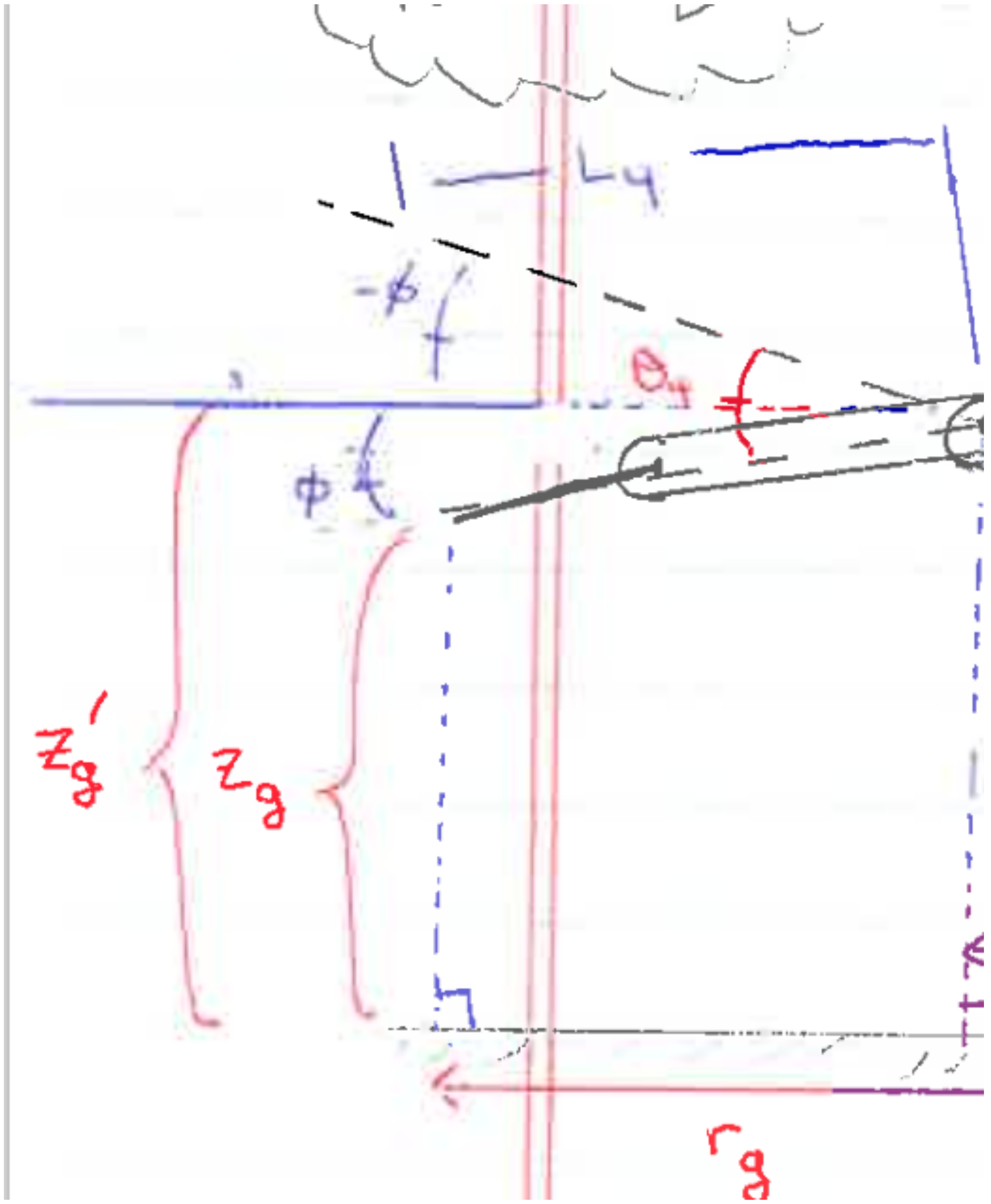


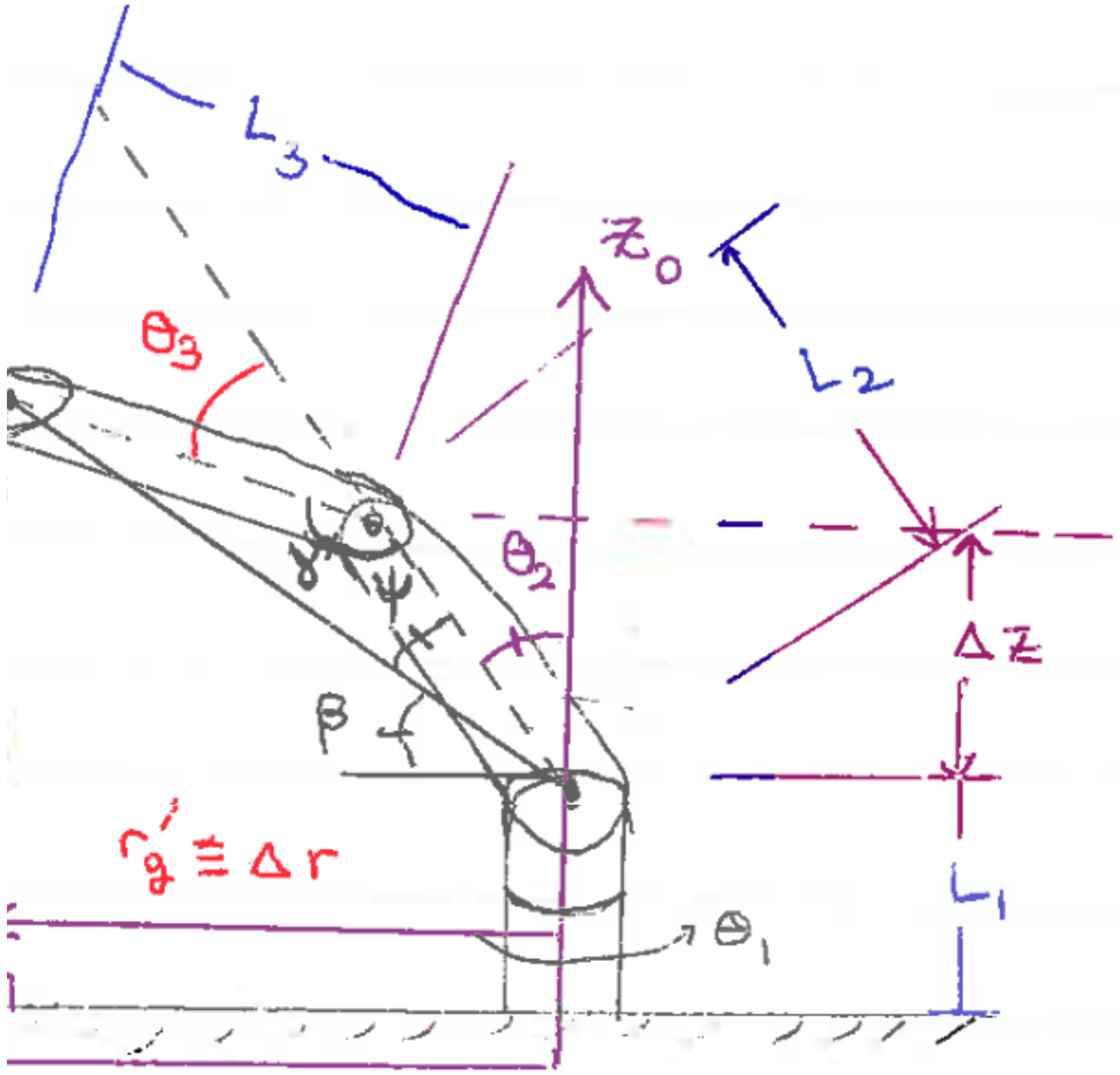
solve for θ_1

$$\theta_1 = \text{atan2}(y_g, x_g)$$

Decoupling:
separate endeffector from
rest of the robot at last joint

solve for θ_3





and…

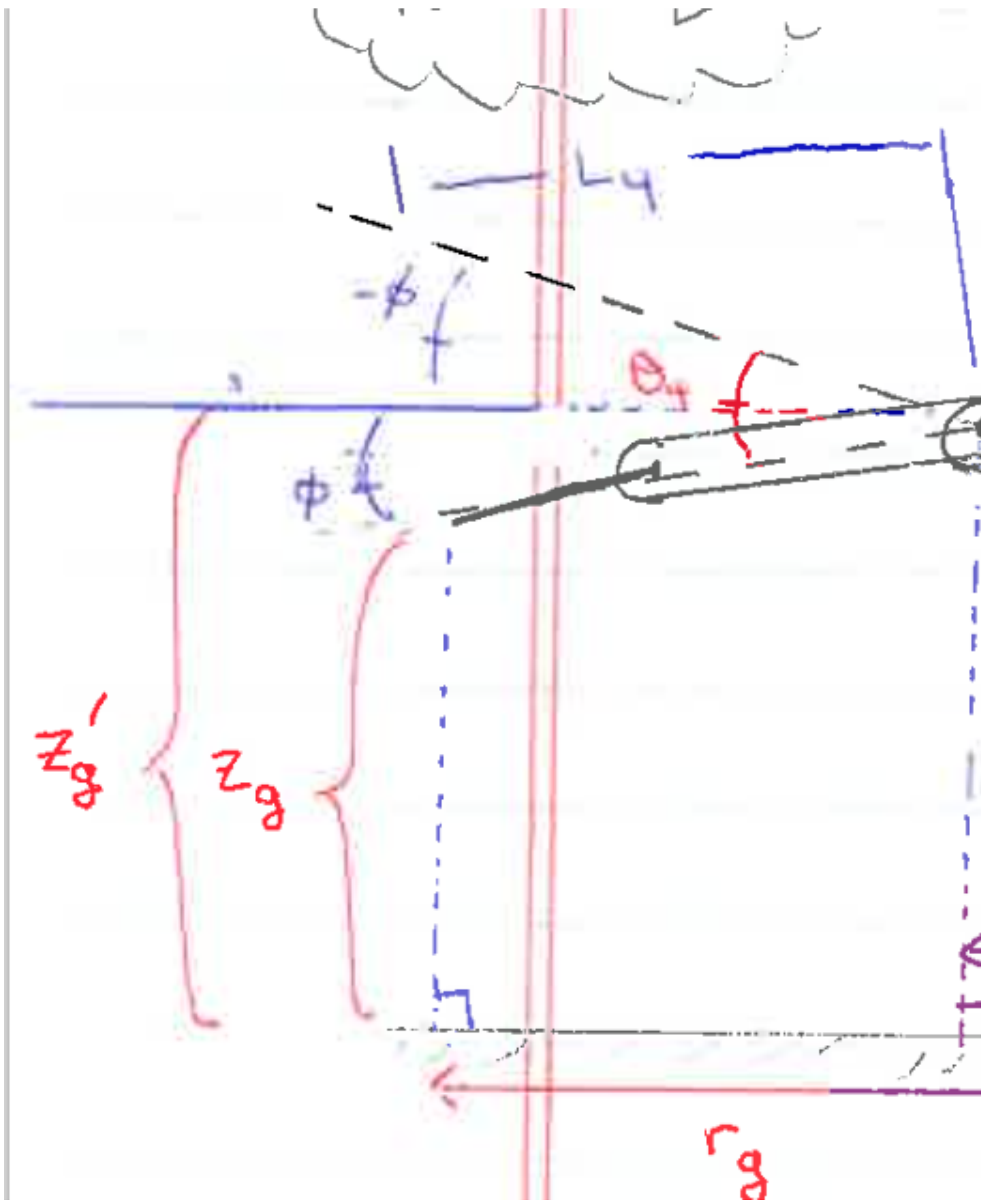
solve for θ_1

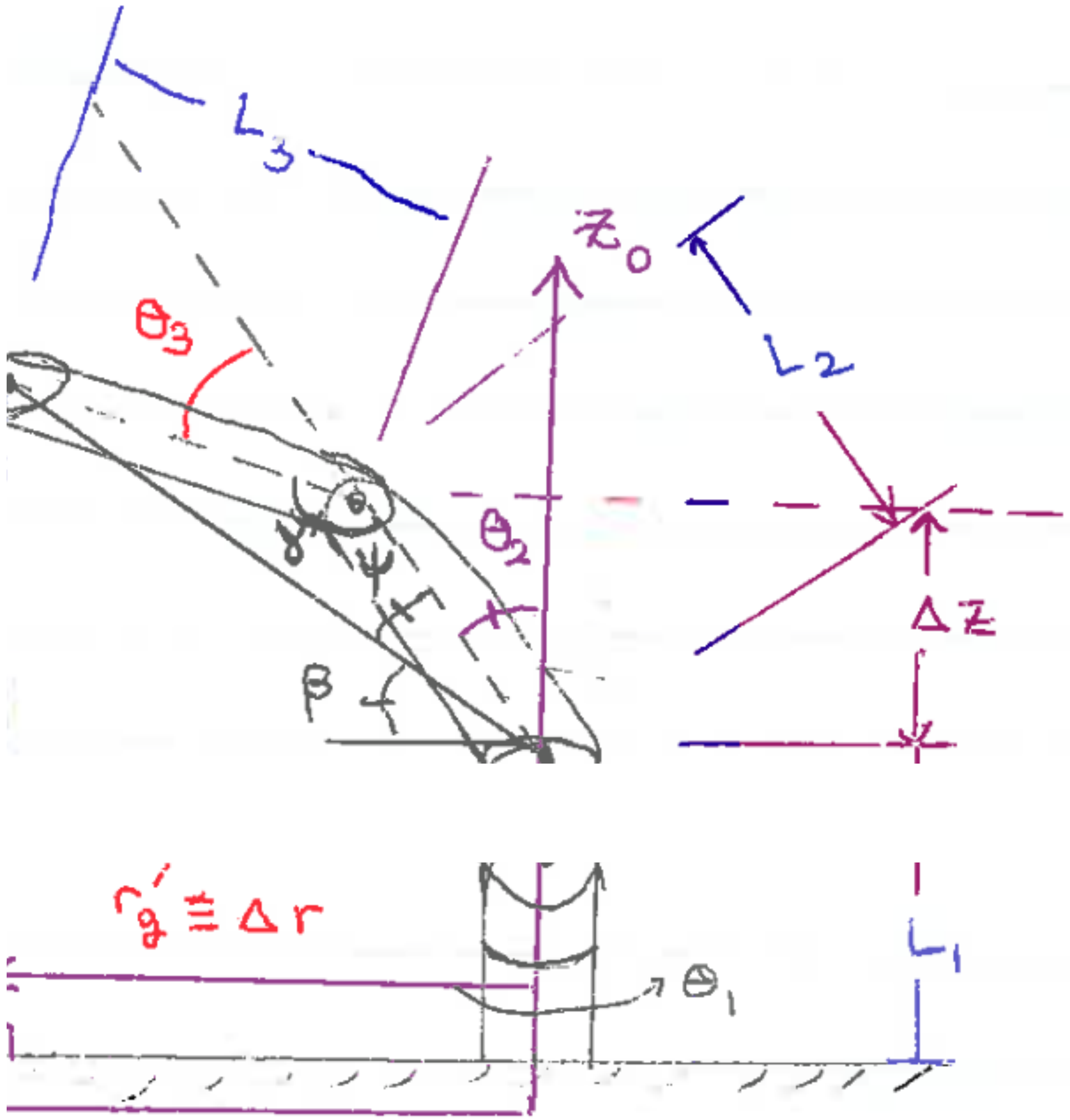
$\theta_1 = \text{atan2}(y_g, x_g)$

Decoupling:

separate endeffector from rest of the robot at last joint

solve for θ_3





and joint 1 from rest of robot

solve for θ_1

$$\theta_1 = \text{atan2}(y_g, x_g)$$

solve for θ_3

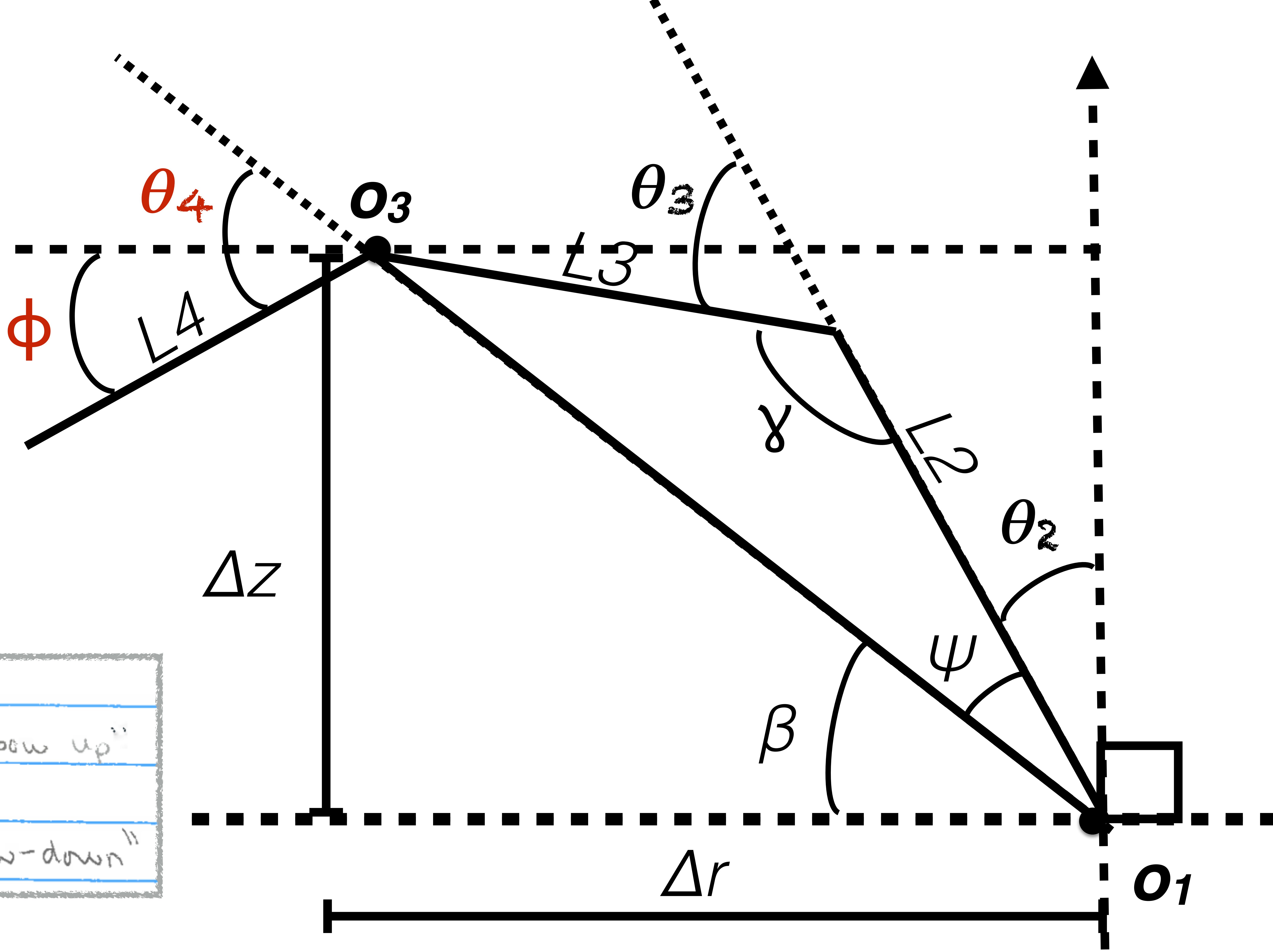
$$\cos\theta_3 = \frac{\Delta z^2 + \Delta r^2 - L_2^2 - L_3^2}{2 L_2 L_3}$$

solve for θ_2

$$\theta_2 = \begin{cases} \frac{\pi}{2} - \beta - \psi & \text{if } \theta_3 > 0 \quad \text{"Elbow up"} \\ \frac{\pi}{2} - \beta + \psi & \text{if } \theta_3 < 0 \quad \text{"Elbow-down"} \end{cases}$$

solve for θ_4

$$\theta_4 = \phi - \theta_2 - \theta_3 + \frac{\pi}{2}$$



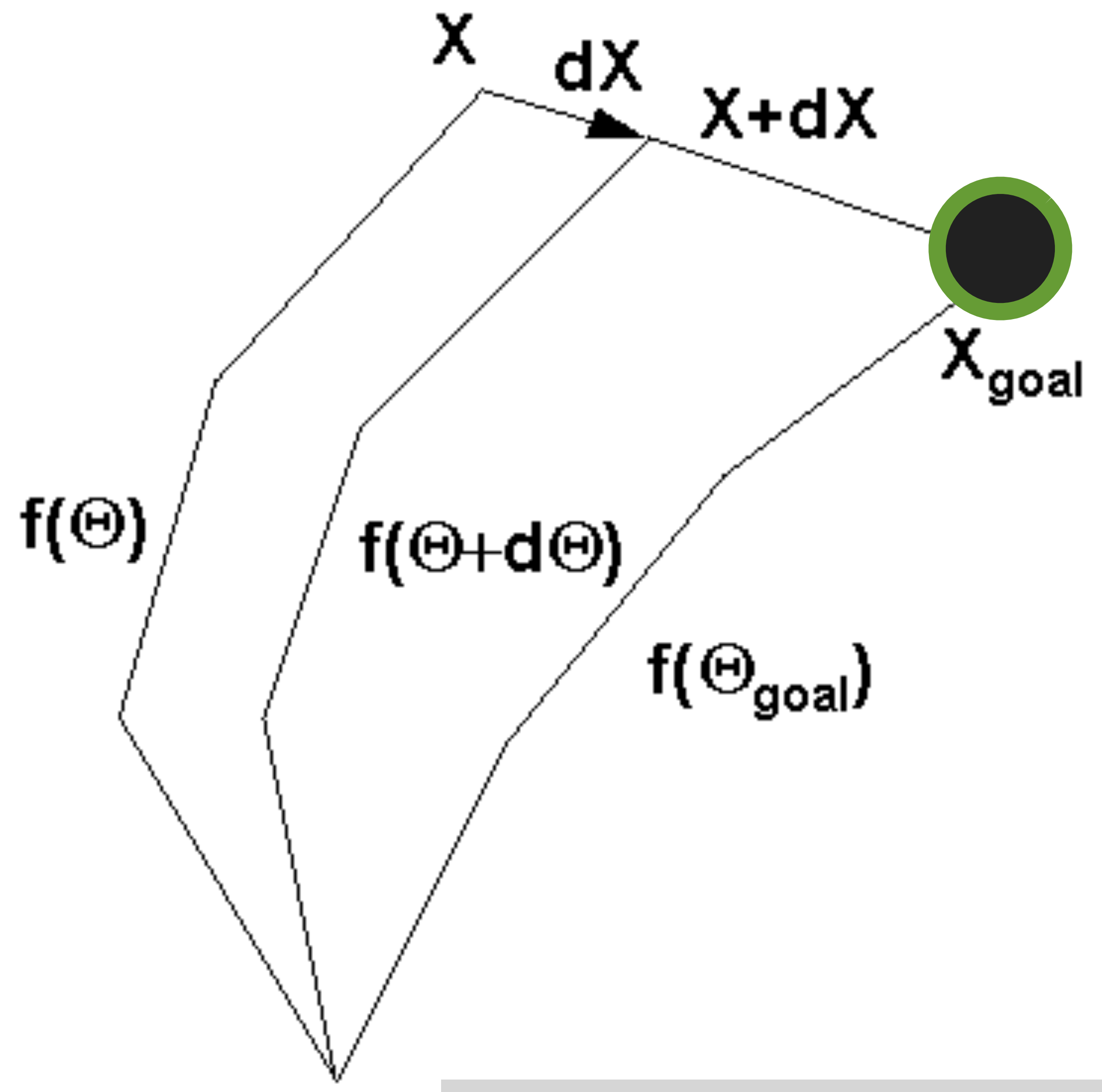
(Addition of angles in arm plane starting from z_0)

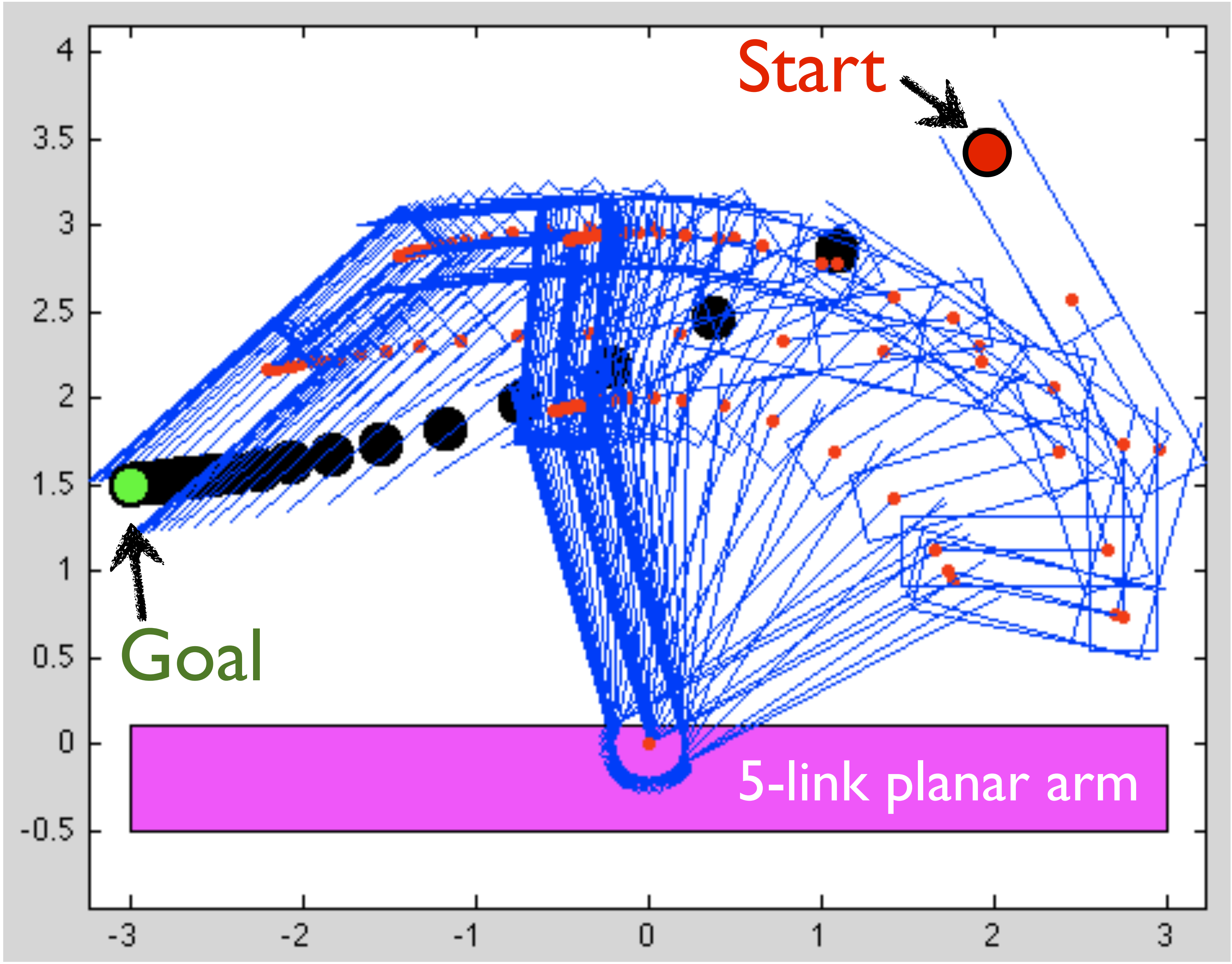
Why Closed Form?

- Advantages
  - Speed: IK solution computed in constant time
  - Predictability: consistency in selecting satisfying IK solution
- Disadvantage
  - Generality: general form for arbitrary kinematics difficult to express

Iterative Solutions to IK

- Minimize error between current endeffector and its desired position
- Transform desired endeffector velocity into configuration space
- Repeatedly step to convergence at desired endeffector position





Inverse Kinematics: 2 possibilites

- **Closed-form solution**: geometrically infer satisfying configuration (Lecture 11)
  - *Speed*: solution often computed in constant time
  - *Predictability*: solution is selected in a consistent manner
- **Solve by optimization**: minimize error of endeffector to desired pose (Lecture 12)
  - often some form of Gradient Descent (a la Jacobian Transpose)
  - *Generality*: same solver can be used for many different robots

Next Class

- IK as an optimization problem
    - Gradient descent optimization
    - Manipulator Jacobian as the derivative of configuration
- Advanced: IK by Cyclic Coordinate Descent

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Inverse Kinematics: Manipulator Jacobian